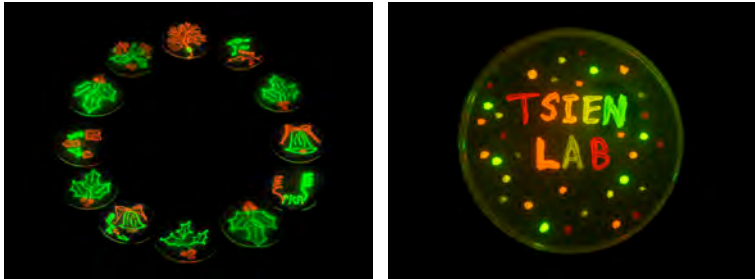
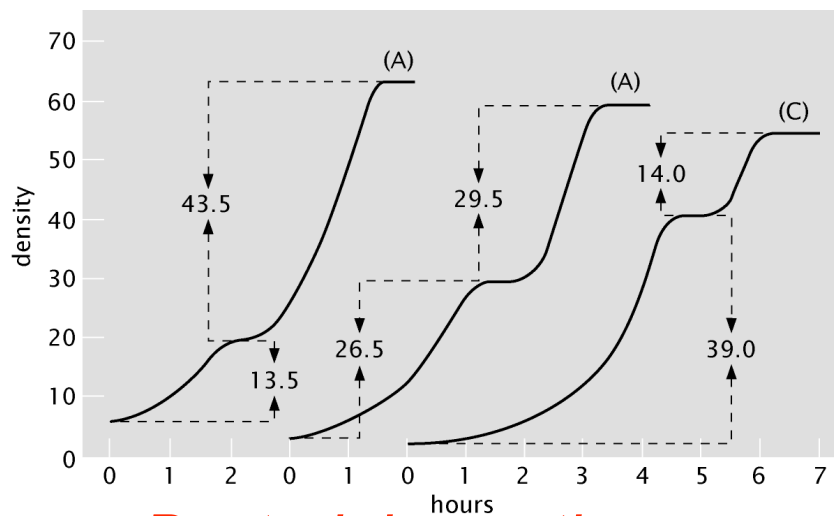
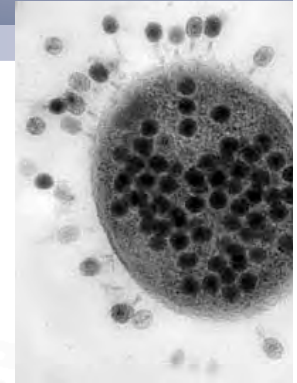


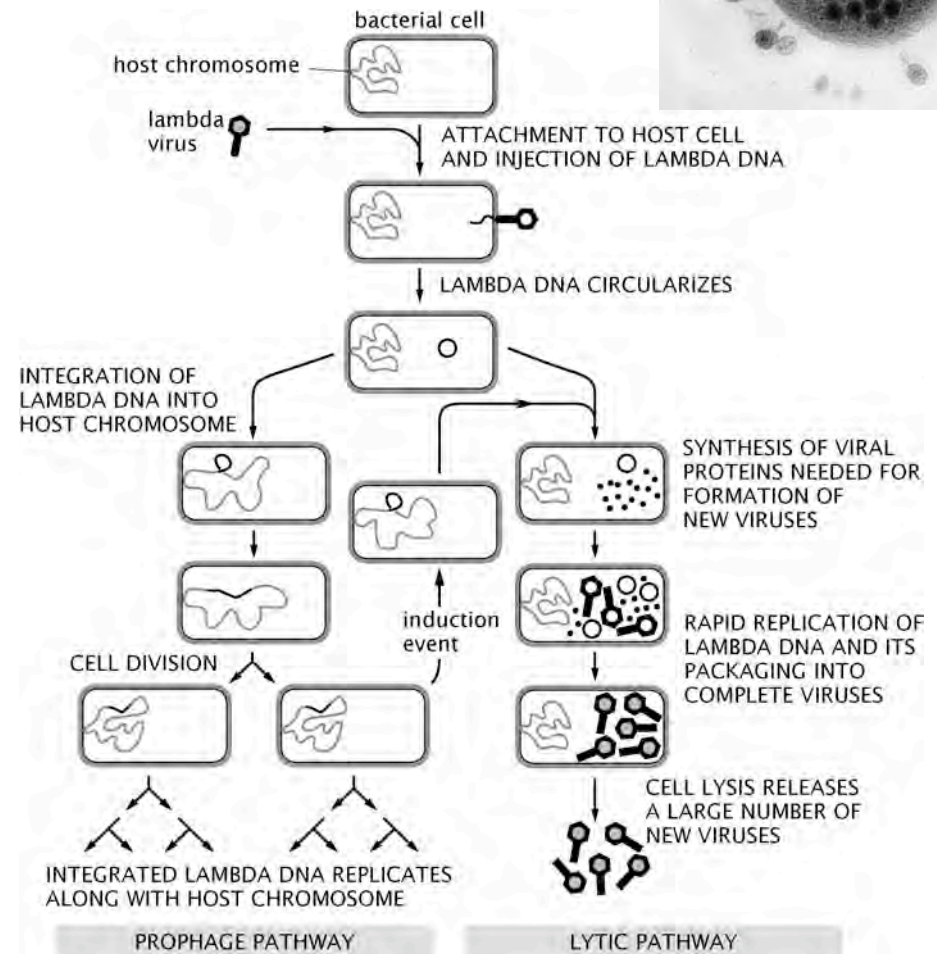
# The Development of the Operon Concept: What Cells Eat and When They Die



• **The big idea: there are genes that control other genes!**



**Bacterial growth curves**



# Exploring Regulatory Diversity

**Table 1**  
Regulation factors for several different regulatory motifs.

| Case                                       | Regulation factor ( $F_{reg}$ )  |
|--|--|
| 1. Simple repressor                        | $(1+r)^{-1}$<br>$\left(1 + \frac{ R }{K_R}\right)^{-1}$  |
| 2. Simple activator                        | $\frac{1 + \frac{a_{10}P}{k_B T}}{1+a}$<br>$\frac{1 + \frac{ A }{K_A} f}{1 + \frac{ A }{K_A}}$   |
| 3. Activator recruited by a helper (H)     | $\frac{1 + \frac{a_{10}P}{k_B T}}{1 + \frac{1 + \frac{a_{10}P}{k_B T}}{1+h}}$<br>$\frac{1 + \frac{ H }{K_H} + \frac{ A }{K_A} f + \frac{ A }{K_A} \frac{ H }{K_H} f_{10}}{1 + \frac{ H }{K_H} + \frac{ A }{K_A} + \frac{ A }{K_A} \frac{ H }{K_H} f_{10}}$   |
| 4. Repressor recruited by a helper (H)     | $\left(1 + \frac{1 + \frac{a_{10}P}{k_B T}}{1+h} r\right)^{-1}$<br>$\frac{1 + \frac{ H }{K_H}}{1 + \frac{ H }{K_H} + \frac{ R }{K_R} + \frac{ R }{K_R} \frac{ H }{K_H} f}$   |
| 5. Dual repressors                         | $(1+r_1)^{-1}(1+r_2)^{-1}$<br>$\left(1 + \frac{ R_1 }{K_{R_1}}\right)^{-1} \left(1 + \frac{ R_2 }{K_{R_2}}\right)^{-1}$  |
| 6. Dual repressors interacting             | $\left(1 + r_1 + r_2 + r_1 r_2 \frac{r_1 r_2}{k_B T}\right)^{-1}$<br>$\left(1 + \frac{ R_1 }{K_{R_1}} + \frac{ R_2 }{K_{R_2}} + \frac{ R_1 }{K_{R_1}} \frac{ R_2 }{K_{R_2}} f\right)^{-1}$   |
| 7. Dual activators interacting             | $\frac{1 + \frac{a_{10}P}{k_B T} + \frac{a_{20}P}{k_B T} + \frac{a_{10}P + a_{20}P}{k_B T}}{1 + a_1 + a_2 + a_1 a_2 \frac{a_{10}P + a_{20}P}{k_B T}}$<br>$\frac{1 + \frac{ A_1 }{K_{A_1}} f_1 + \frac{ A_2 }{K_{A_2}} f_2 + \frac{ A_1 }{K_{A_1}} \frac{ A_2 }{K_{A_2}} f_{12}}{1 + \frac{ A_1 }{K_{A_1}} + \frac{ A_2 }{K_{A_2}} + \frac{ A_1 }{K_{A_1}} \frac{ A_2 }{K_{A_2}} f_{12}}$ |
| 8. Dual activators cooperating via looping | $\frac{1 + \frac{a_{10}P}{k_B T} + \frac{a_{20}P}{k_B T} + \frac{a_{10}P + a_{20}P}{k_B T} + \frac{F_{loop}}{k_B T}}{(1+a_1)(1+a_2)}$<br>$\frac{1 + \frac{ A_1 }{K_{A_1}} f_1 + \frac{ A_2 }{K_{A_2}} f_2 + \frac{ A_1 }{K_{A_1}} \frac{ A_2 }{K_{A_2}} f_{12}}{\left(1 + \frac{ A_1 }{K_{A_1}}\right) \left(1 + \frac{ A_2 }{K_{A_2}}\right)}$  |
| 9. Repressor                               |  |
| 10. N no                                   |  |

**Better census needed!**

P = number of RNAP molecules  
≈ 10,000 ~ 1,000

R = number of repressor molecules  
≈ 10

A = number of activator molecules  
≈ 1,000

DNA Promoter Gene of interest

Regulatory symbol i in terms of regulatory TF we in the conc the RNA

**Key point: We can work out the regulation factor for many other scenarios including other looping scenarios.**



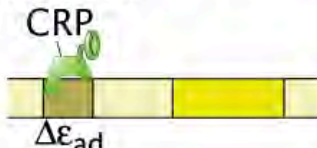
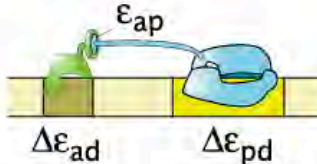
| STATE | WEIGHT   |
|-------|--|
|       | 1  |
|       | $\frac{P}{N_{ns}} e^{-\Delta\epsilon_{pd}}$  |
|       | $\frac{A}{N_{ns}} e^{-\Delta\epsilon_{a_1d}}$  |
|       | $\frac{A}{N_{ns}} e^{-\Delta\epsilon_{a_2d}}$  |
|       | $\frac{A}{N_{ns}} \frac{A}{N_{ns}} e^{-(\Delta\epsilon_{a_1d} + \Delta\epsilon_{a_2d})}$   |
|       | $\frac{P}{N_{ns}} \frac{A}{N_{ns}} e^{-(\Delta\epsilon_{pd} + \Delta\epsilon_{a_1d} + \epsilon_{a_1p})}$   |
|       | $\frac{P}{N_{ns}} \frac{A}{N_{ns}} e^{-(\Delta\epsilon_{pd} + \Delta\epsilon_{a_2d} + \Delta\epsilon_{a_2p})}$   |
|       | $\frac{P}{N_{ns}} \frac{A}{N_{ns}} \frac{A}{N_{ns}} e^{-(\Delta\epsilon_{pd} + \Delta\epsilon_{a_1d} + \Delta\epsilon_{a_2d} + \epsilon_{a_1p} + \epsilon_{a_2p} + F_{loop})}$ |

**Synergistic Activation**

# How Should We Think About Regulation Quantitatively?

“Thermodynamic Models” –  
Equilibrium Notions

Rate Equation Perspective

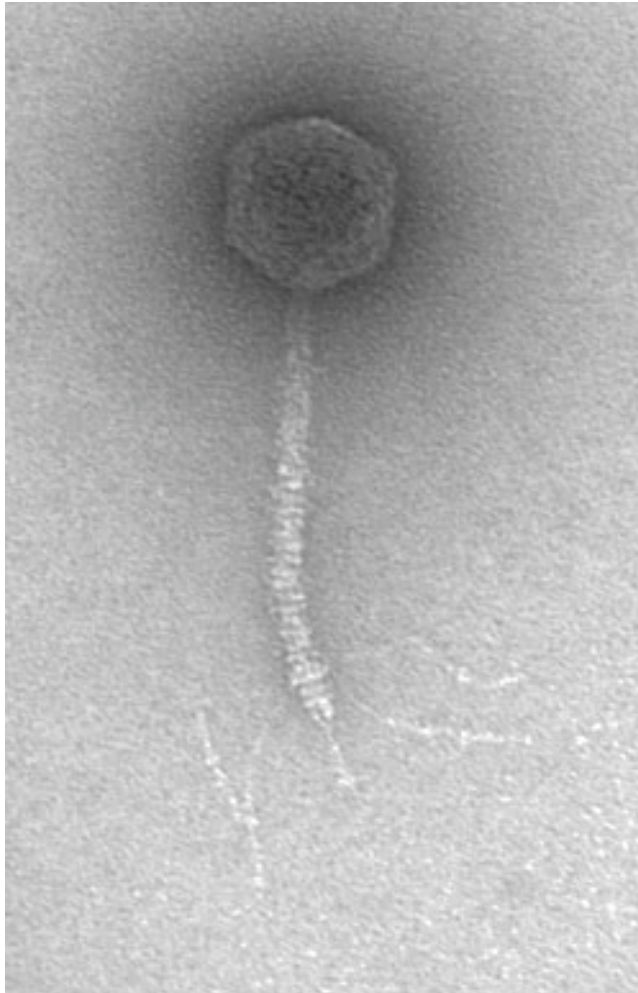
| STATE   | WEIGHT   |
|---|--|
|  <p>Activator binding site</p>   | 1  |
|  <p>activated</p> <p><math>\Delta\epsilon_{pd}</math></p>  | $\frac{P}{N_{NS}} e^{-\Delta\epsilon_{pd}/k_B T}$  |
|  <p>CRP</p> <p><math>\Delta\epsilon_{ad}</math></p>  | $\frac{A}{N_{NS}} e^{-\Delta\epsilon_{ad}/k_B T}$  |
|  <p><math>\Delta\epsilon_{ad}</math></p> <p><math>\epsilon_{ap}</math></p> <p><math>\Delta\epsilon_{pd}</math></p> | $\frac{P}{N_{NS}} \frac{A}{N_{NS}} e^{-(\Delta\epsilon_{pd} + \Delta\epsilon_{ad} + \epsilon_{ap})/k_B T}$ |

$$\begin{aligned} \frac{d[\text{mRNA}_{\text{Rep}}]}{dt} &= V_{\text{mRNA-Rep}} - (k_{\text{d,mRNA-Rep}} + \mu) \cdot [\text{mRNA}_{\text{Rep}}] \\ \frac{d[\text{Rep}]}{dt} &= V_{\text{Rep}} - (k_{\text{d,Rep}} + \mu) \cdot [\text{Rep}] \\ \frac{d[\text{mRNA}_{\text{ZYA}}]}{dt} &= V_{\text{mRNA-ZYA}} - (k_{\text{d,mRNA-ZYA}} + \mu) \cdot [\text{mRNA}_{\text{ZYA}}] \\ \frac{d[\beta\text{gal}]}{dt} &= V_{\beta\text{gal}} - (k_{\text{d}} + \mu) \cdot [\beta\text{gal}] \\ \frac{d[\text{Perm}]}{dt} &= V_{\text{Perm}} - (k_{\text{d}} + \mu) \cdot [\text{Perm}] \\ \frac{d[\text{Lac}_{\text{out}}]}{dt} &= V_{\text{Lac}} - V_{\text{cat,Lac}} - V_{\text{Lac-Allo}} - \mu \cdot [\text{Lac}_{\text{out}}] \\ \frac{d[\text{Allo}]}{dt} &= V_{\text{Lac-Allo}} - V_{\text{cat,Allo}} - \mu \cdot [\text{Allo}] \\ \frac{d[\text{cAMP}]}{dt} &= V_{\text{cAMP}} - (k_{\text{cat}} + \mu) \cdot [\text{cAMP}] \\ \frac{d[\text{Glu}_{\text{out}}]}{dt} &= (V_{\text{out,Glu}} - V_{\text{in,Glu}}) \cdot X \\ \frac{d[\text{Lac}_{\text{cat}}]}{dt} &= -V_{\text{in,Lac}} \cdot X \\ \frac{dX}{dt} &= \mu X \\ \frac{d[\text{Glu6P}]}{dt} &= V_{\text{in,Glu}} + 2 \cdot (V_{\text{cat,Lac}} + V_{\text{cat,Allo}}) - \frac{\mu}{Y_{X/\text{Glu6P}}} - \mu \cdot [\text{Glu6P}] \end{aligned}$$

Wong, Gladney, and Keasling



# *The Lambda Switch: The Other Hydrogen Atom of Gene Regulation*

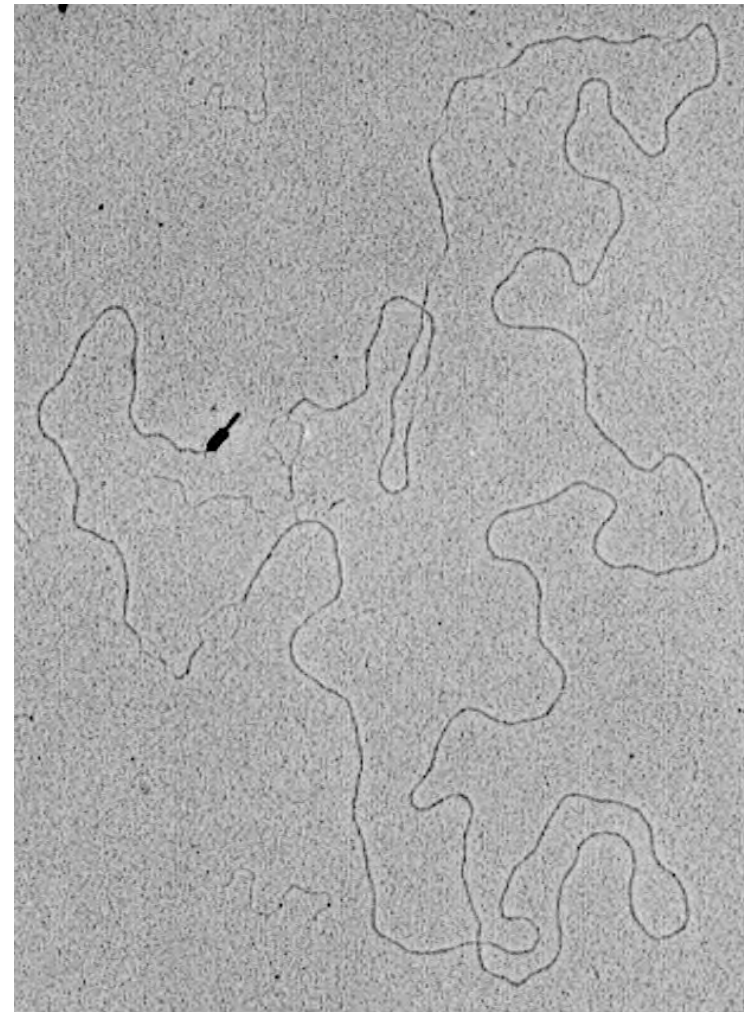
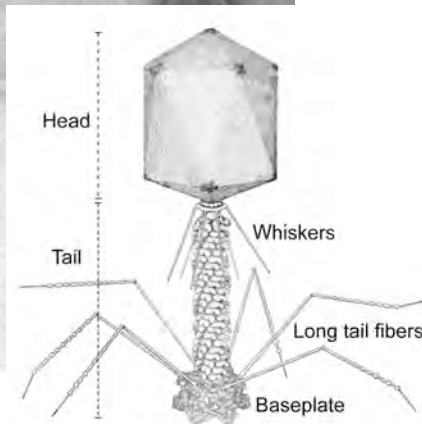
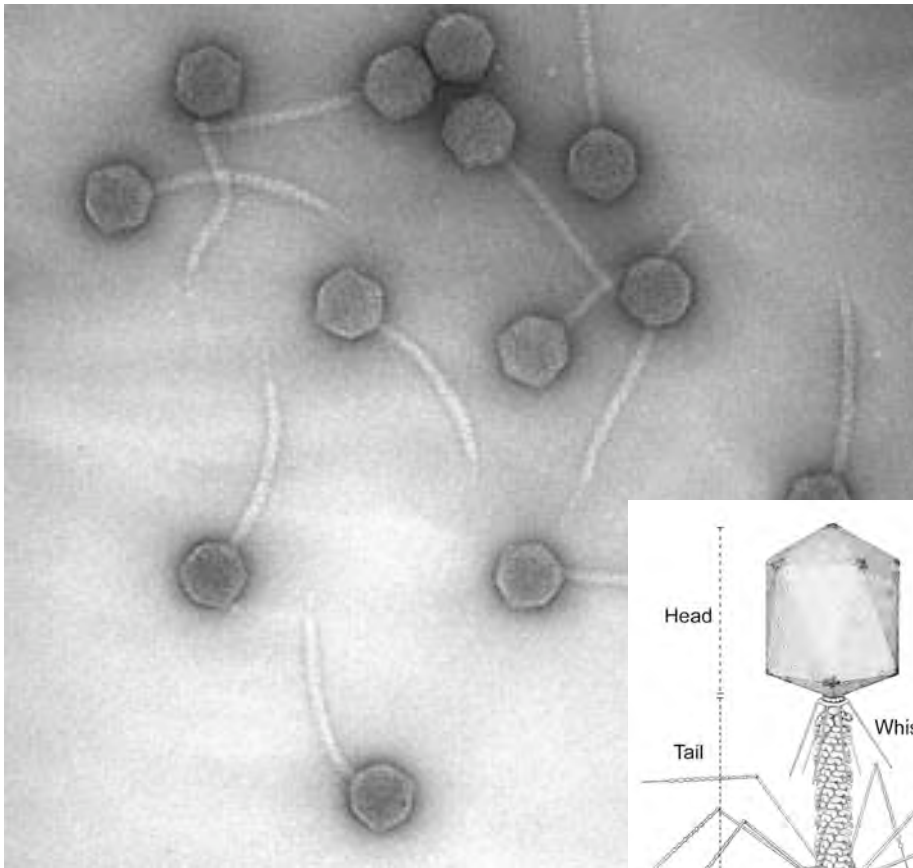


Roger Hendrix

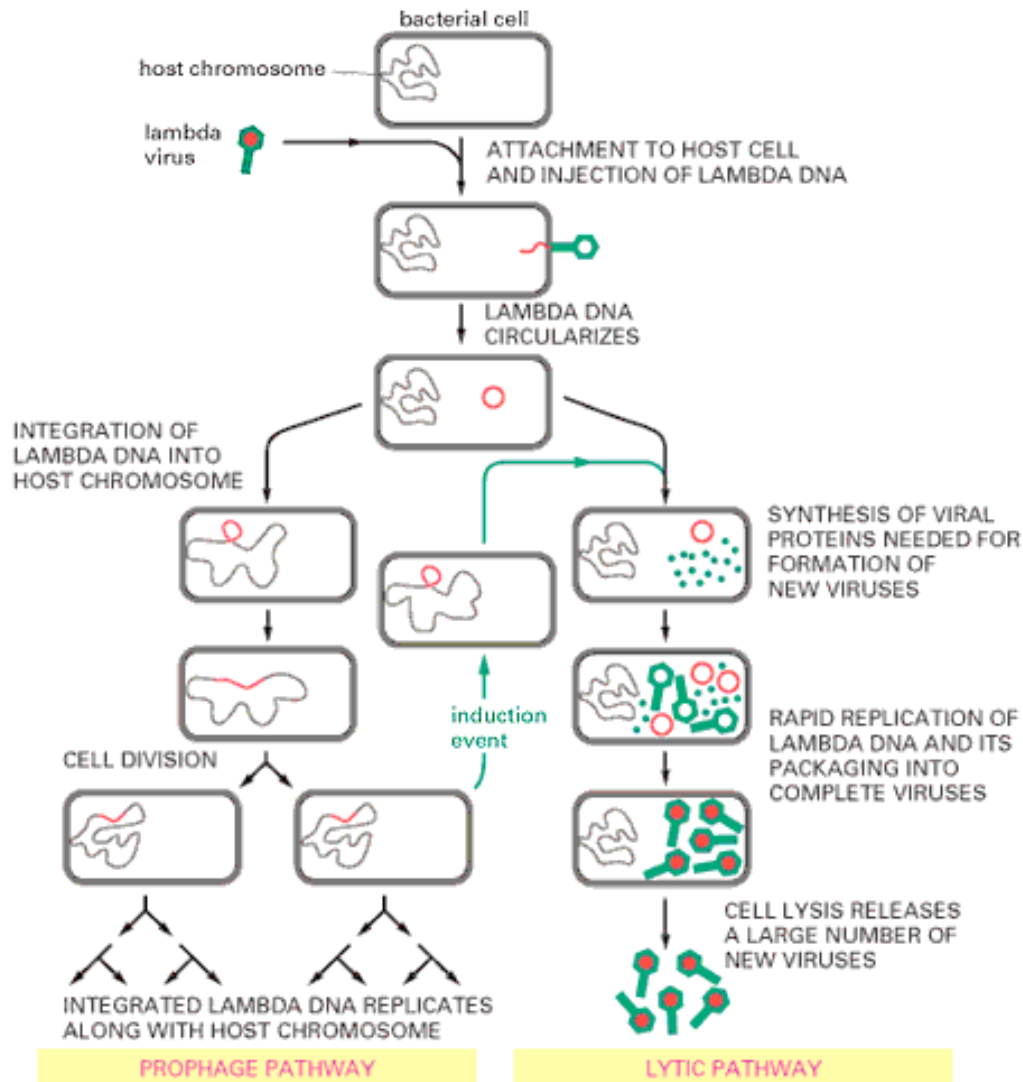


# Bacteriophage and Their Genomes

<http://www.biochem.wisc.edu/inman/empics/0020b.j>

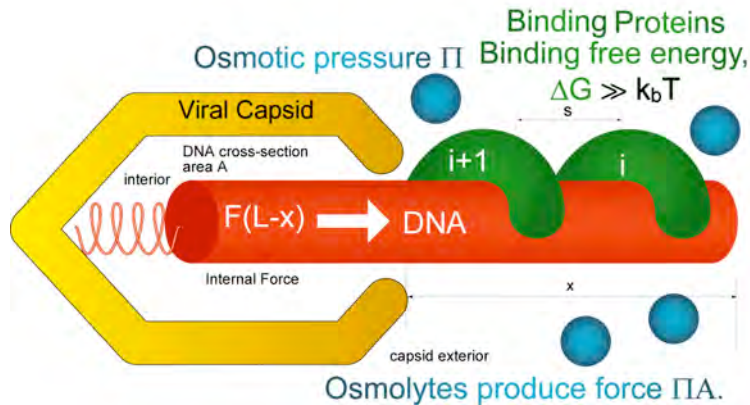


# The Life Cycle of Bacteriophage Lambda

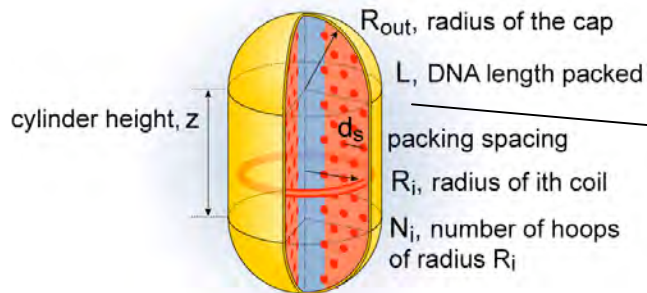




# Physical Consequences of the Tight Squeeze in the Life Cycle of a Bacteriophage

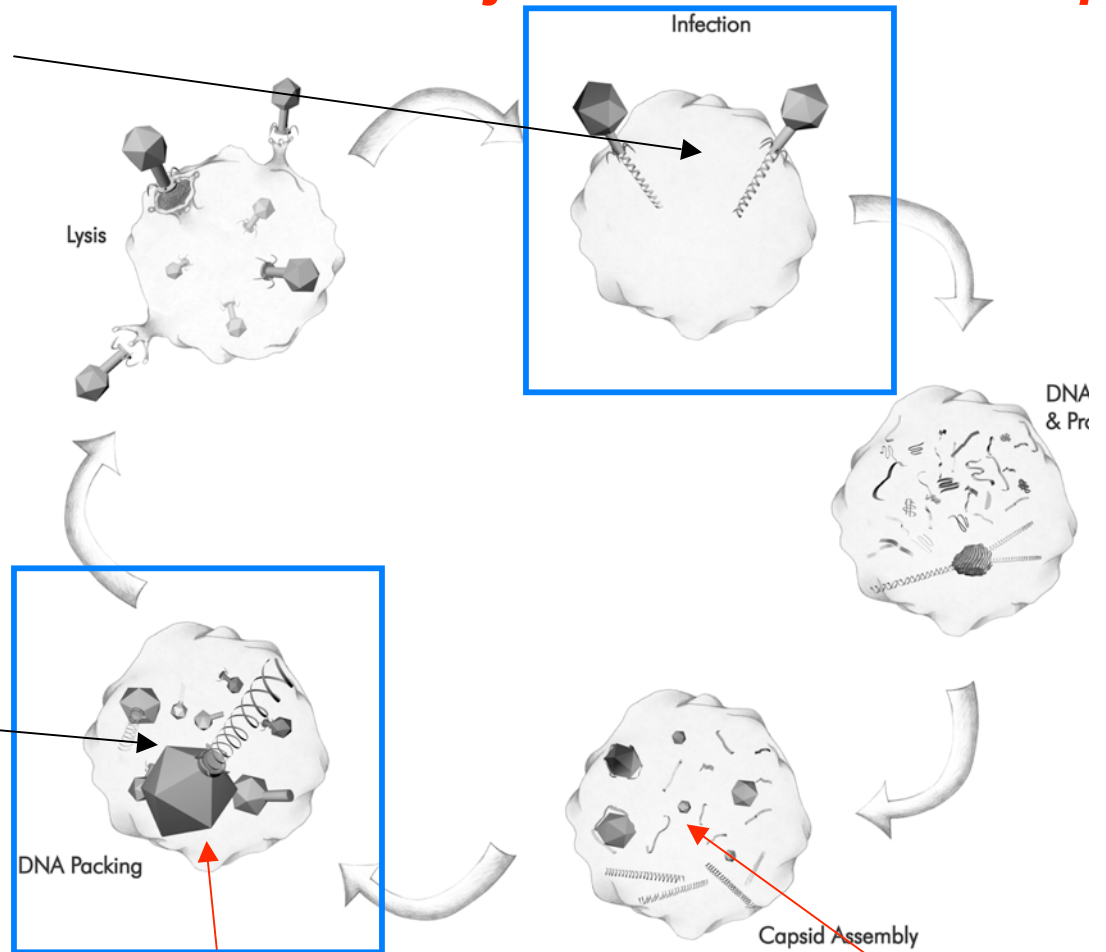


**Forceful ejection**



**Construct a physical model of these processes.**

**Rate of ejection:  $\approx 100 - 1000 \text{ bp/s}$**



**Rate of packing:  $100 \text{ bp/sec}$   
"Some assembly required"**

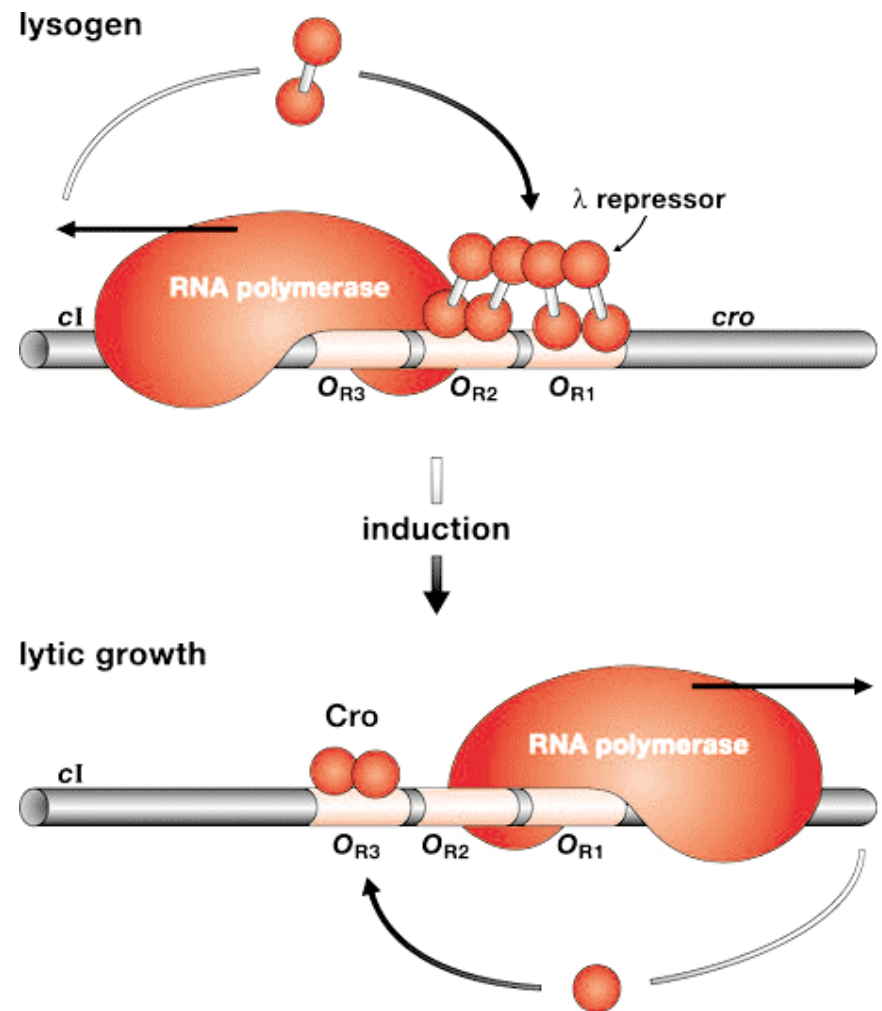
**Self-assembly**

# A Genetic Switch

**A  
GENETIC  
SWITCH**  
Third Edition  
Phage Lambda Revisited



MARK PTASHNE

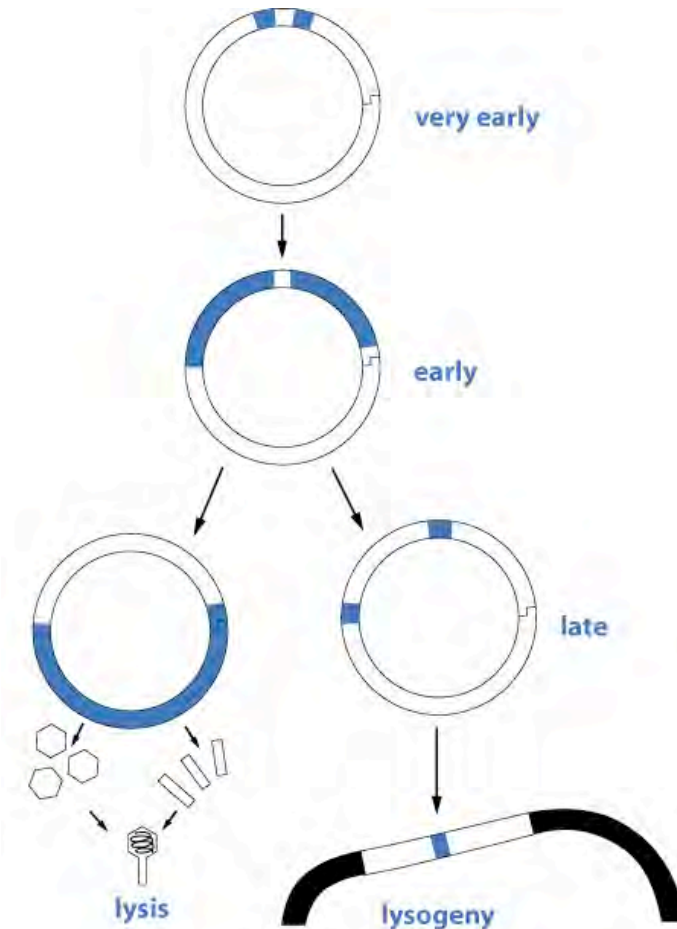




# The Lambda Genome

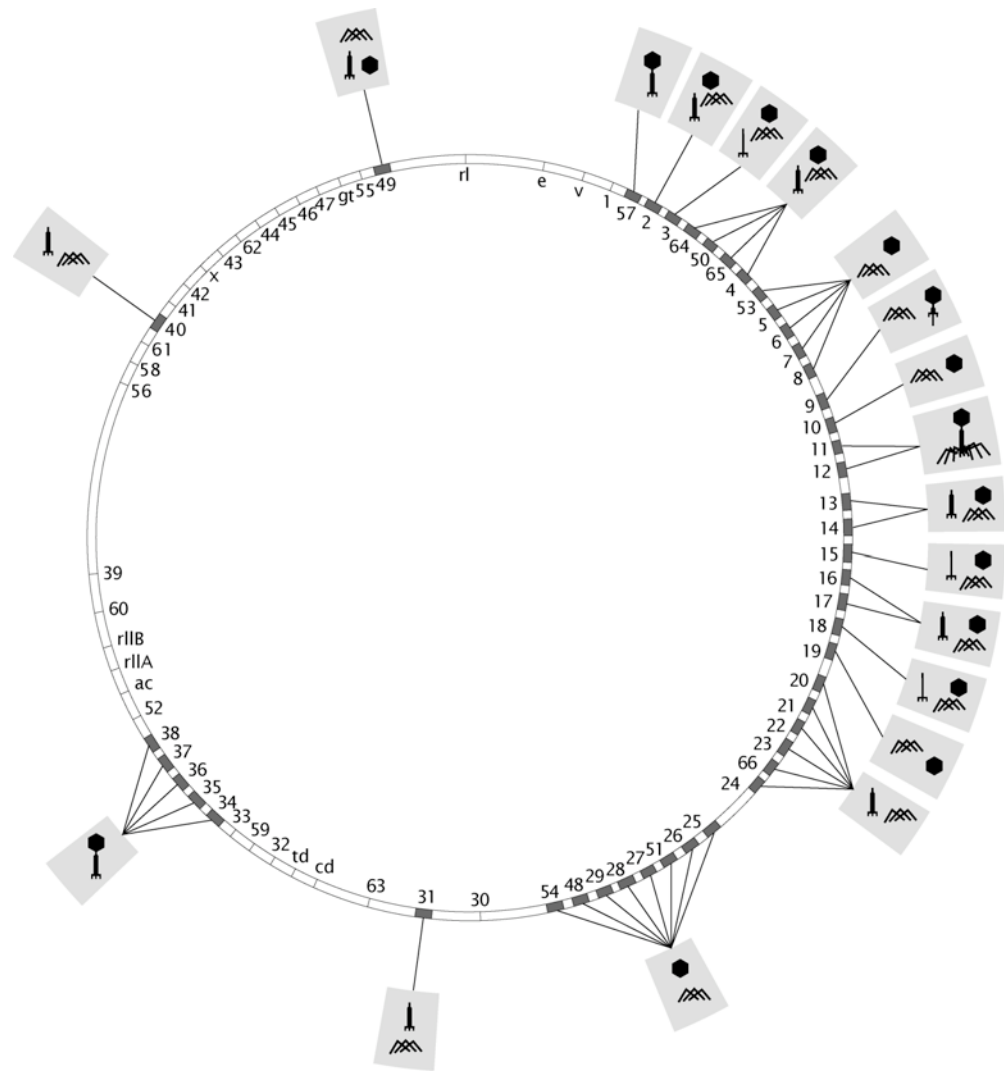


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Chapter 3, Figure 1

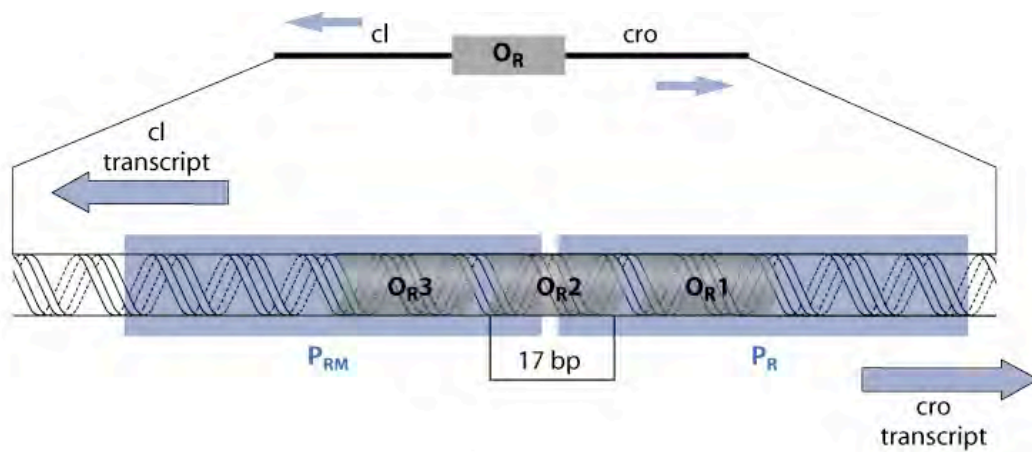


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Chapter 3, Figure 3

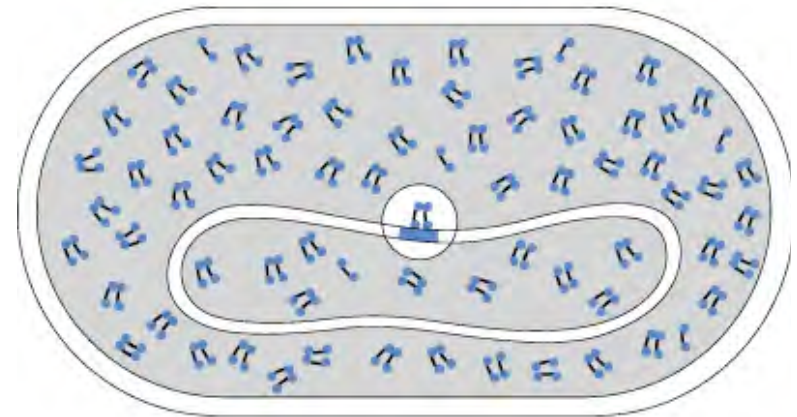
# A More Detailed Example of the Parrts List



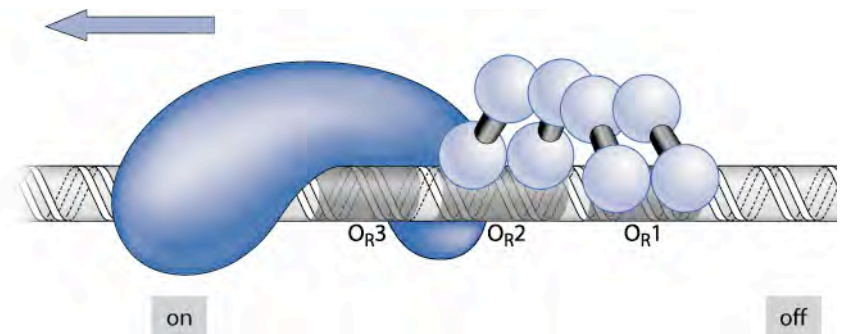
# The Lambda Switch: Lysogenic State



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 Chapter 1, Figure 4



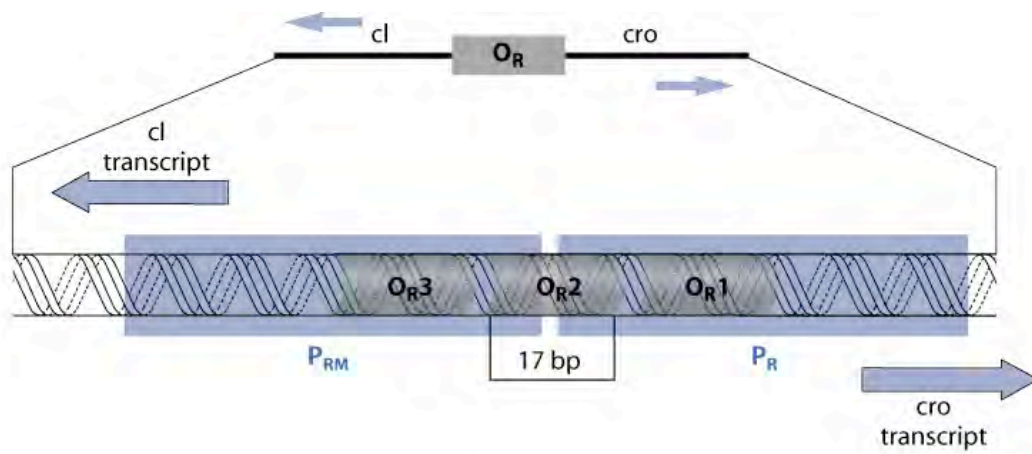
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 Chapter 1, Figure 8



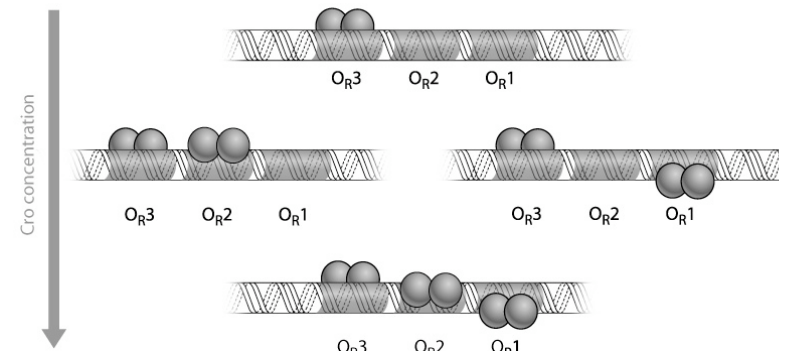
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 Chapter 1, Figure 19



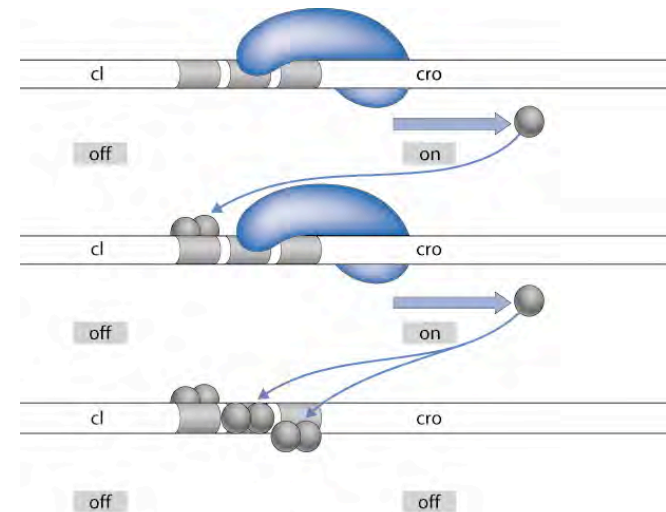
# The Lambda Switch: Lytic State



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 Chapter 1, Figure 4

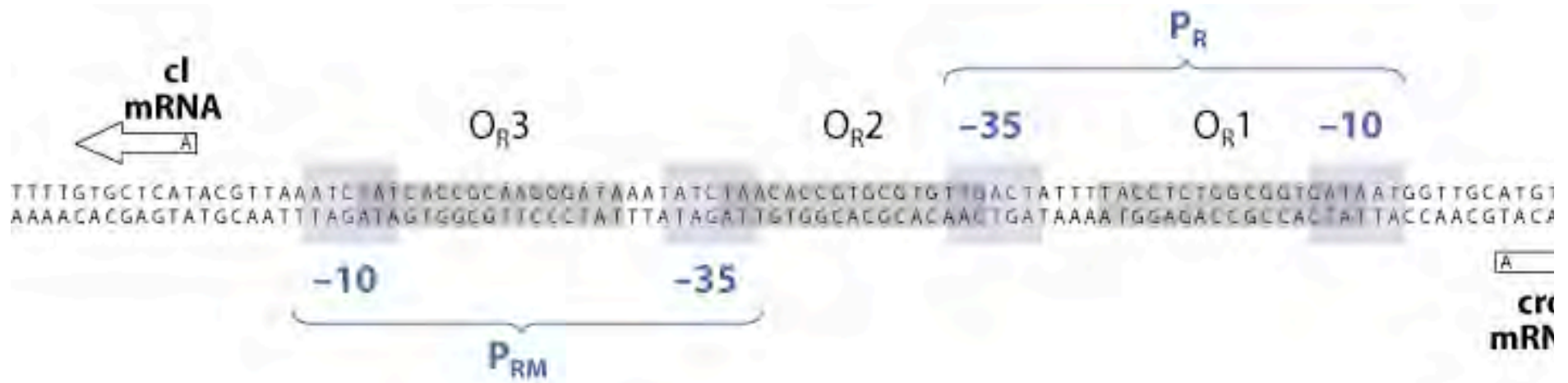


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 Chapter 1, Figure 23



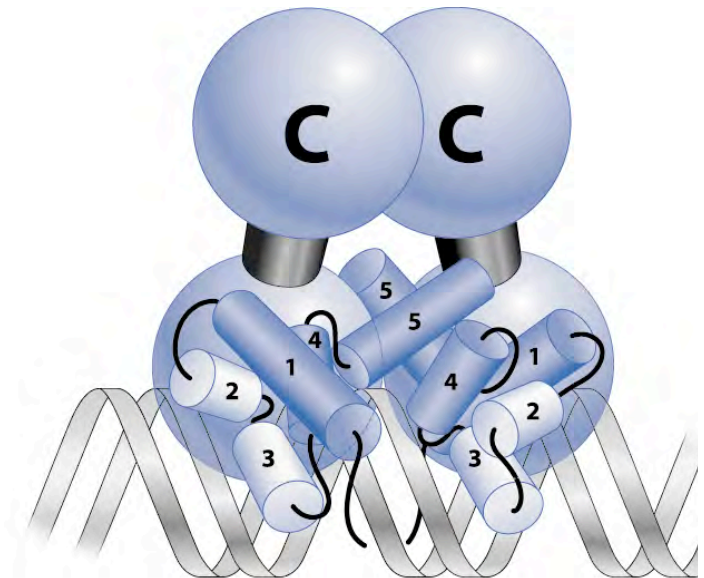
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 Chapter 1, Figure 24

# DNA Geography of the Switch



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Chapter 2, Figure 16

# Binding of Transcription Factors



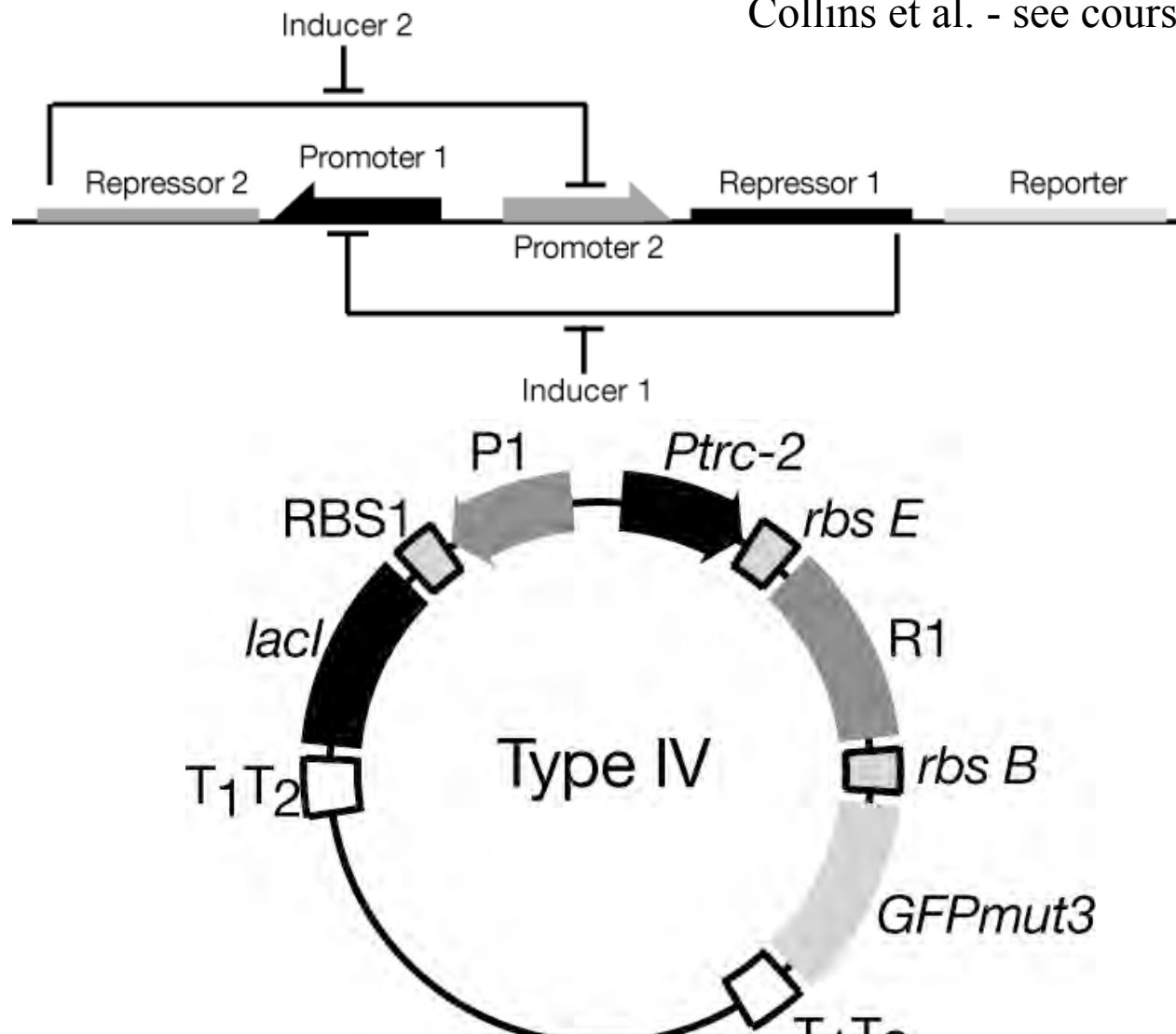
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 Chapter 2, Figure 11a

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 Chapter 2, Figure 6

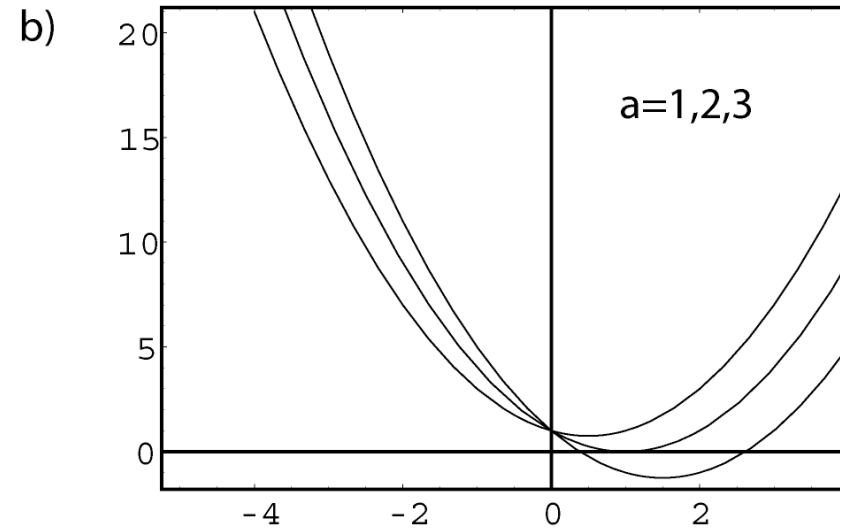
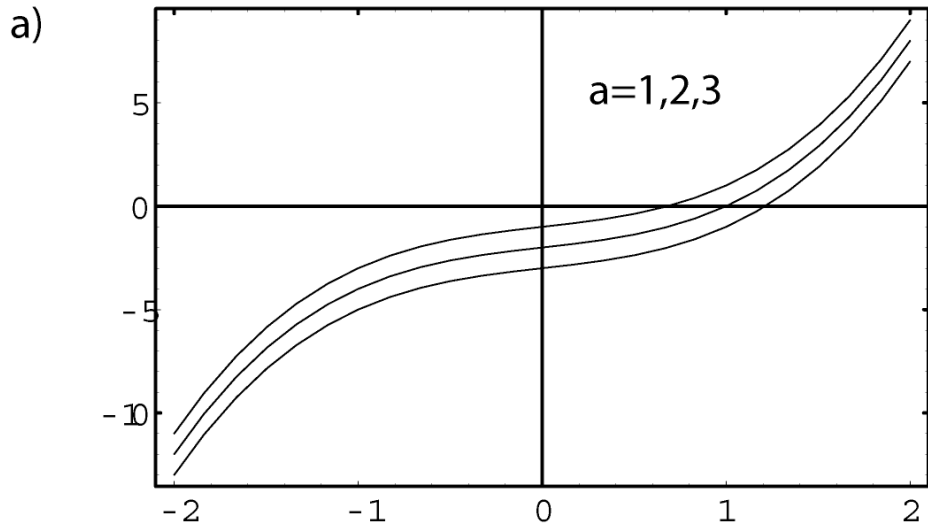


# Synthetic Genetic Switch

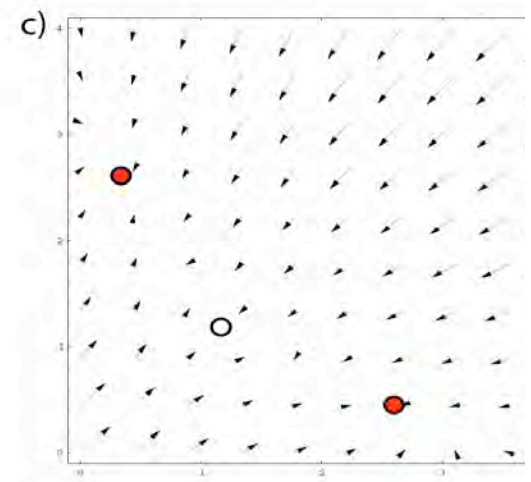
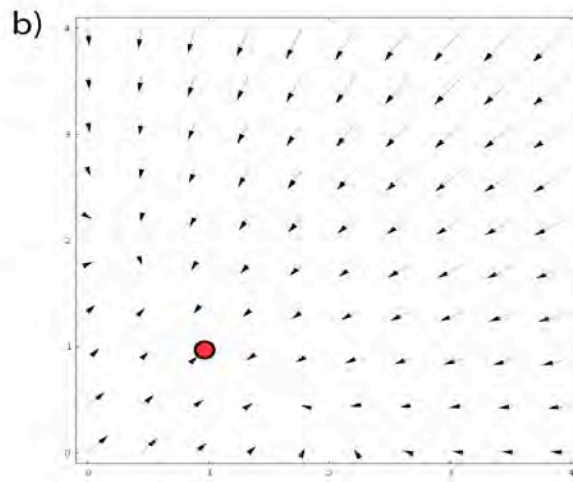
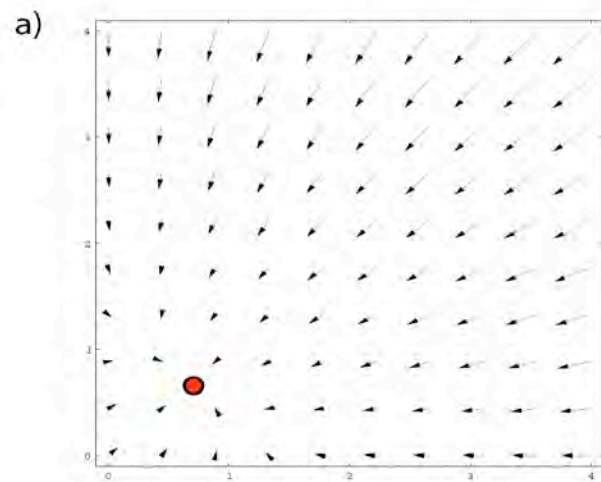
Collins et al. - see course website



# Stable Solutions



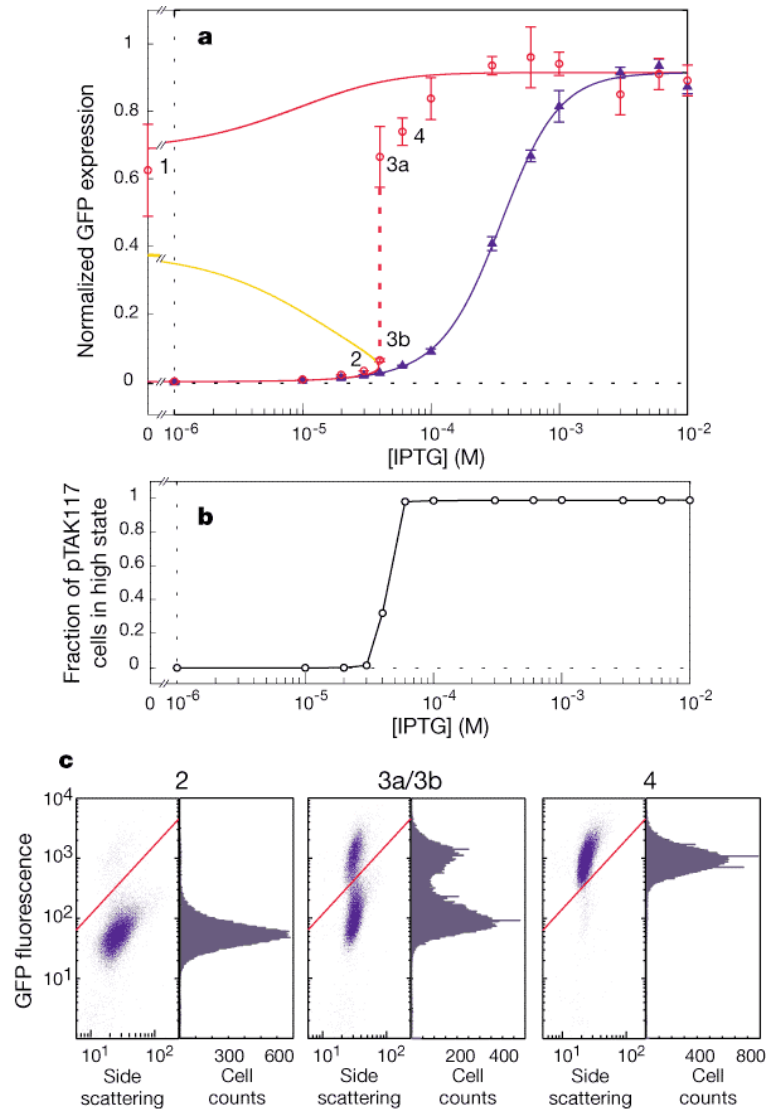
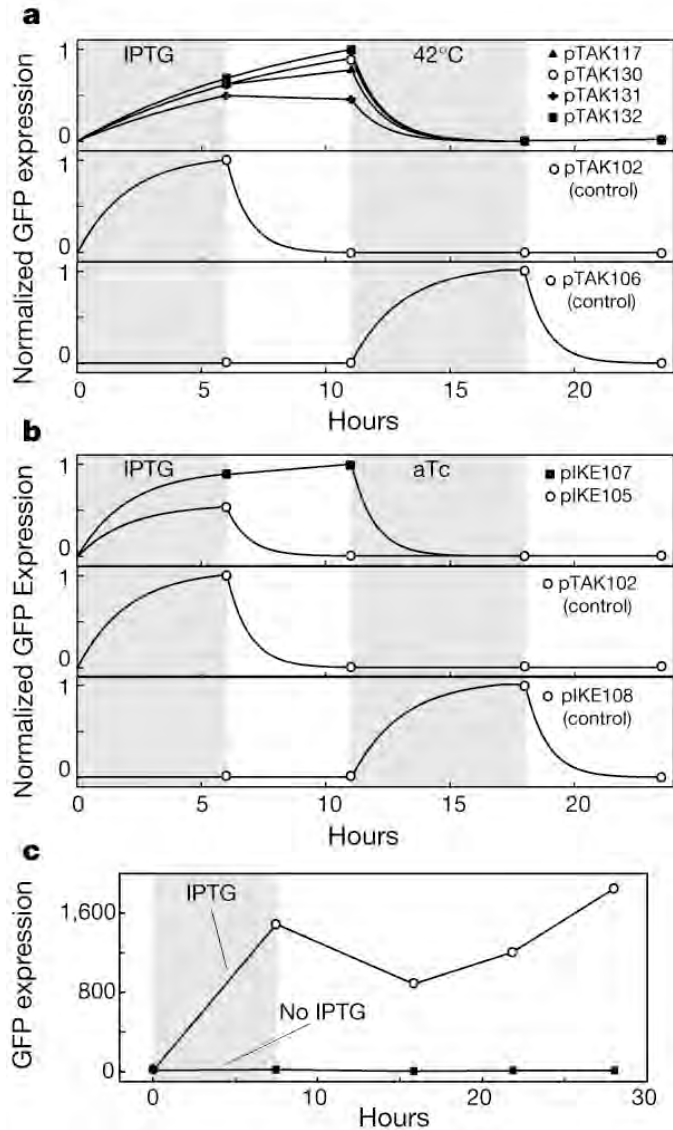
# *Phase Portrait for the Switch*





# Synthetic Genetic Switch

Collins et al. - see course website



# Coupling of Genes in Networks

