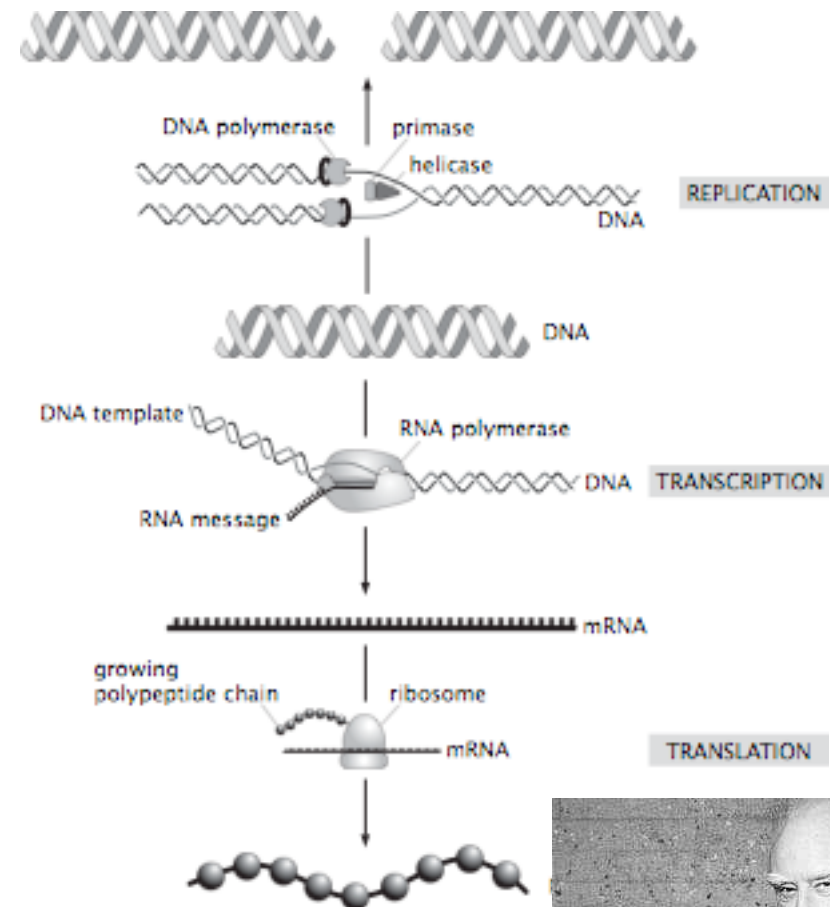


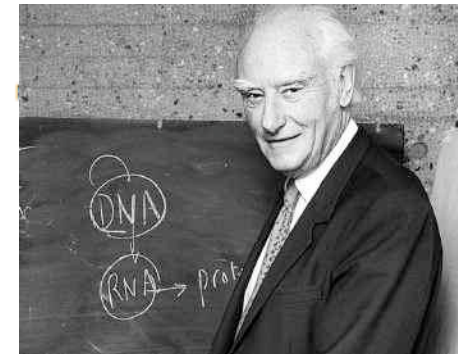
$F(n_{bp}) = \frac{\alpha}{n_{bp}} \gamma^{\ln N_p}$

# The Central Dogma of Molecular Biology: How Genes Lead to Proteins $\frac{\pi d}{R} k_B T$

- ◆ Crick and others mused over the “two great polymer languages”.
- ◆ Central dogma explains the chain of events relating them.
- ◆ The ribosome is the universal translating machine that speaks both languages.
- ◆ We have seen what genes are and how they serve as the informational memory of organisms. But we have NOT said how they are controlled.



Now we have the background to tackle the question we started with: how do cells make decisions?

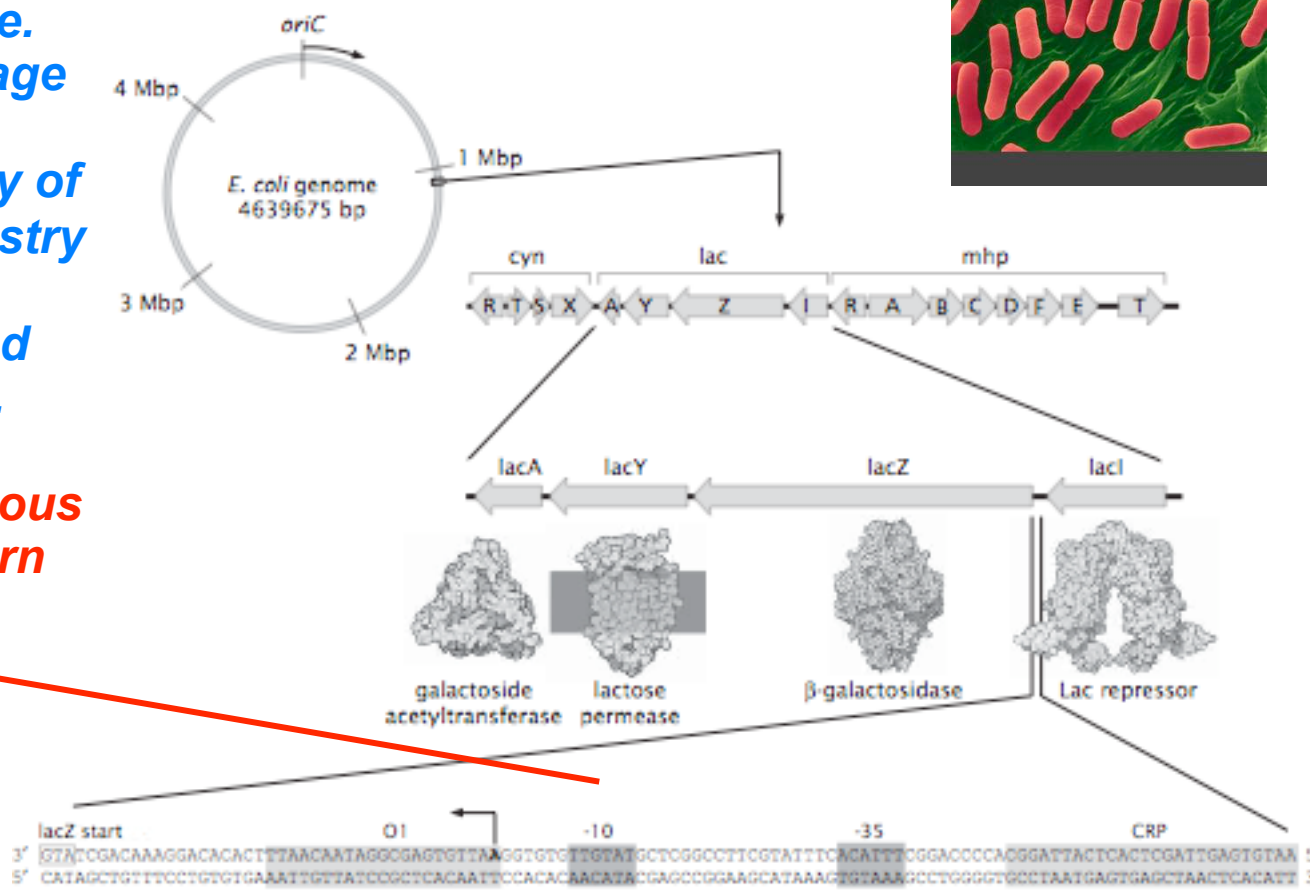


$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Not All DNA Codes for Proteins

$$E_{bend} = \frac{\pi \frac{d}{2} k_B T}{R}$$

- ◆ The *E. coli* genome is a circle with roughly 4.7 million base pairs.
- ◆ How many genes? An estimate.
- ◆ The genes related to sugar usage have been one of the most important stories in the history of modern biology and biochemistry (and take us right back to the great debate on vitalism played out with Pasteur in the 1800s).
- ◆ “Promoter” region on DNA is subject to intervention by various molecular bouncers that govern the gene.



*The regulatory landscape*

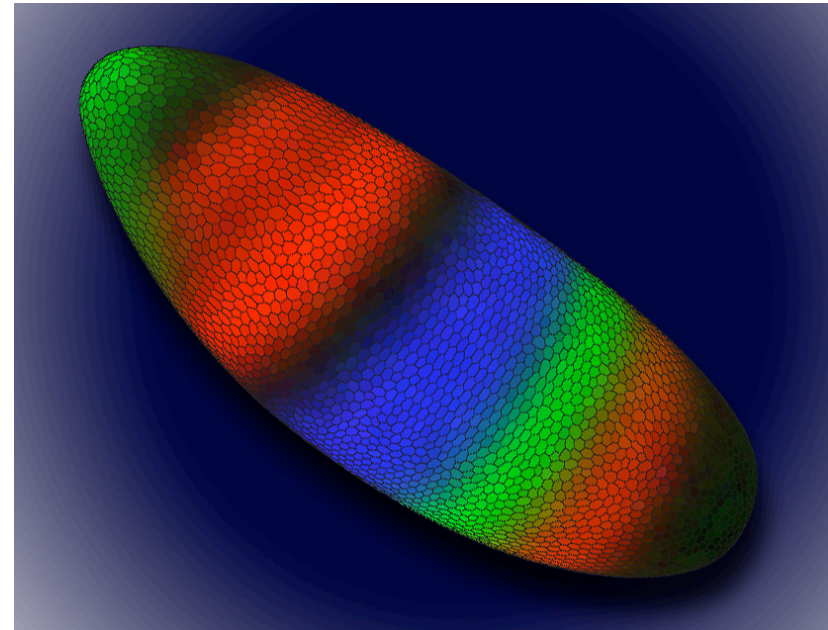
$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Ways to Measure Gene Expression

$$E_{bend} = \frac{\pi d_p k_B T}{R}$$

- ◆ **Basic point: looking for “reporters” of the level of expression of gene of interest.**
- ◆ **Can ask the system to report on the level of gene expression at various steps in the processes linking DNA to active protein.**
- ◆ **Promoter occupancy, level of mRNA, level of active protein.**

<http://www.lbl.gov/Science-Articles/Archive/sabl/2008/Feb/genome-mystery.html>

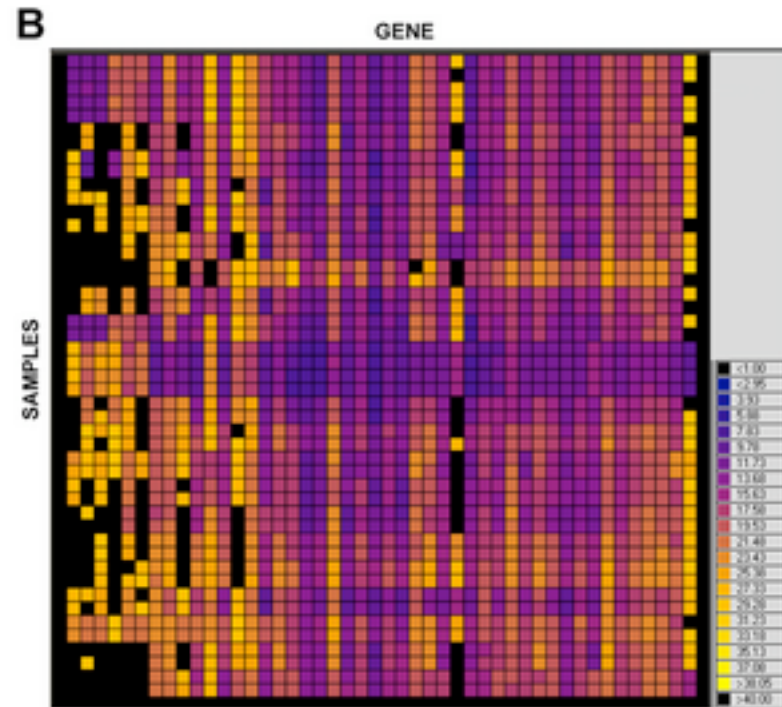
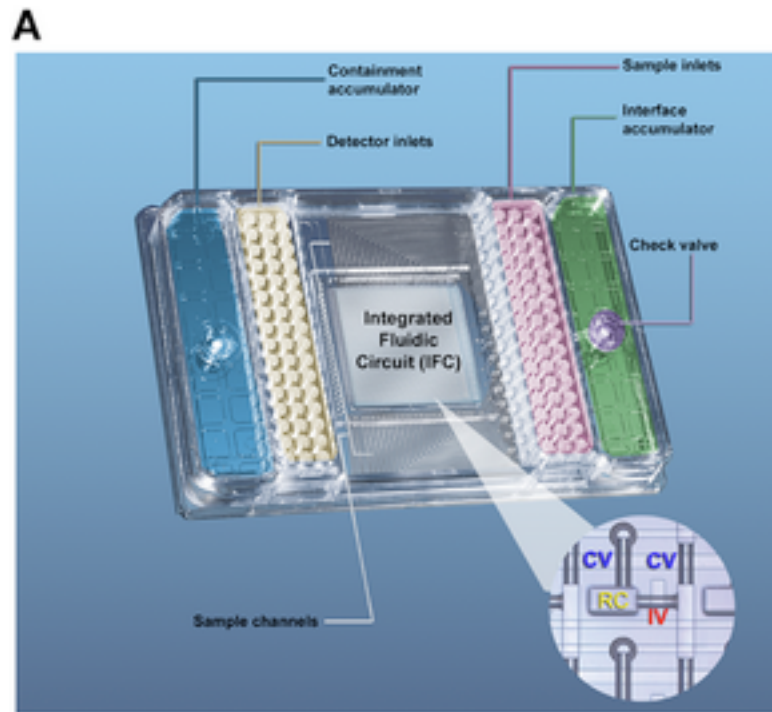


This image shows a *Drosophila* embryo colored to show the expression patterns of early gene regulators. Each color represents the level of expression of one of three gene regulators, Knirps (green), Kruppel (blue), and Giant (red). Color intensity reflects a higher level of expression. The darker areas of the embryo are cells where none of these gene regulators are expressed, and the yellowish areas indicate that both Knirps and Giant are being expressed.

$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Count the Messenger RNA Molecules

$$F_{bend} = \frac{S_p k_B T}{R}$$



$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

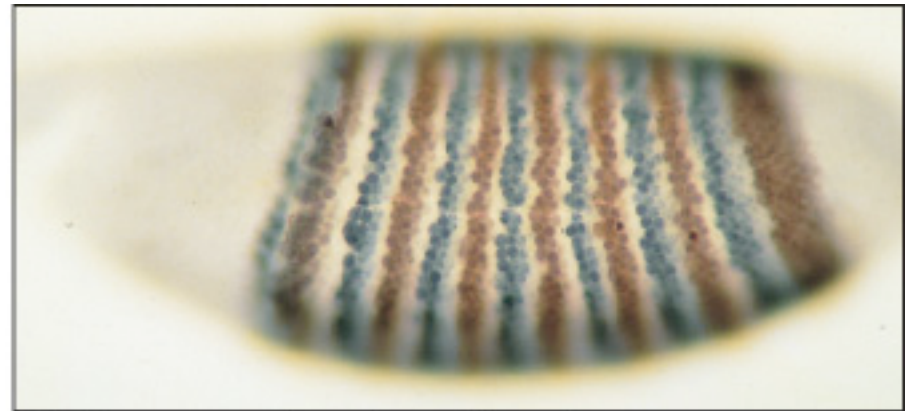
# Enzymatic Assay or In-Situ Hybridization

$$E_{bend} = \frac{\pi \frac{d}{2} k_B T}{R}$$

- ◆ **Enzymatic assays** – promoter leads to the production of a protein that then does some enzymatic action on the substrate which yields a product that can be visualized.
- ◆ **In-situ hybridization** – described the other day – probe is complementary to the RNA of interest and is labelled for detection.



2.7 hours after fertilization



3.5 hours after fertilization

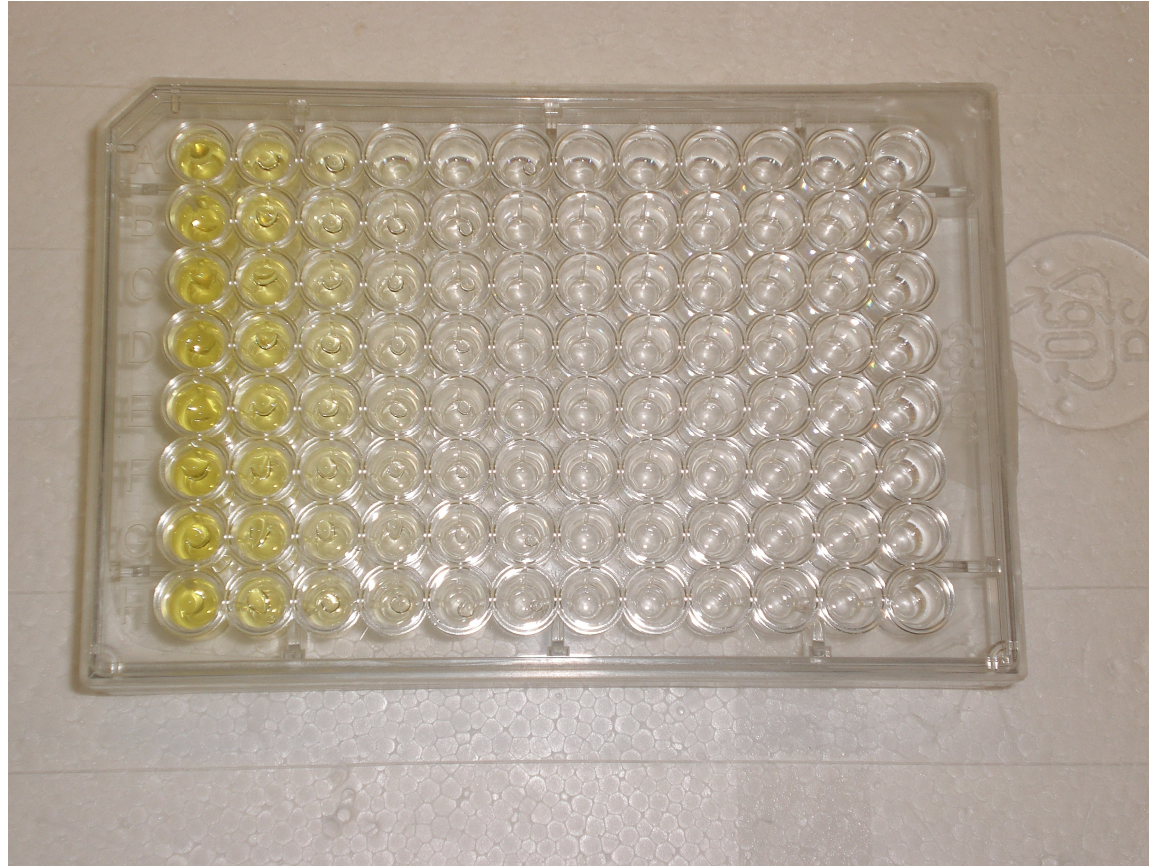
Figure 21–39. Molecular Biology of the Cell, 4th Edition.

$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Enzymatic Assay or In-Situ Hybridization

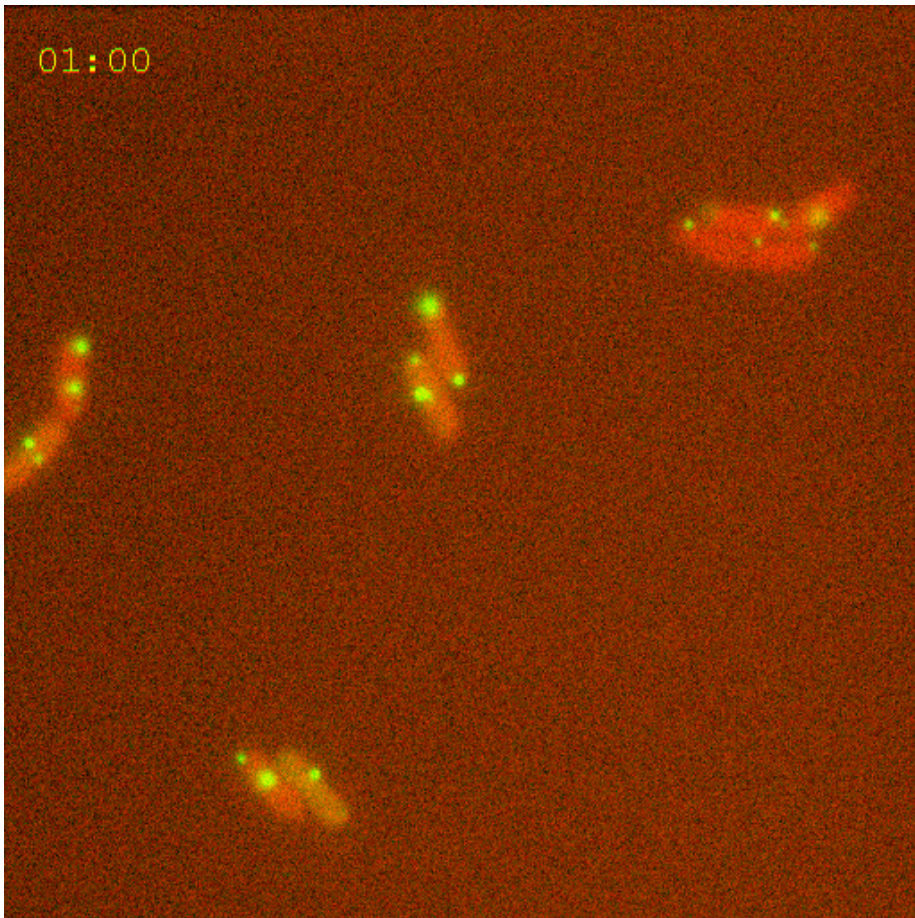
$$E_{bend} = \frac{\pi \frac{d}{4} k_B T}{R}$$

- ◆ **Enzymatic assays** – promoter leads to the production of a protein that then does some enzymatic action on the substrate which yields a product that can be visualized.
- ◆ **In-situ hybridization** -

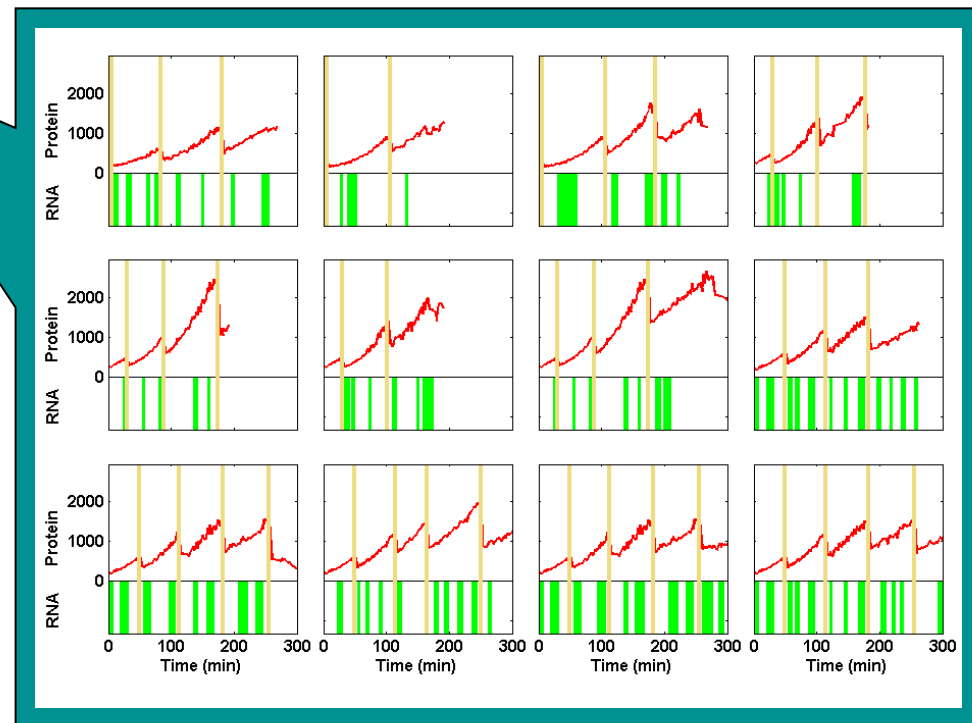


# Information Processing in Living Cells: Beyond First Approximations

$$\frac{\pi d_p k_B T}{R}$$



## Ido Golding



Department of Physics

**ILLINOIS**

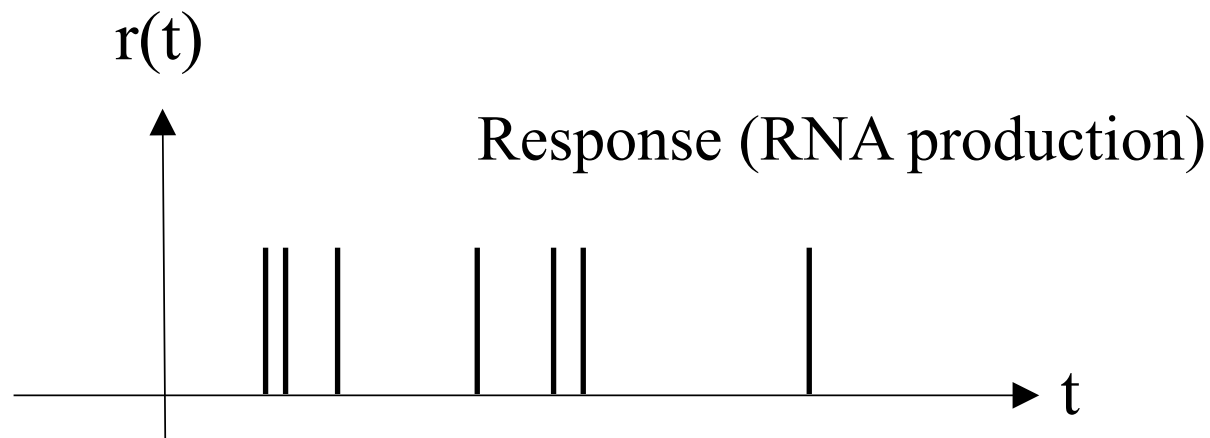
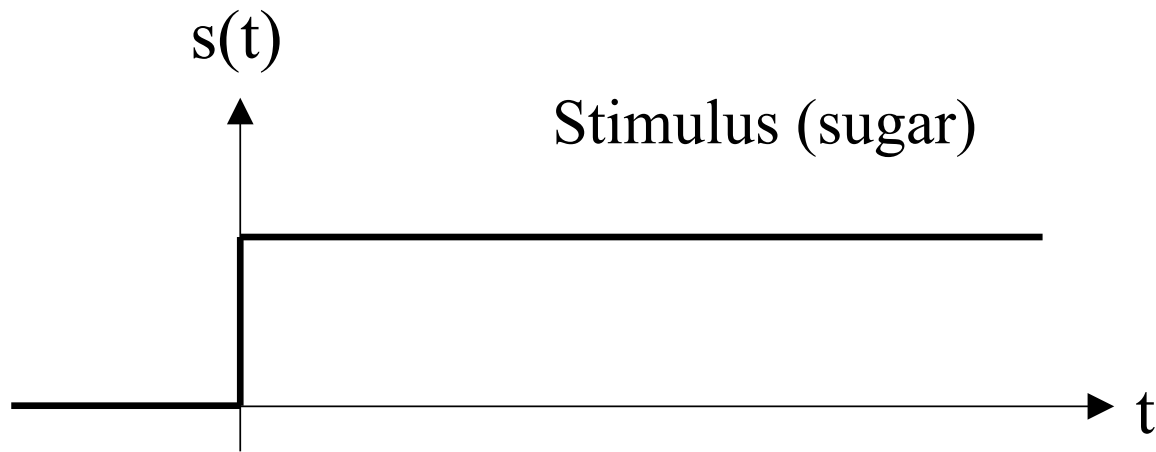
UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN

Center for the Physics  
of Living Cells

$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Simple Case of Turning a Gene "On"

$$E_{\text{bend}} = \frac{\pi \frac{d}{p} k_B T}{R}$$



Approximations used to describe the process...

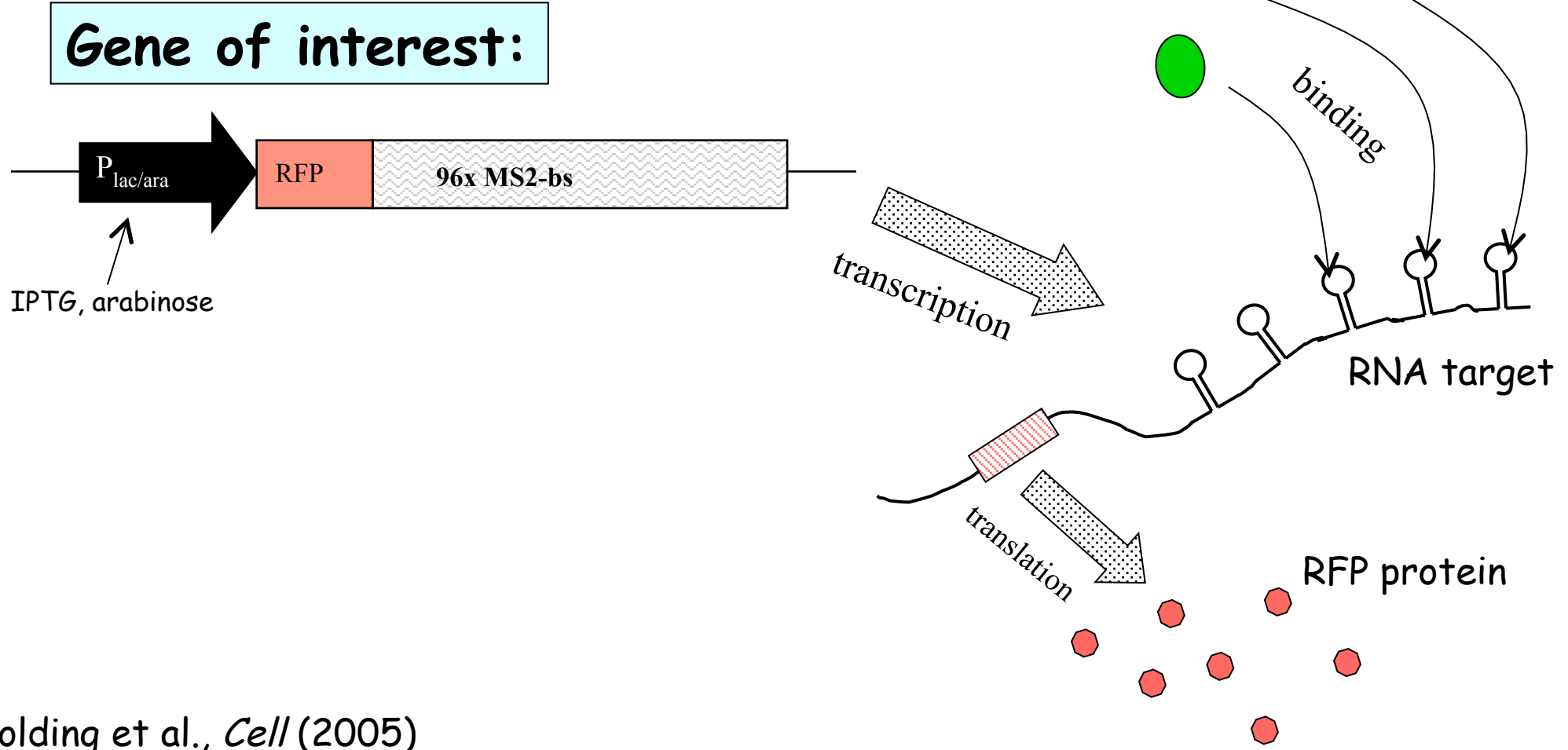


$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Engineering bacteria to report on gene activity

$$E_{bind} = \frac{K_{off}}{R}$$

(RNA-tagging protein;  
in excess in the cell)



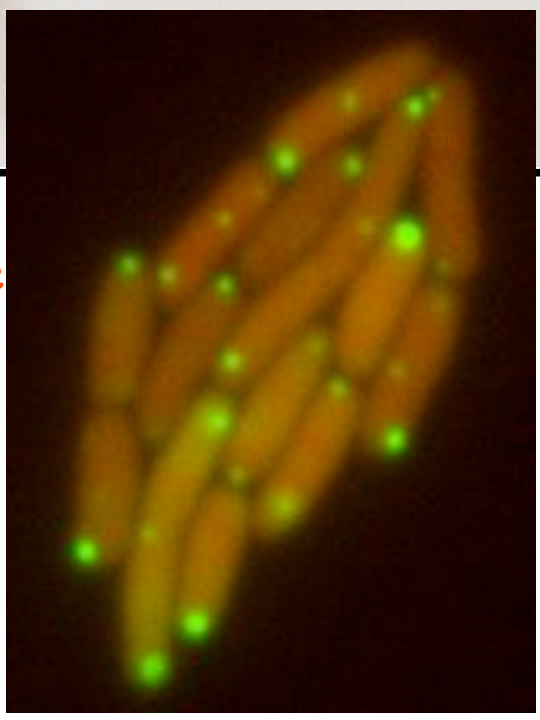
$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Measuring mRNA & protein numbers

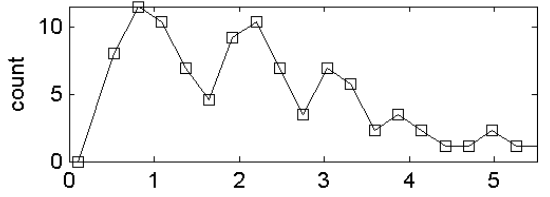
mRNA  $\propto$  number of bound MS2-GFPs  
 $\propto$  photon flux from localized green fluorescence

Protein  $\propto$  number of RFPs  
 $\propto$  photon flux from whole-cell red fluorescence

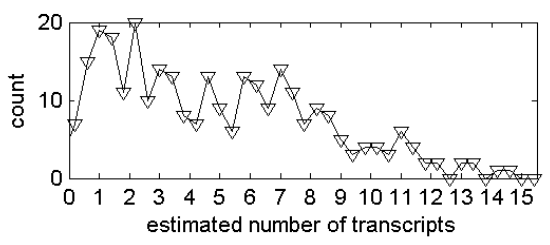
$$\frac{\pi d_p k_B T}{R}$$



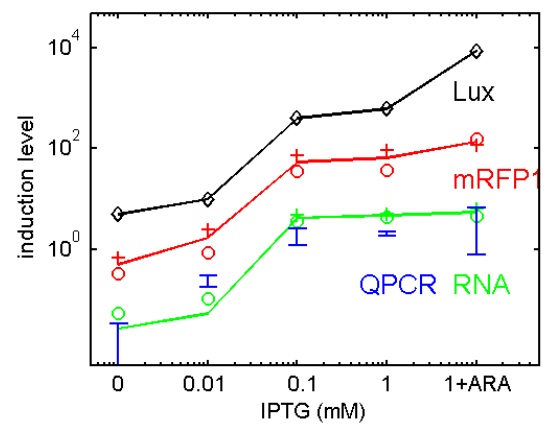
Histogram of RNA copy number:



1<sup>st</sup> peak =  
inter-peak interval  $\approx$   
50-100 X GFP =  
1 transcript

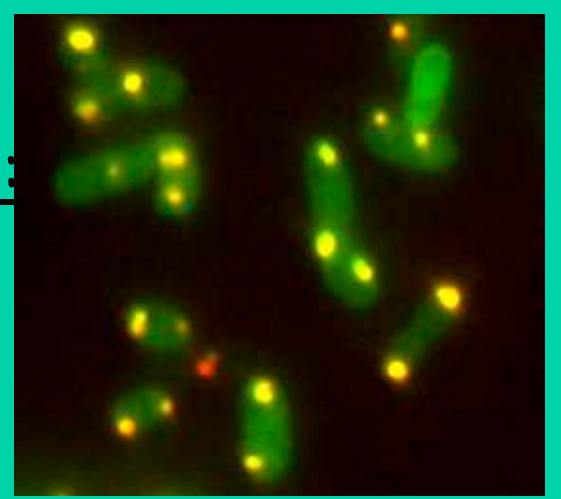


Controls:  
QPCR  
Protein levels



Lux: Lutz & Bujard 1997

Controls:  
FISH



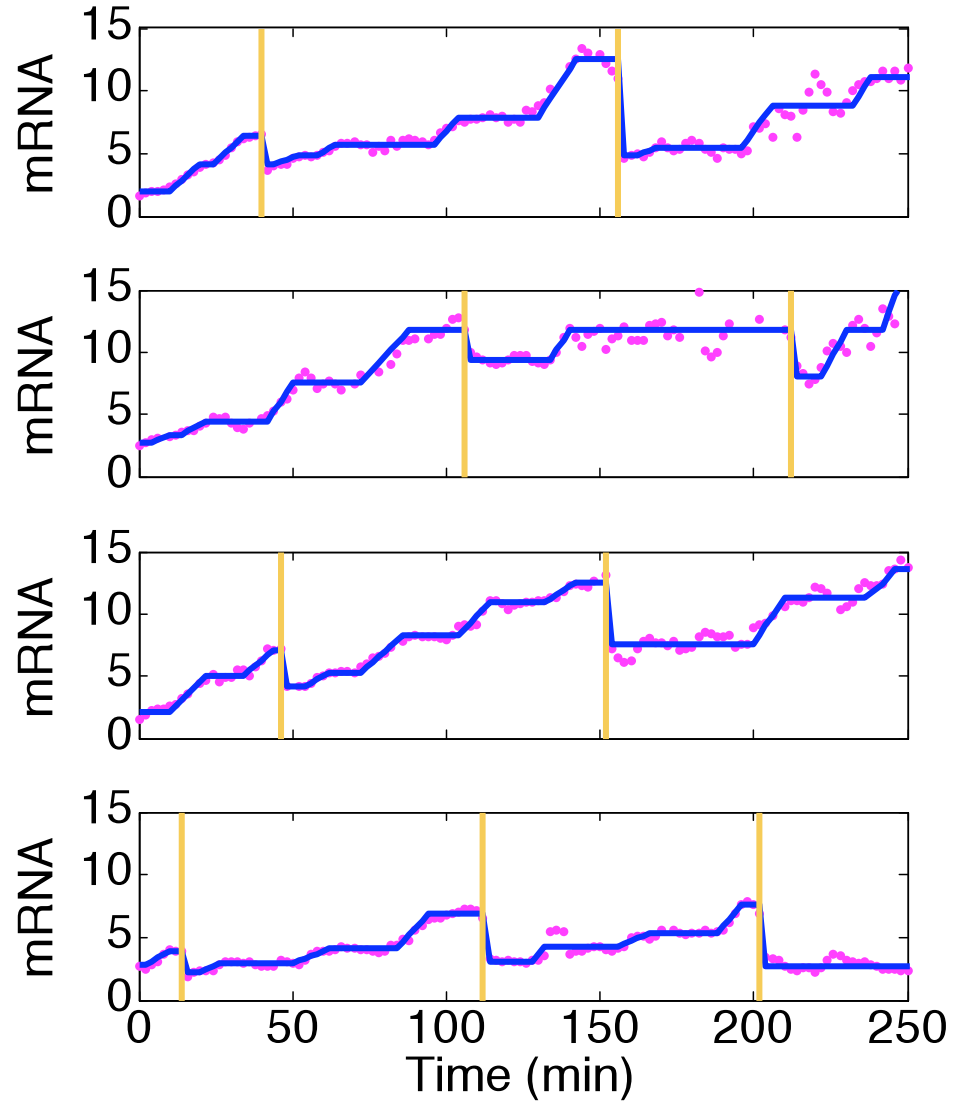
(Thanks to: A. Raj, A. van Oudenaarden)

$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

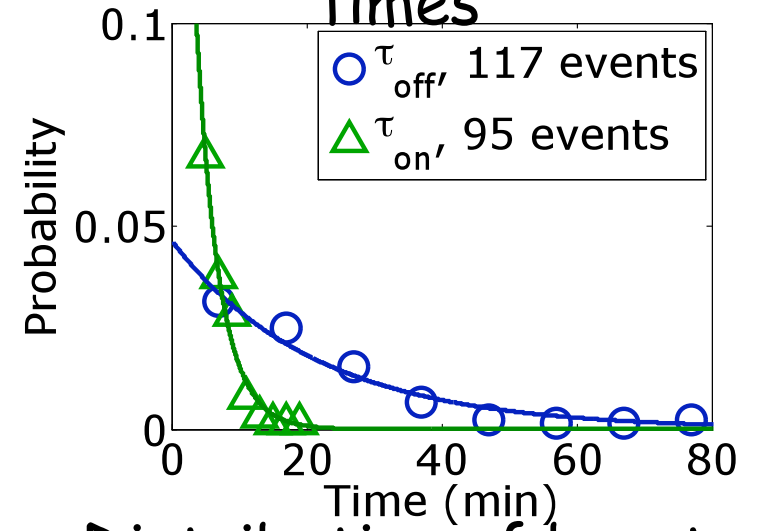
# RNA kinetics in individual cells

$$E_{bend} = \frac{\pi d_p k_B T}{R}$$

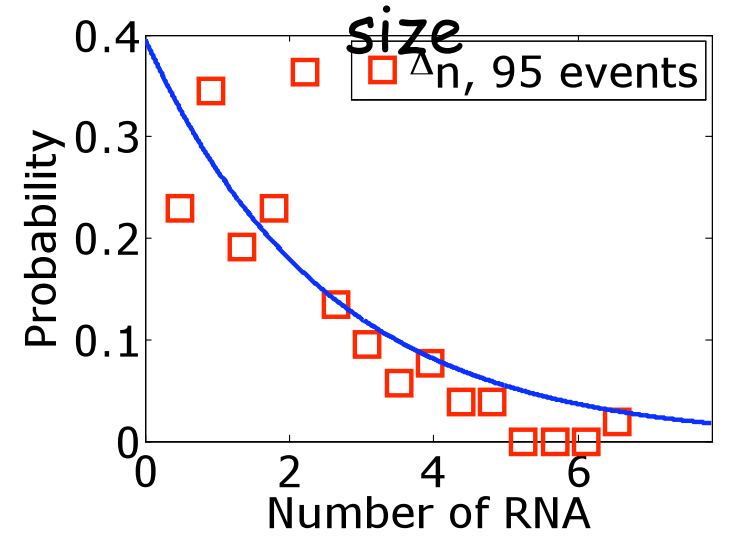
# mRNA vs time



Distribution of on & off times



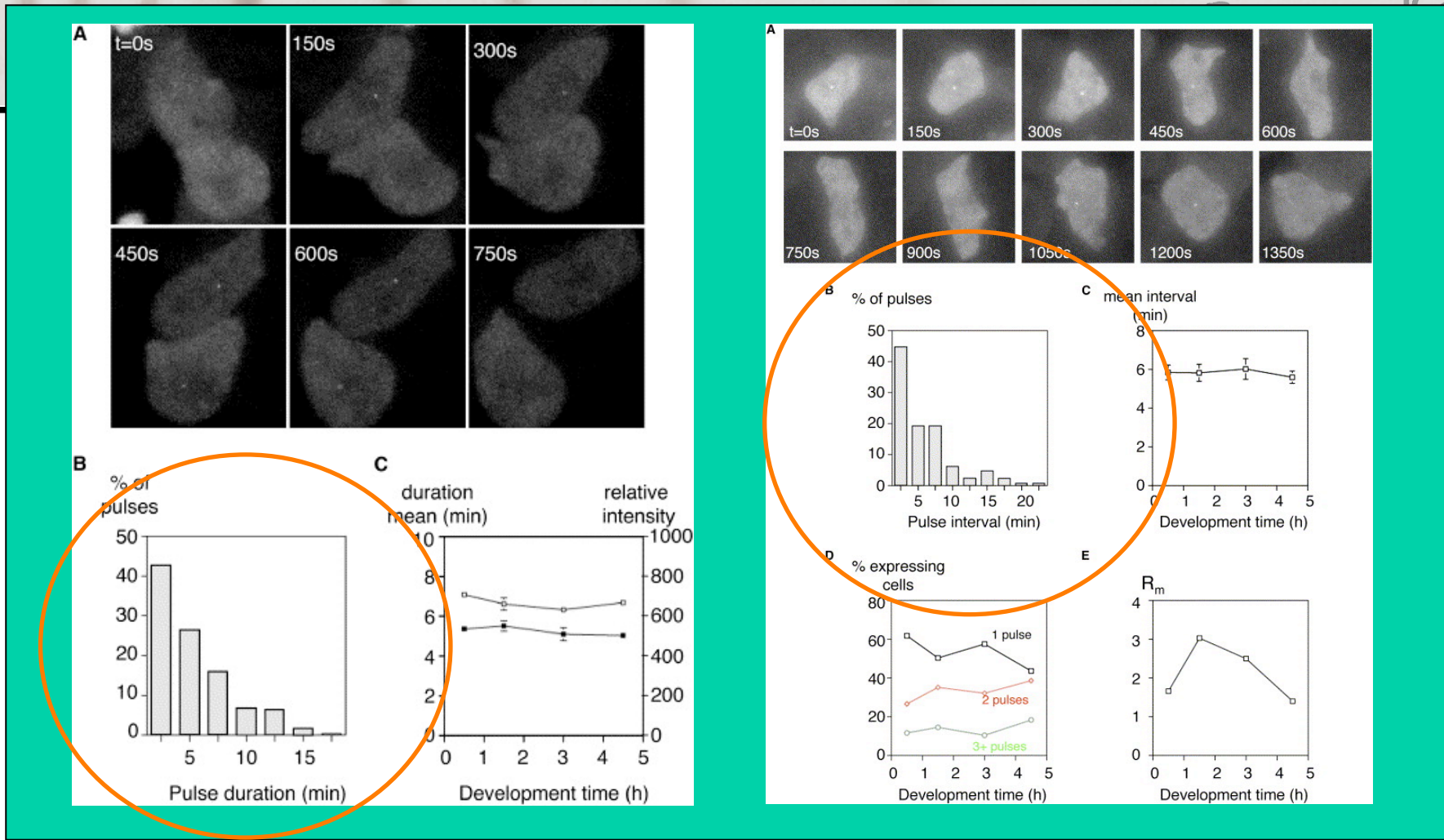
Distribution of burst size



$$F(N_{bp}) = \frac{\alpha}{N_{bp}} + \gamma \ln N_{bp}$$

# Transcriptional bursting in eukaryotes

$\pi d p k_B T$   
R



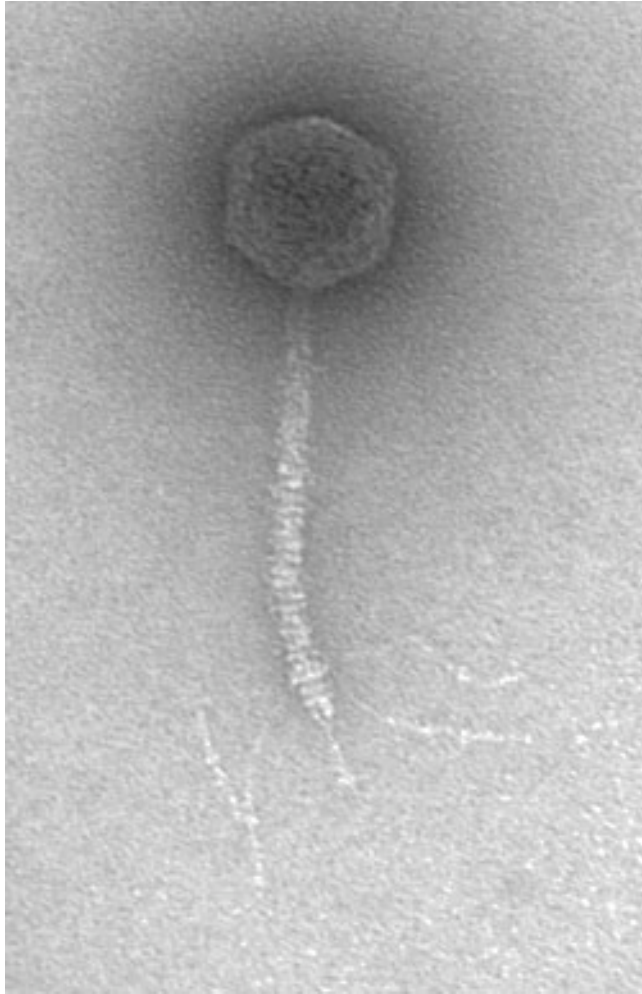
Chubb JR, Trcek T, Shenoy SM, Singer RH. *Curr. Biol.* (2006)

See also: Golding & Cox, *Curr. Biol.* (2006)

Raj A, Peskin CS, Tranchina D, Vargas DY, Tyagi S, *PLoS Biol.* (2006)

"Stochastic mRNA Synthesis in Mammalian Cells".

$F(n_{bp}) \propto e^{-\gamma \ln N_{bp}}$   
*The Lambda Switch: The Other Hydrogen Atom of Gene Regulation*  $E_{bend} = \frac{\pi^2 d_p k_B T}{R}$



Roger Hendrix

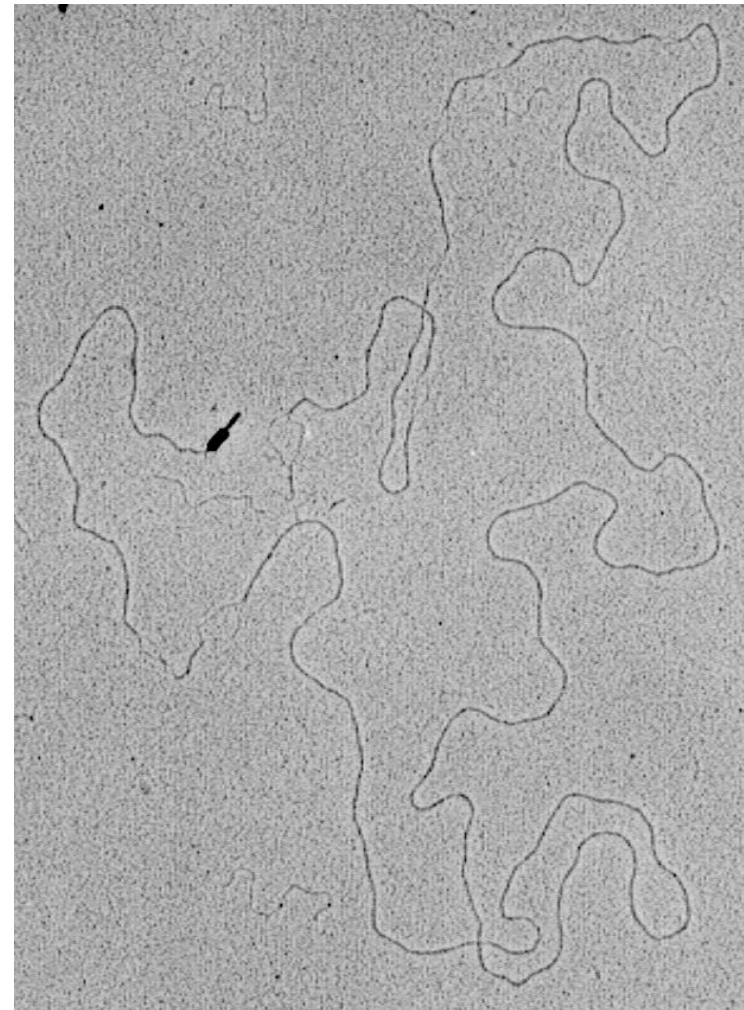
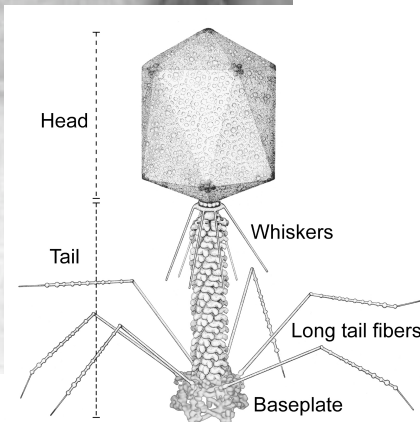
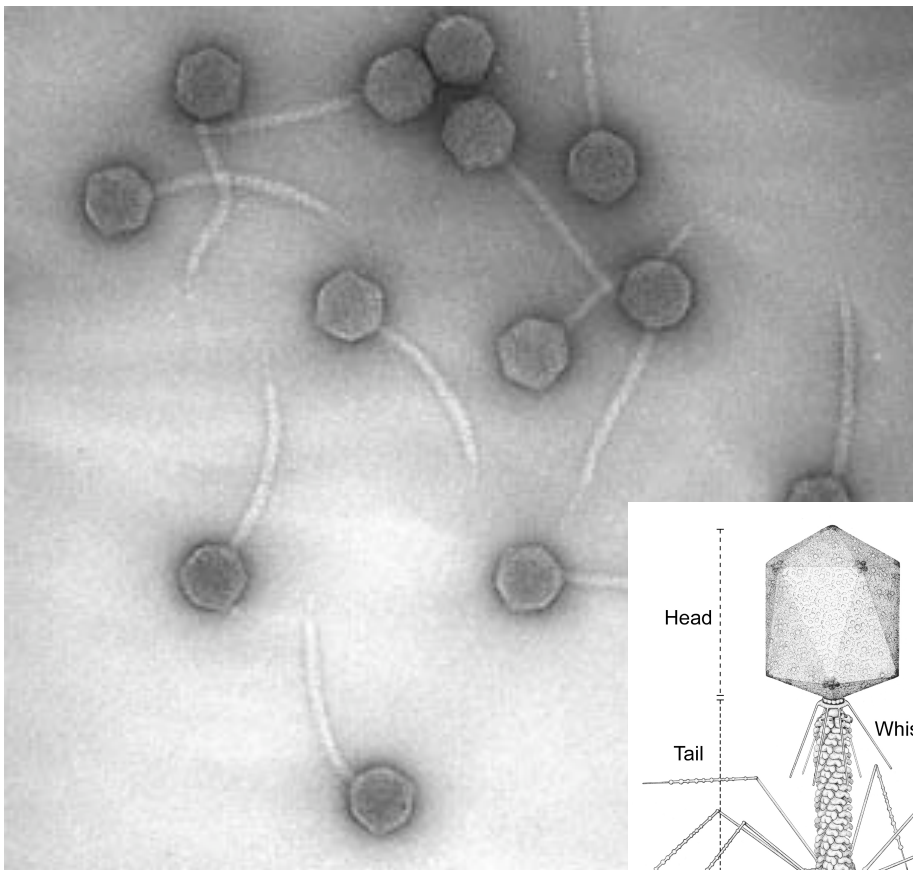


$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma l n N_{bp}$$

# Bacteriophage and Their Genomes

$$E_{bend} = \frac{\pi \frac{d}{2} k_B T}{R}$$

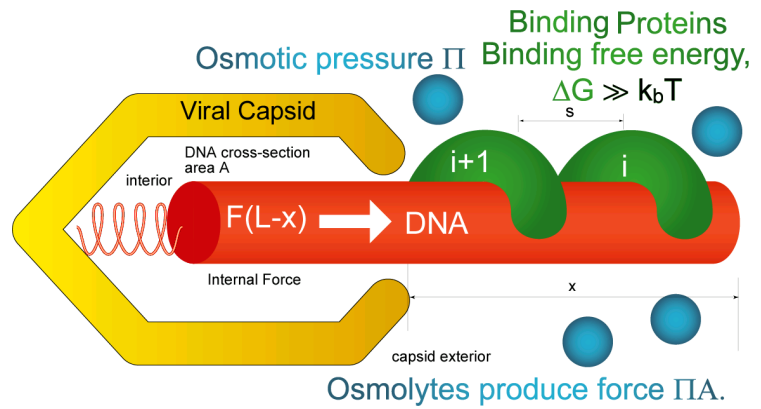
<http://www.biochem.wisc.edu/inman/empics/0020b.jpg>



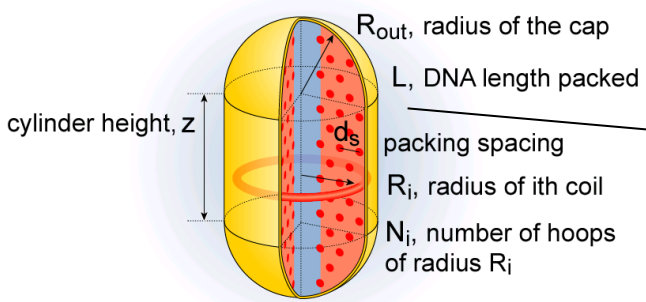
$$F(n_{bp}) = \frac{\alpha}{n} + \gamma \ln n_{bp}$$

# Physical Consequences of the Tight Squeeze in the Life Cycle of a Bacteriophage

$$= \frac{\pi d_p^2 k_B T}{4R}$$

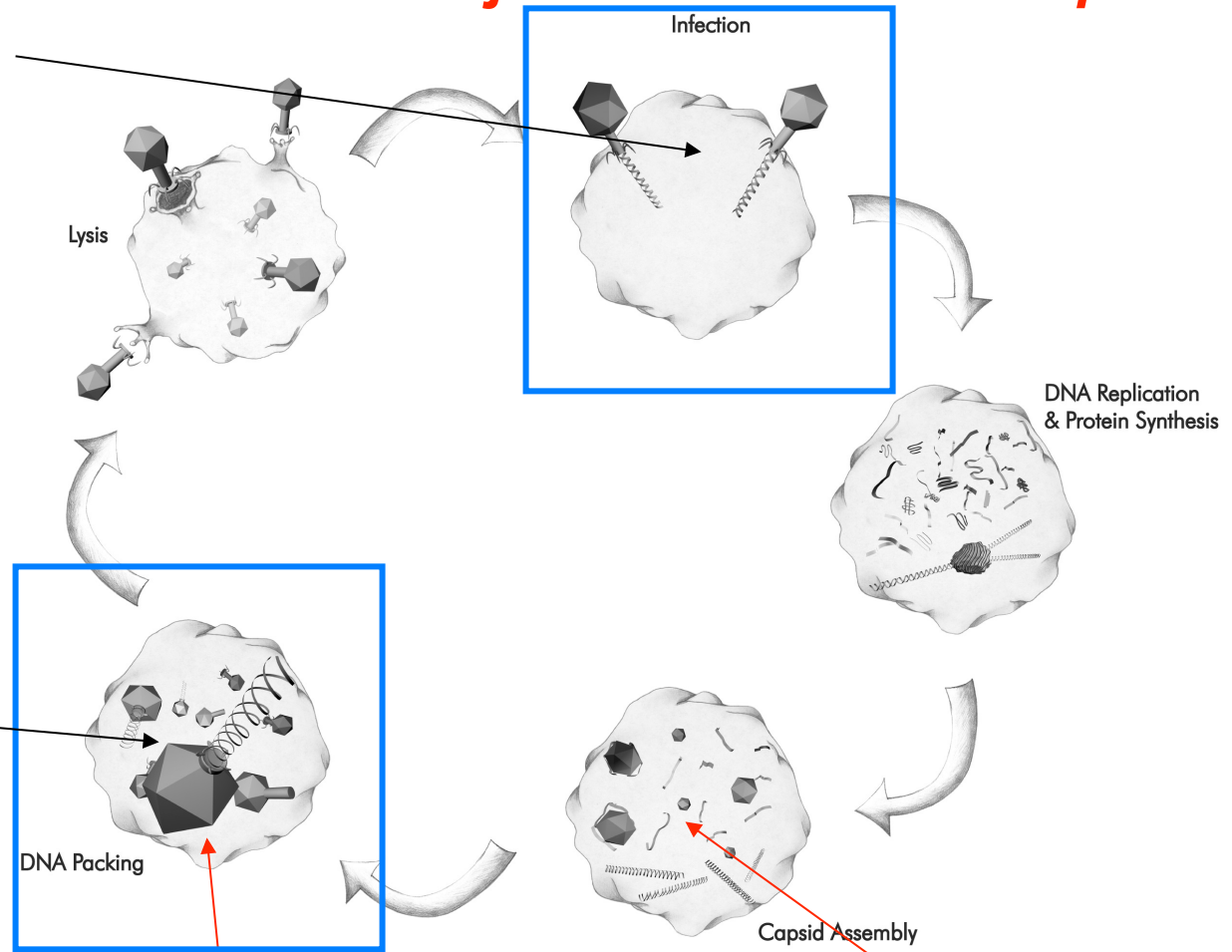


**Forceful ejection**



**Construct a physical model of these processes.**

**Rate of ejection:  $\approx 100 - 1000 \text{ bp/sec}$**



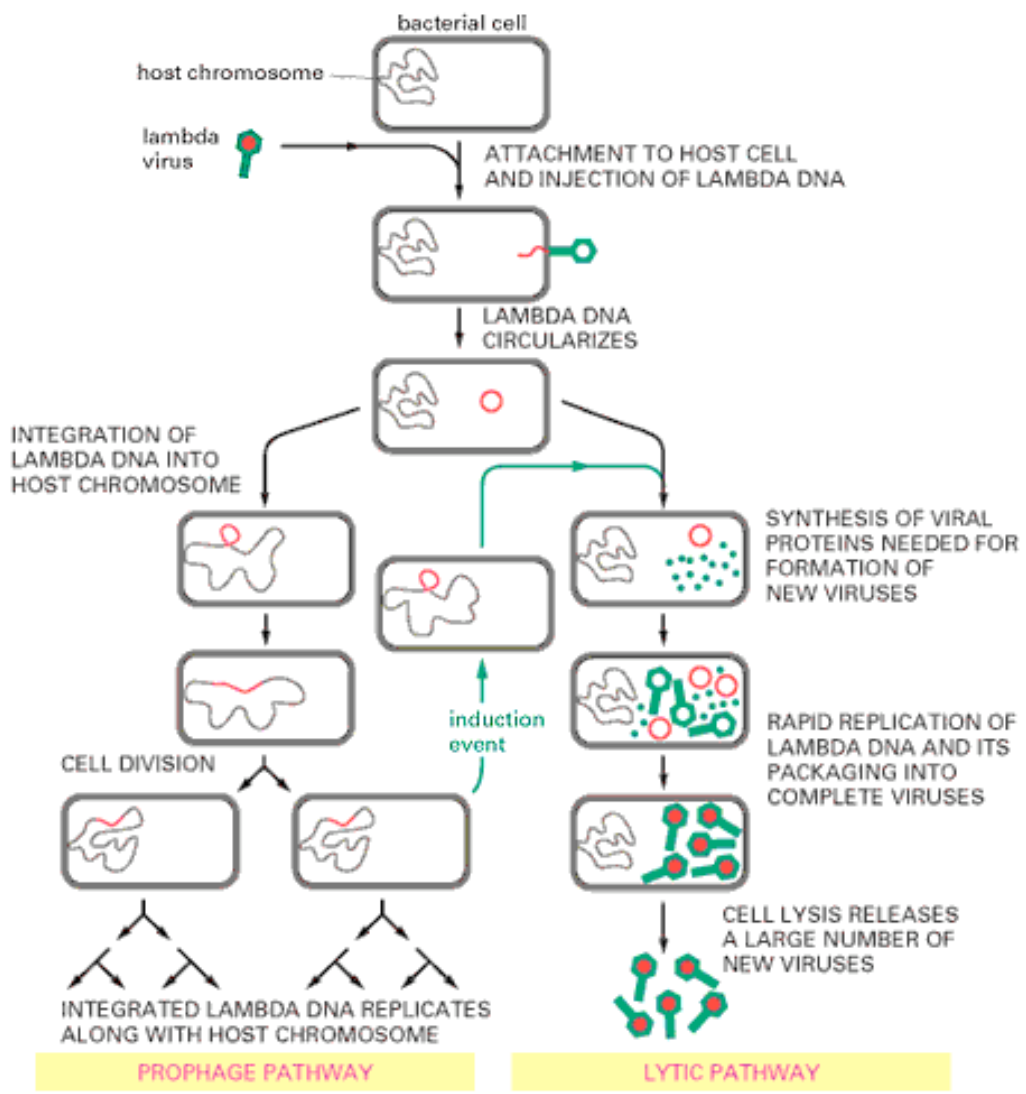
**Rate of packing:  $100 \text{ bp/sec}$   
"Some assembly required"**

**Self-assembly**

$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# The Life Cycle of Bacteriophage Lambda

$$F_{bend} = \frac{a \cdot \frac{d}{2} \cdot k_B T}{R}$$

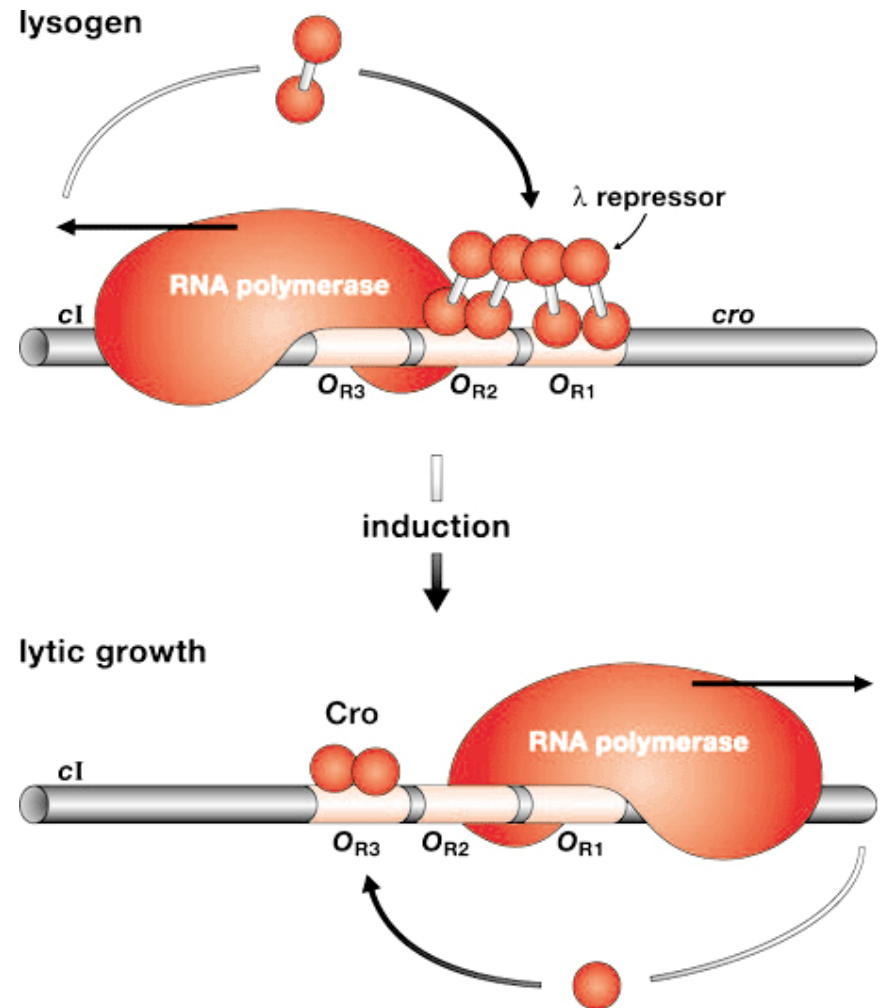
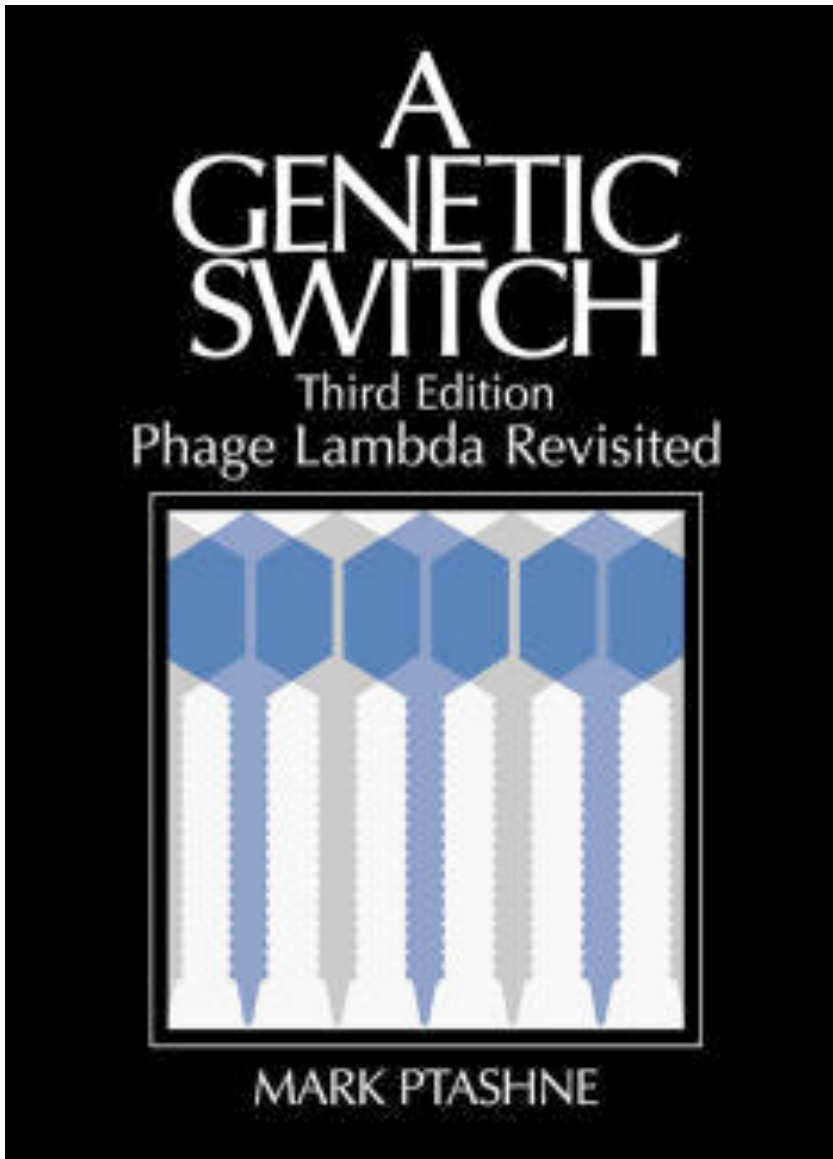




$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# A Genetic Switch

$$E_{bend} = \frac{\pi d_p k_B T}{R}$$



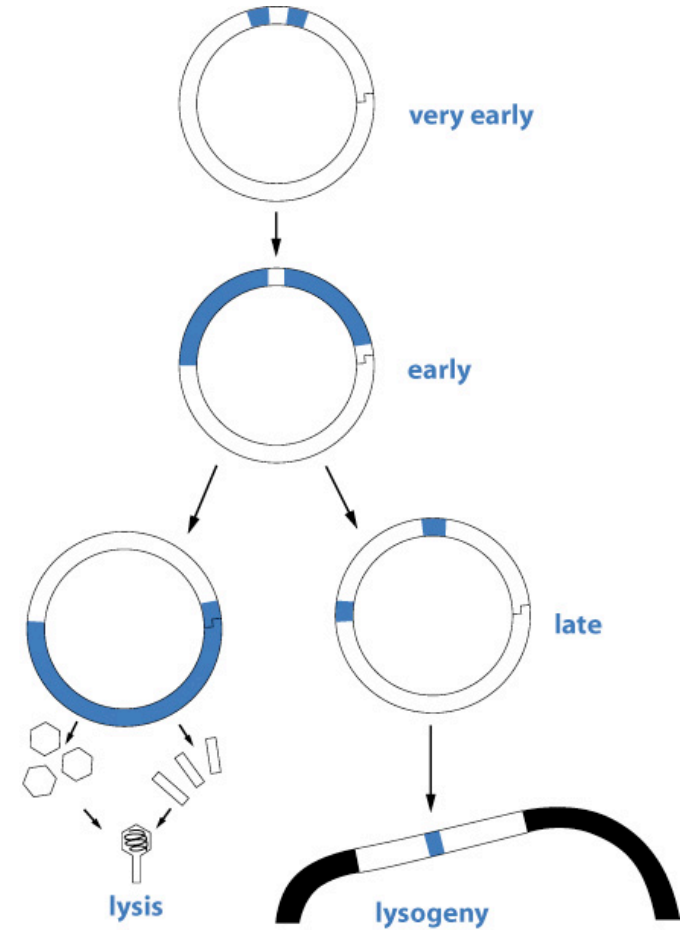
$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# The Lambda Genome

$$E_{bend} = \frac{\pi \frac{d}{2} k_B T}{R}$$



*A Genetic Switch*, 3rd edition, 2004  
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 Chapter 3, Figure 1



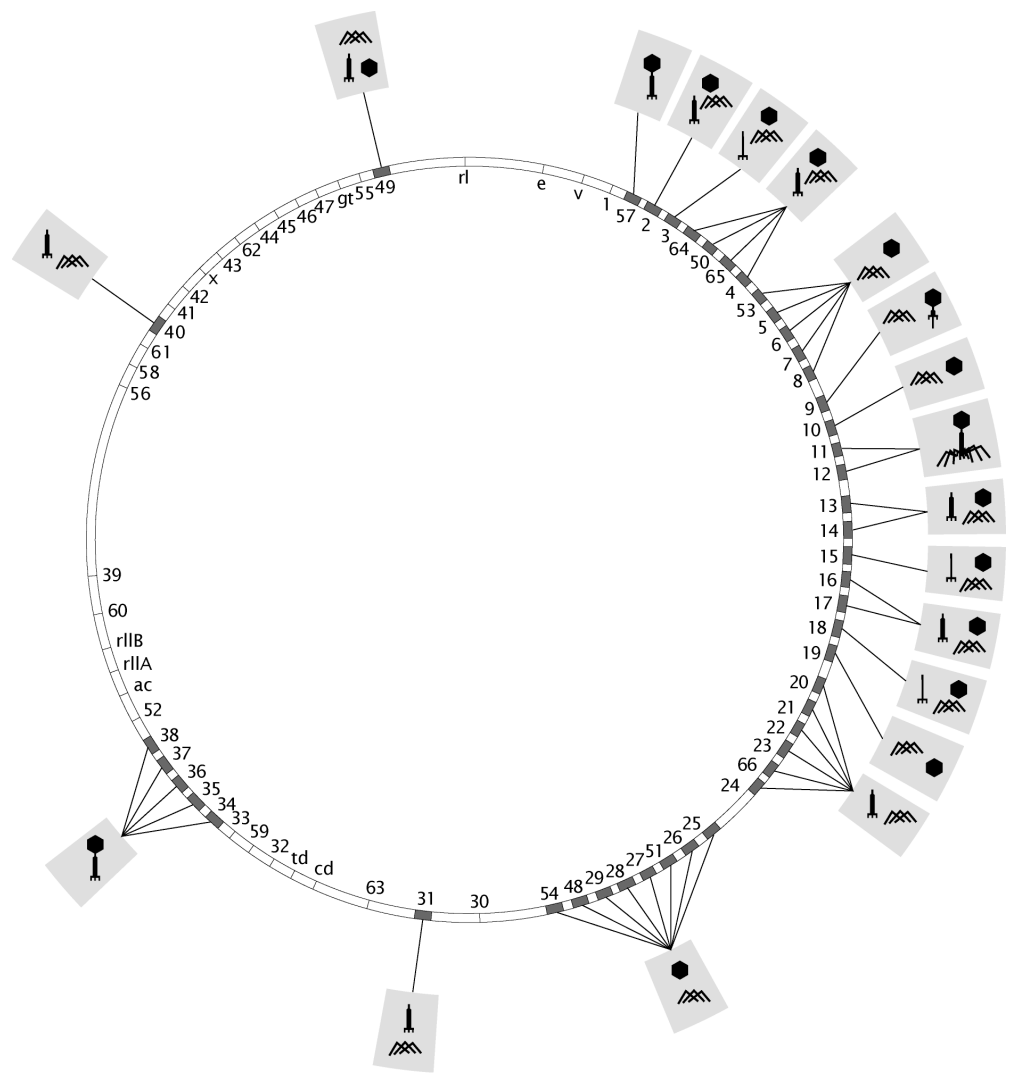
*A Genetic Switch*, 3rd edition, 2004  
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 Chapter 3, Figure 3

$$F(n_{bp}) = \frac{\alpha}{A_{bp}} + \gamma \ln N_{bp}$$

# More Detailed Example of the Parrrts

List

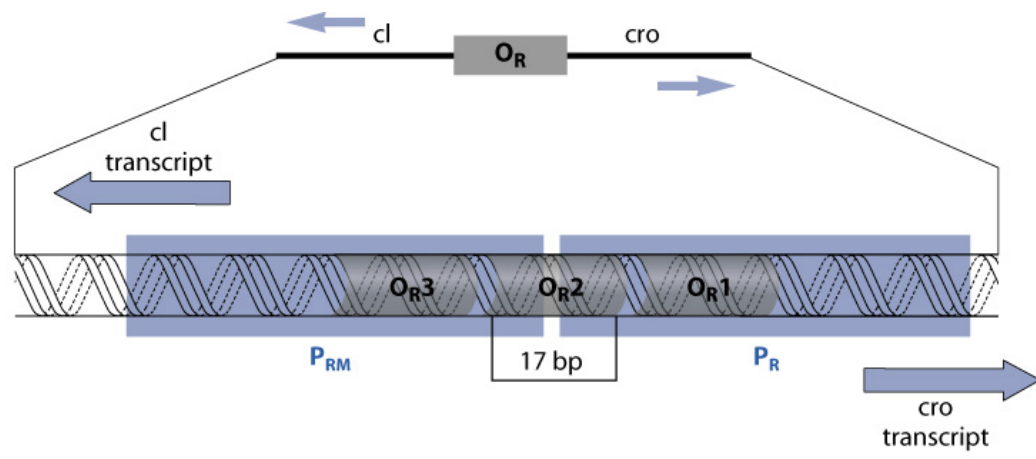
$$E_{bend} = \frac{\pi d_p k_B T}{R}$$



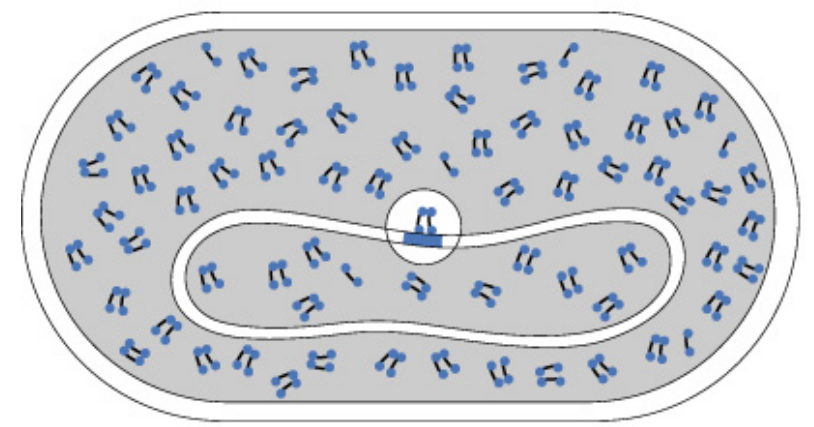
$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma l u N_{bp}$$

# The Lambda Switch: Lysogenic State

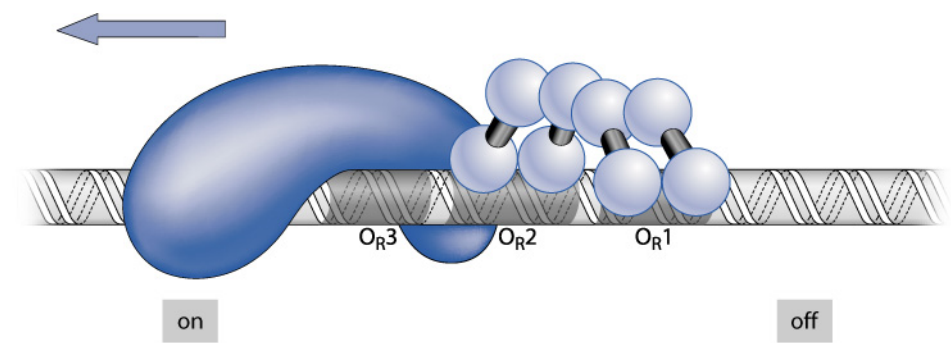
$$F_{bend} = \frac{\pi \frac{d}{2} k_B T}{R}$$



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 Chapter 1, Figure 4



*A Genetic Switch*, 3rd edition, 2004  
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 Chapter 1, Figure 8

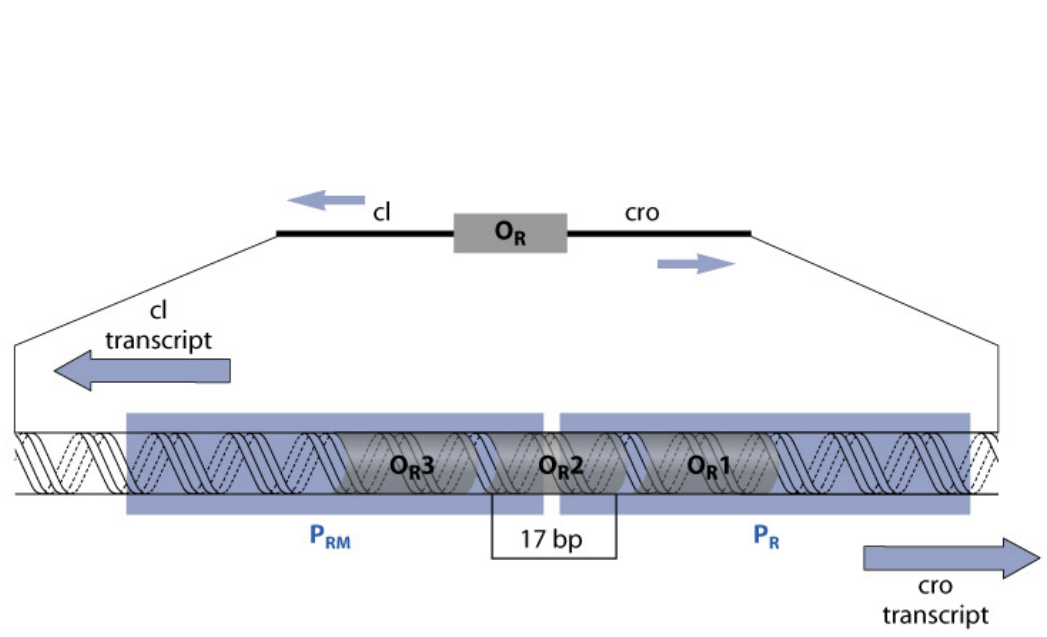


*A Genetic Switch*, 3rd edition, 2004  
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 Chapter 1, Figure 19

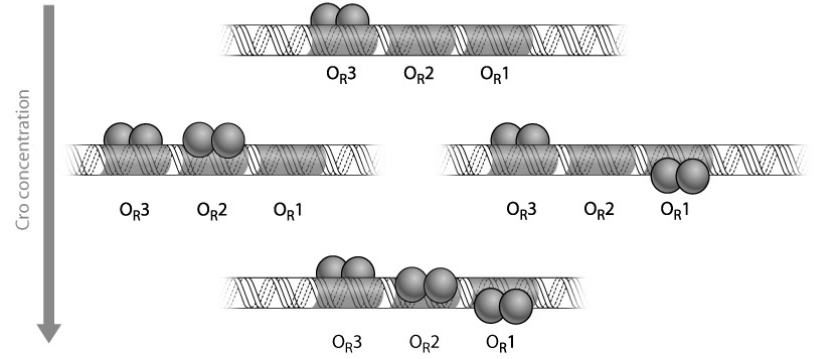
$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma l u N_{bp}$$

# The Lambda Switch: Lytic State

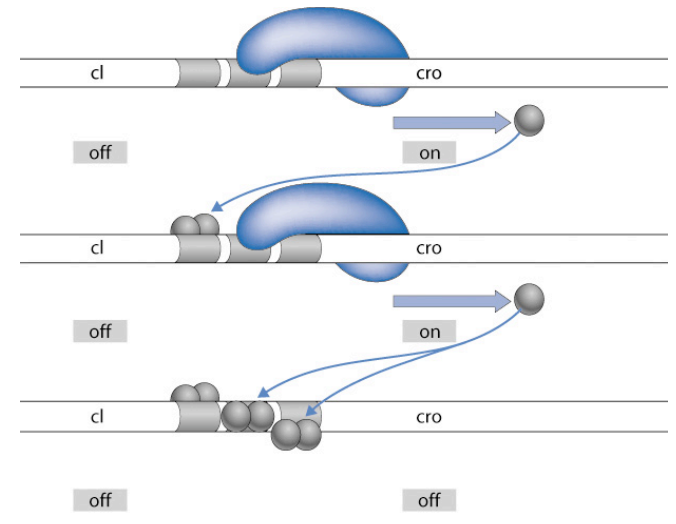
$$E_{bend} = \frac{\pi d_p k_B T}{R}$$



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 Chapter 1, Figure 4



*A Genetic Switch*, 3rd edition, 2004  
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 Chapter 1, Figure 23

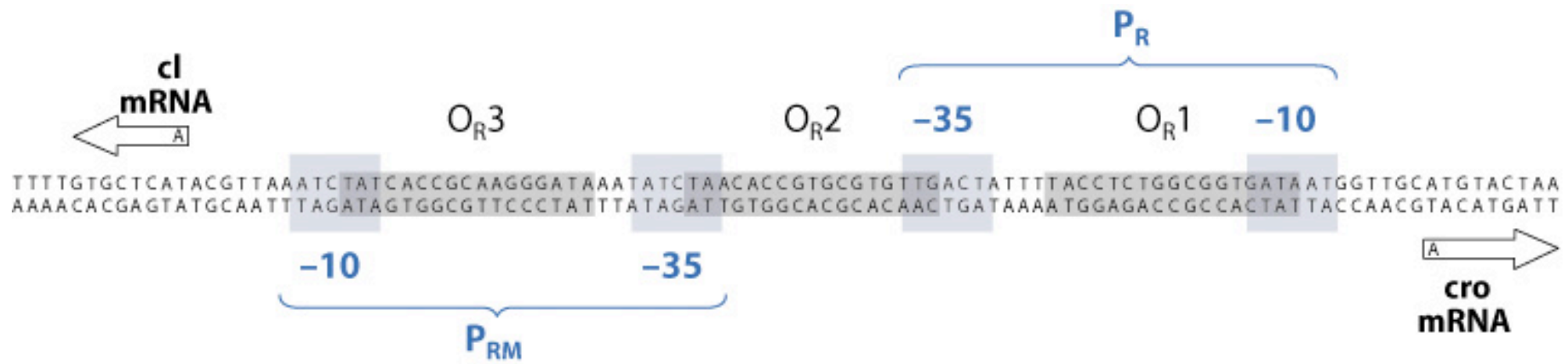


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 Chapter 1, Figure 24

$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# DNA Geography of the Switch

$$E_{bend} = \frac{\pi \frac{d}{2} k_B T}{R}$$

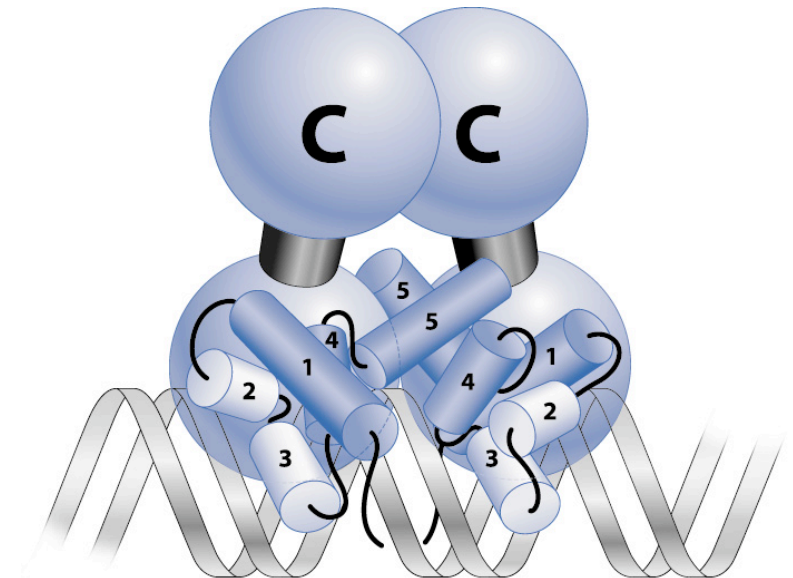
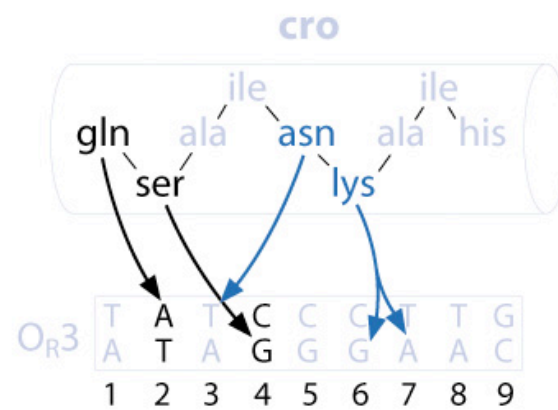
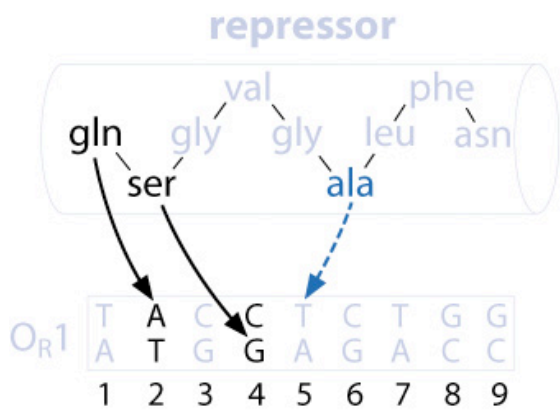


*A Genetic Switch*, 3rd edition, 2004  
 © Cold Spring Harbor Laboratory Press  
 Chapter 2, Figure 16

$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Binding of Transcription Factors

$$E_{bend} = \frac{\pi d_p k_B T}{R}$$



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 Chapter 2, Figure 11a

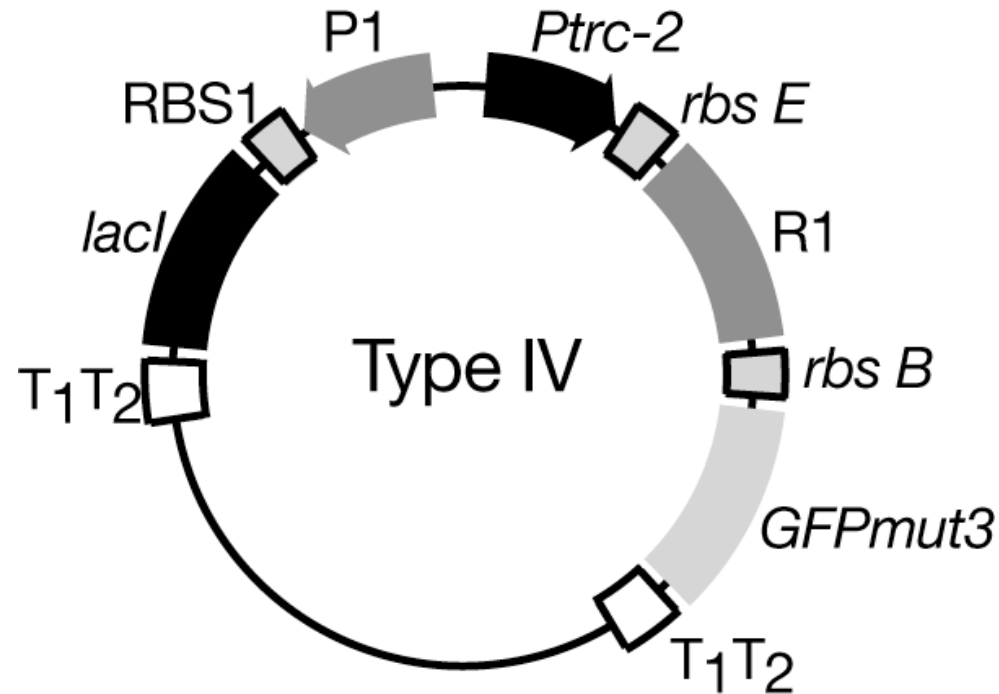
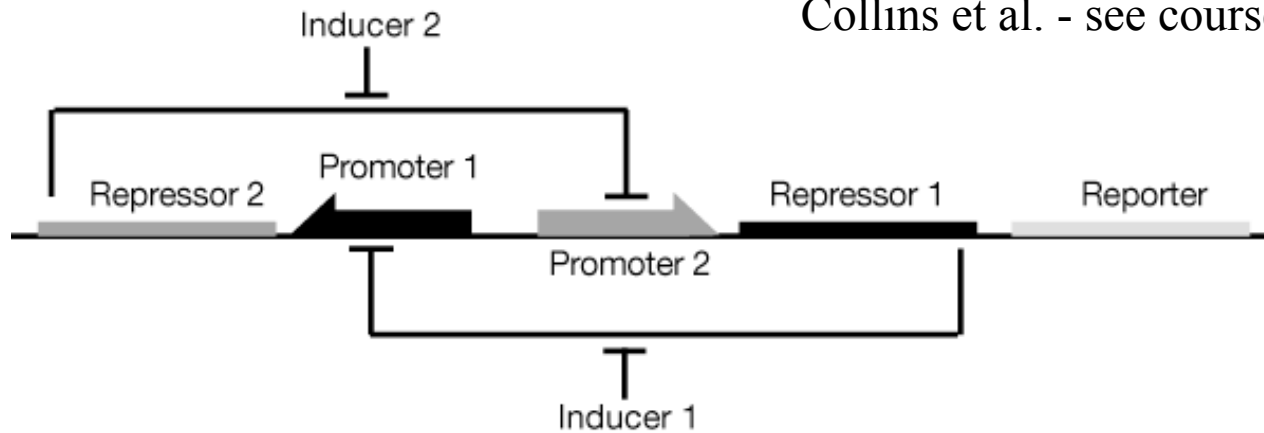
*A Genetic Switch*, 3rd edition, 2004  
 © Cold Spring Harbor Laboratory Press  
 Chapter 2, Figure 6

$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Synthetic Genetic Switch

$$E_{bend} = \frac{\pi d_p k_B T}{R}$$

Collins et al. - see course website

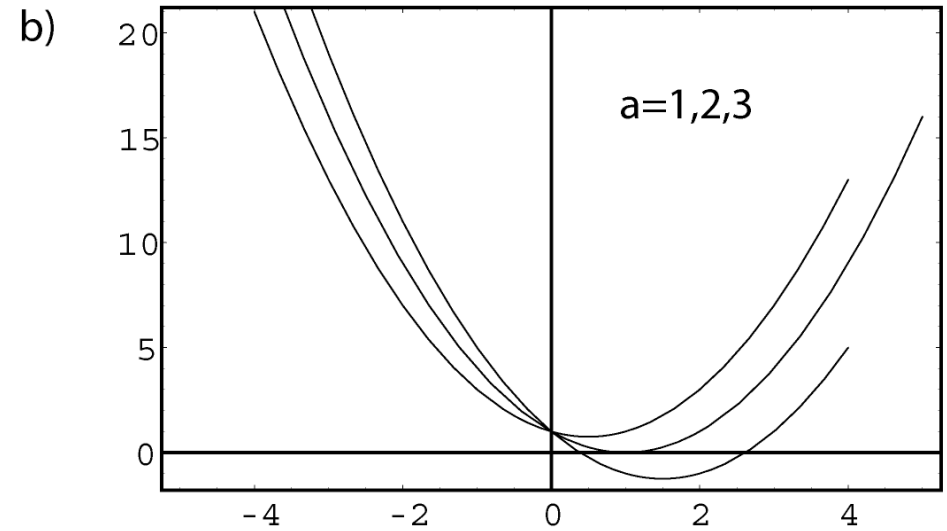
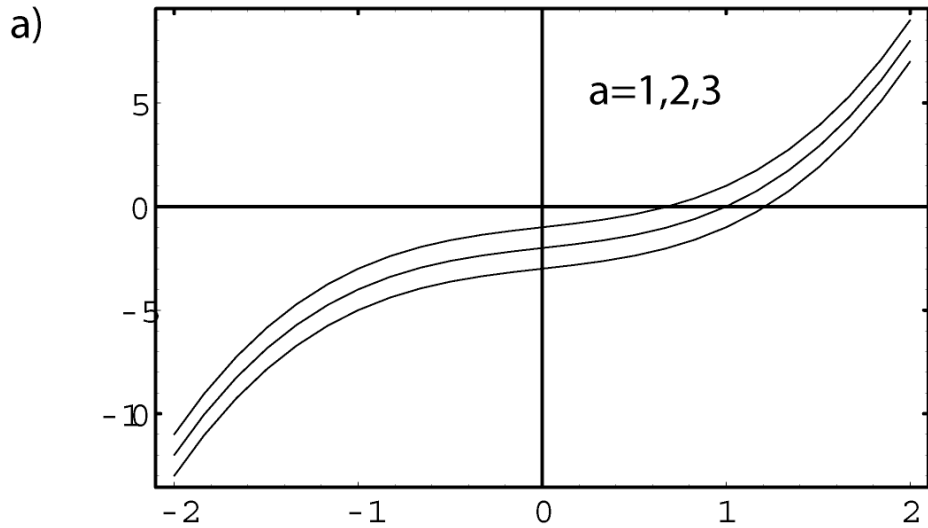




$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln n_{bp}$$

# Stable Solutions

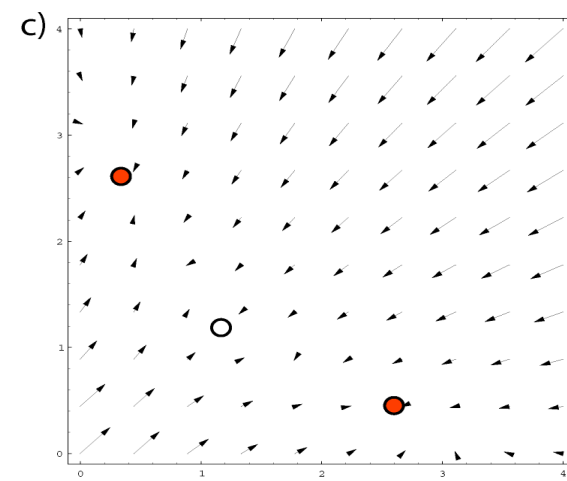
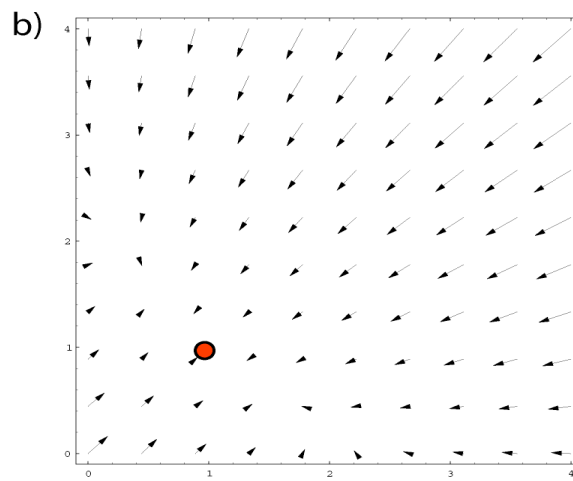
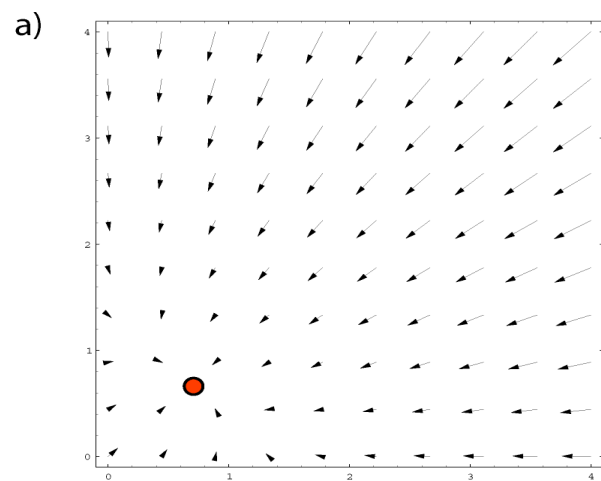
$$E_{\text{bend}} = \frac{\pi \frac{d}{2} k_B T}{R}$$



$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln n_{bp}$$

# Phase Portrait for the Switch

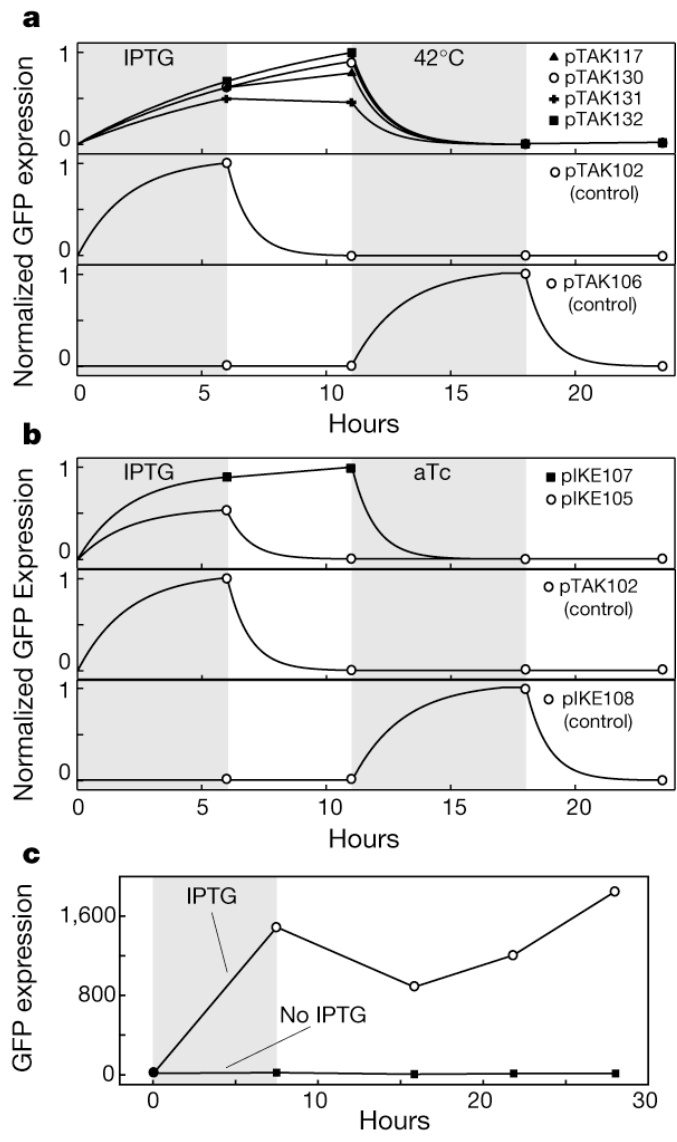
$$E_{\text{bend}} = \frac{\pi d_p k_B T}{R}$$



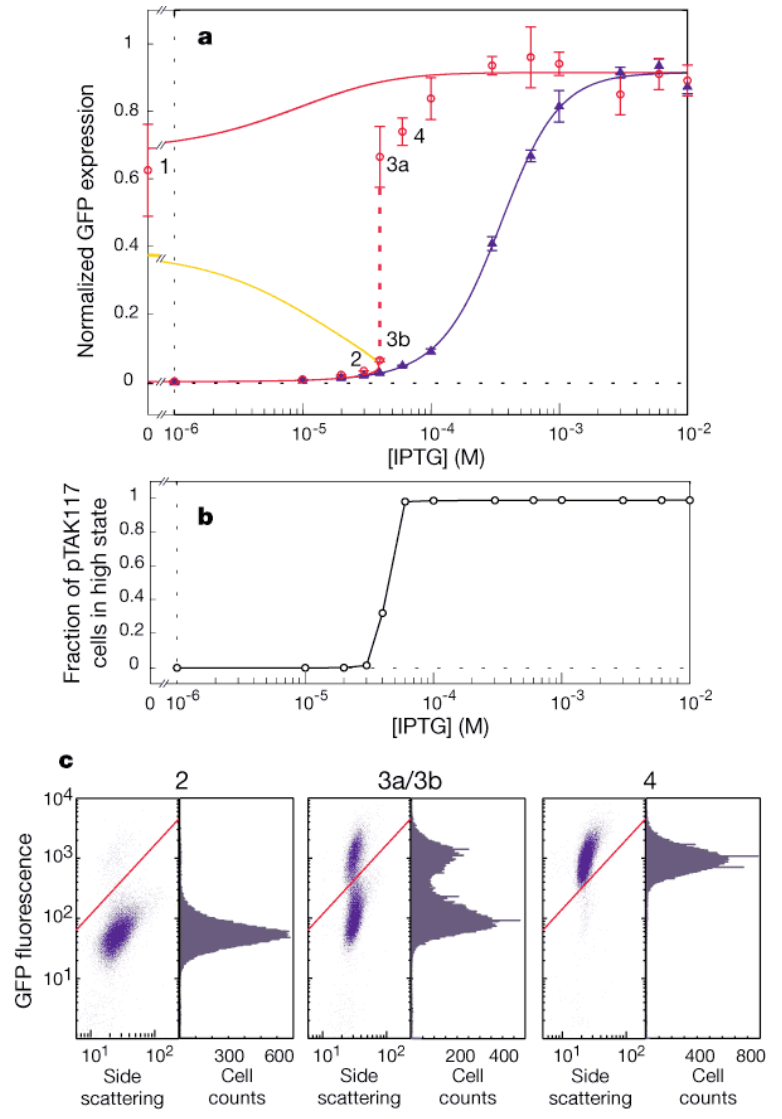
$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Synthetic Genetic Switch

$$E_{bend} = \frac{\pi \frac{d}{2} k_B T}{R}$$



Collins et al. - see course website



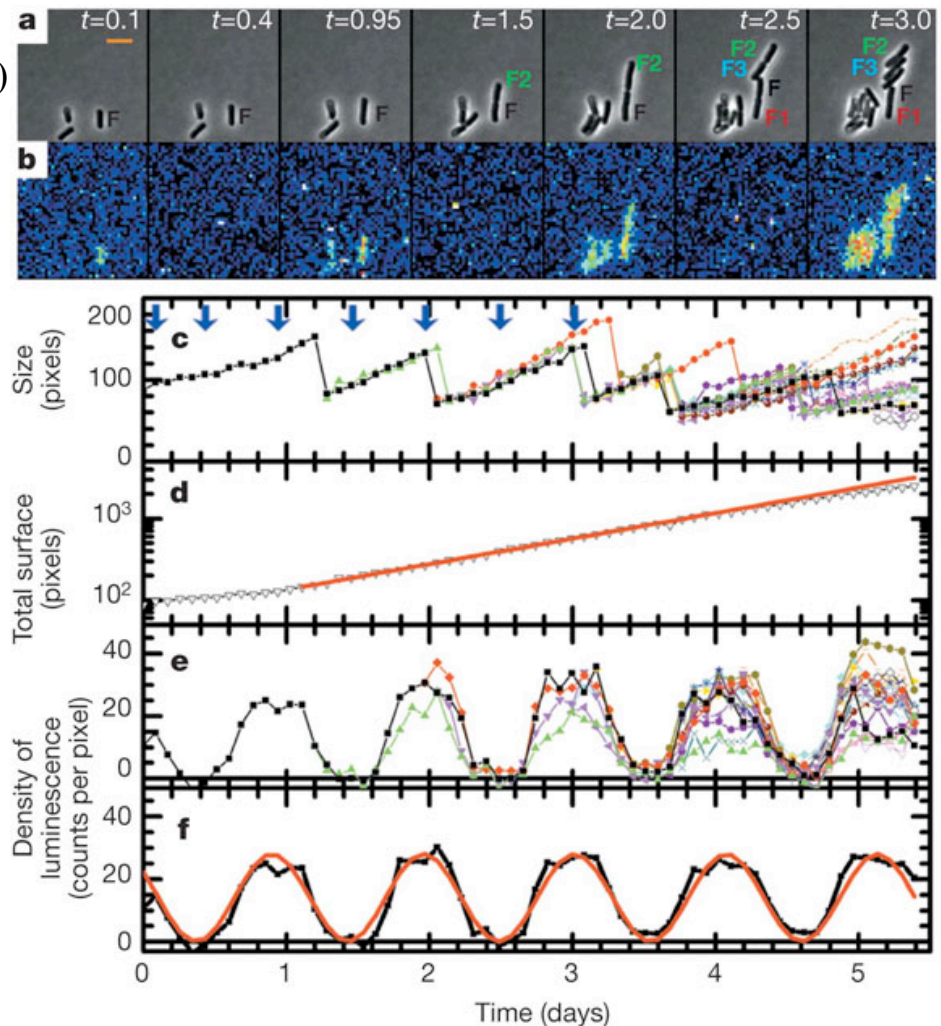
$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Gene Expression in Cyanobacteria

$$F_{bend} = \frac{\pi \frac{d}{p} k_B T}{R}$$

(Mihalcescu, Hsing, Leibler, Nature 2004)

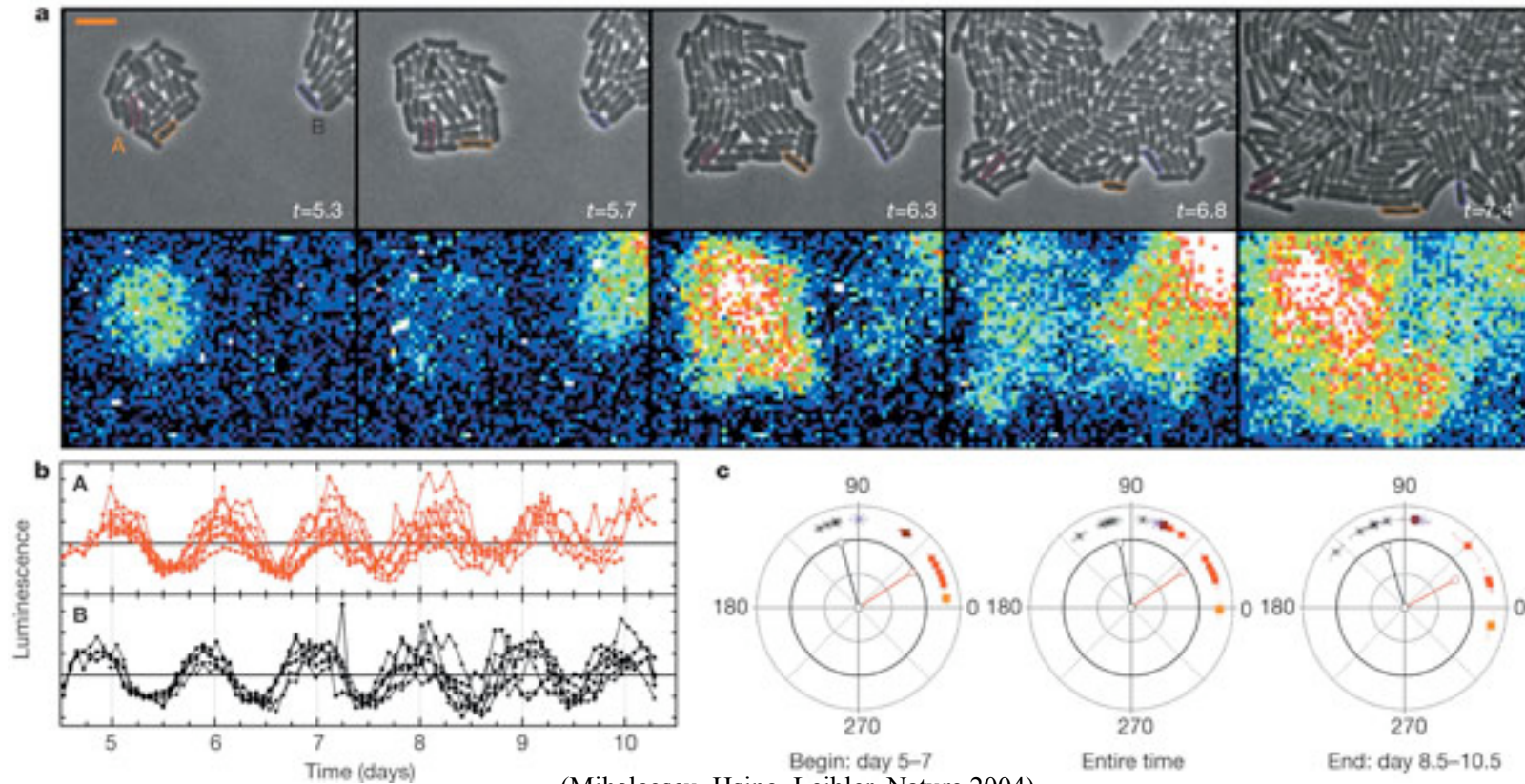
a, Snapshots of phase-contrast image showing cell F and its progeny and b, related bioluminescence image at different times  $t$  (given in days, a 24 h period of time) from the beginning of the measurement. Pixels in the bioluminescence images were binned 3 times 3 (pseudo-colour, where red is high signal intensity and blue is low signal intensity). Scale bar, 5 microm. c, The size of the cell F and all its progeny as a function of time measured from the phase-contrast images (non-binned pixels). The arrows point to the time where the snapshots in (a) and (b) were taken. d, The total number of pixels occupied by F and its all progeny versus time (black line) plotted in a logarithmic scale. The red line is the corresponding exponential growth fit: total size ( $t$ ) = initial size times  $2^{t/\tau}$  with  $\tau = 23.04$  plusminus  $0.17$  h. e, Density of bioluminescence for the same cell and all its progeny versus time. f, The average density of bioluminescence versus time (black line) and its fit (red line) with:  $\text{left fenced}(t)\text{right fence} = B + A \cos(2\pi t/T_0 + \phi_0)$ . The resulting period is  $T_0 = 25.4$  plusminus  $0.12$  h, the initial phase  $\phi_0 = 52$  plusminus  $2.8^\circ$ , the amplitude  $A = 12.9$  plusminus  $0.3$  counts per pixel and the offset  $B = 14.8$  plusminus  $0.3$  counts per pixel.



$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Gene Expression in Cyanobacteria

$$F_{bend} = \frac{\pi d_p k_B T}{R}$$



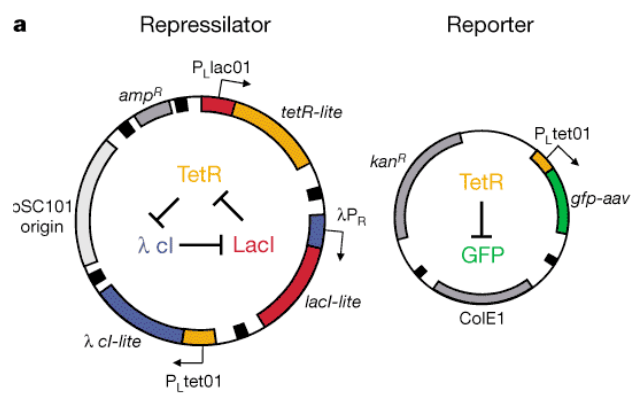
(Mihalcescu, Hsing, Leibler, Nature 2004)

a, Upper part shows the phase-contrast snapshots of colonies A and B; lower part shows the related bioluminescence images. Scale bar, 5 microm. b, Normalized density of bioluminescence of individual cyanobacterial cells. Each colour corresponds to the progeny from one of the initial cells: red line, colony A; black line, colony B. c, Phase of individual oscillators as a function of their original colony and their evolution in time: red square, colony A; asterisk, colony B. An example of the exact location for three of the cells tracked and their phase evolution is shown, marked by the corresponding coloured lines: magenta, orange and purple. The change of the phase in time was quantified by a fit over a different period of time: the first 2 days (days 5-7), the entire time (days 5-10.5) and the last 2 days of the measurement (days 8.5-10.5). The fit function is  $f(t) = B + A \cos(2\pi t/T_0 + \phi)$ , with  $T_0 = 24.78$  h. The line segments in each graph, with corresponding colours, represent the resulting vector  $\text{Pres} = \sum \text{Pi}$ , where  $\text{Pi}$  is the unit vector whose orientation is the measured angle of the same colony cell  $i$ .

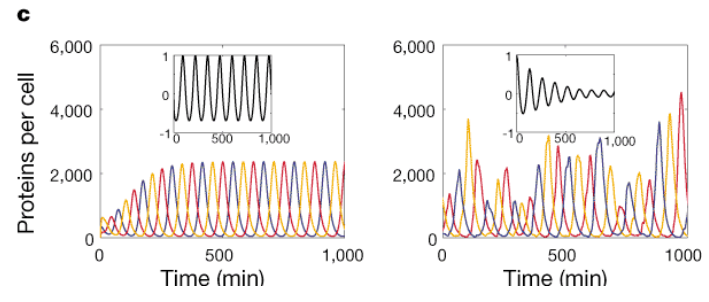
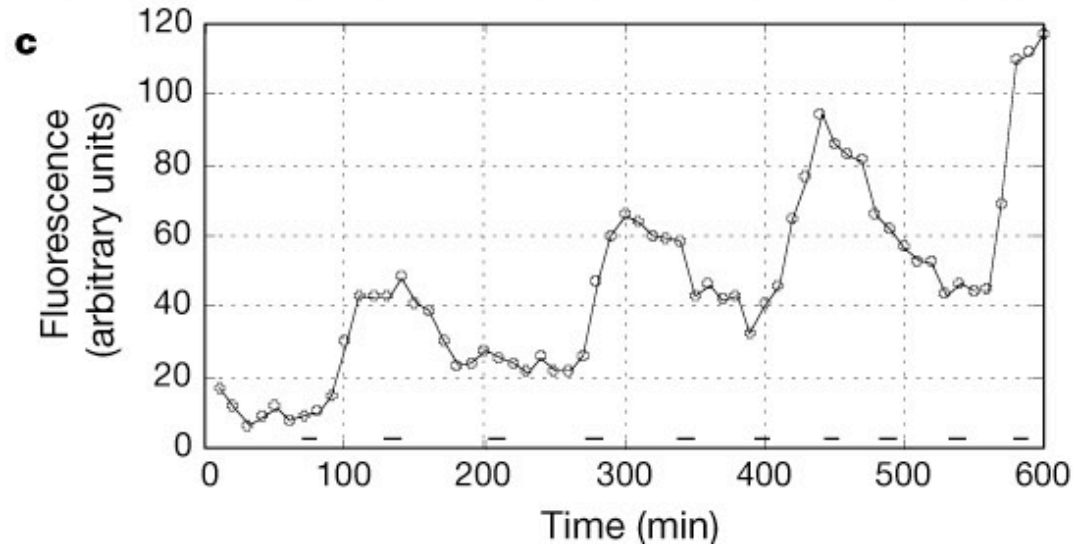
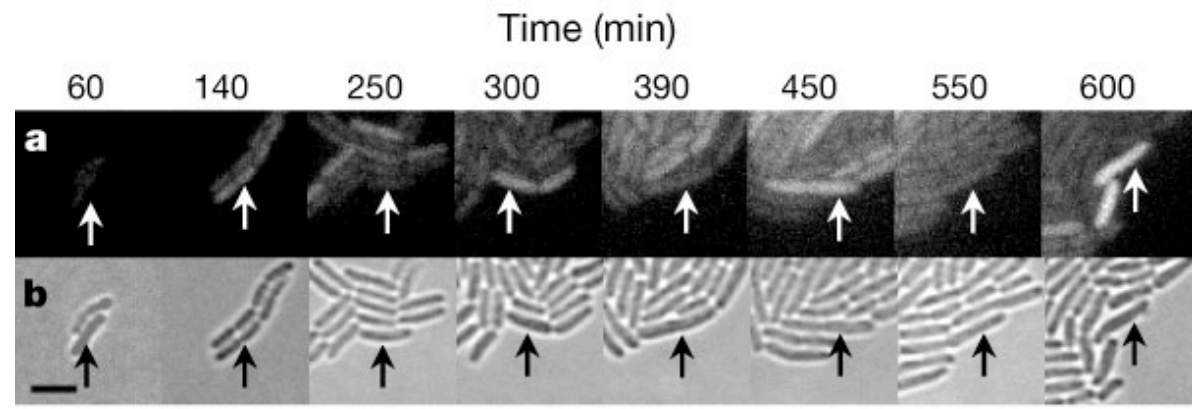
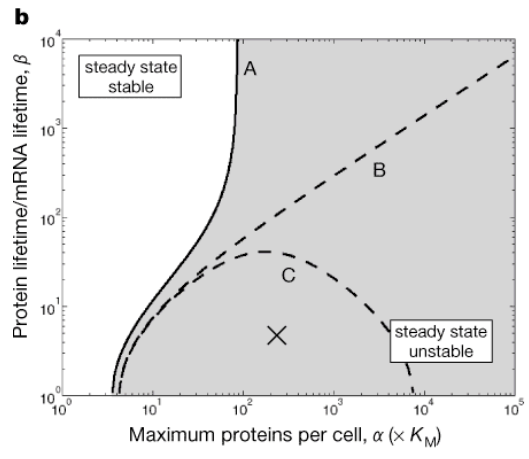
$$F(n_{bp}) = \frac{\alpha}{n_{bp}} + \gamma \ln N_{bp}$$

# Synthetic Transcriptional Oscillator

$$E_{bend} = \frac{\pi d_p k_B T}{R}$$



(Elowitz, Leibler, Nature 2002)



$$F(N_{bp}) = \frac{\alpha}{N_{bp}} + \gamma \ln N_{bp}$$

# Coupling of Genes in Networks

$$E_{bend} = \frac{\pi \frac{d}{2} k_B T}{R}$$

