# Supplementary Data <br> Reduced amino acid alphabets improve the sensitivity and selectivity of pairwise sequence alignments 

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## I. ACTIN HOMOLOGS

Fig. S1 highlights an example of three proteins with extensive structural but scant sequence similarity, in this case between ParM, which is encoded on a transferable plasmid found in bacteria such as E. coli; actin, which is found in eukaryotes, and Ta0583, a recently crystallized protein found in the archaeon T. acidophilum.


Figure S1: Comparison of sequence vs structural similarity. This schematic shows eukaryotic actin from humans and two actin homologs, prokaryotic ParM from E. coli and archaeal Ta0583 from T. acidophilum. These three proteins share a common fold but have very low sequence identity, illustrated here by comparing sequence vs structural agreement following superposition of the three structures. In both panels A and B red indicates low, white moderate and blue high agreement. In panel A we see that sequence conservation is poor between the three proteins overall, with only a few residues conserved identically in all three (blue) or in two of three (white). In panel B we observe that the structures themselves show much higher similarity; the structures of ParM and Ta0583 are colored by the RMSD of their $\alpha$-carbon backbones from actin with red indicating $\approx 12 \AA$ deviation, white $\approx 6 \AA$ deviation and blue indicating near overlap. There are numerous examples of proteins in this "twilight zone" [1] of low sequence identity ( $\lesssim 25 \%$ ) that have a common fold. The proteins shown here were aligned using STAMP [7], included in the MultiSeq [6] extension of VMD [2] and the figure was made with MolScript v2.1.2 [3]. The PDB accession codes are 1yag for actin, 1 mwm for ParM and 2fsj for Ta0583.

## II. ADDITIONAL RESULTS

## A. Mean pooled precision

Precision vs. recall curves are shown in panel A of Fig. S2 for GBMR4, HSDM17 and SDM12; the mean pooled precision is the area under this curve. The mean pooled precision for all of the HSDM, SDM, and GBMR alphabets is plotted in panel B of Fig. S2.


Figure S2: Reduced alphabet performance in mean pooled precision (A) Precision vs. recall curves for the top reduced alphabet performers. The mean pooled precision is the area under this curve and indicates the ability of a particular matrix to maintain high selectivity over a wide range of error rates. At some point, each matrix loses the ability to selectively reject false positives and the curve drops precipitously to low precision values. (B) Mean pooled precision indicates the average precision achieved by a matrix over the entire range of recall. Points indicate reduced alphabets that were tested; the connecting lines are a guide to the eye. A perfect method would achieve a mean pooled precision value of unity, with all true positives ranked ahead of false ones. The HSDM17 matrix is the top performer in this metric; the dashed black lines in panels A and B show the performance of BL62 11/1 for reference.

## B. Area under the ROC curve

Receiver Operating Characteristic curves are shown in Fig. S3(A) for SDM12, HSDM17 and GBMR4. The total area under the curve vs. number of letters in these schemes is shown in panel B.


Figure S3: Reduced alphabet performance in area under the Receiver Operating Characteristic curve. (A) Receiver Operating Characteristic (ROC) curves for the top performing alphabets. The integral of this curve gives a measure of how well the entire pooled list of hits is sorted; a perfect method would have an ROC area of unity. (B) Overall sensitivity of the SDM alphabets as measured by the area under the ROC curve. The level of sensitivity of BL62 $11 / 1$ is shown with the black dashed line. Points indicate reduced alphabets that were tested; the connecting lines are a guide to the eye.

## C. Recall at 0.01 EPQ

Panel A of Fig. S4 shows the recall vs. error rate curves under linear normalization for GBMR4, HSDM17 and SDM12 with better-performing matrices generating curves that tend toward the lower-right hand corner indicating high recall at low error rates. Comparing this with panel A of Fig. S2 we can see that GBMR4 is able to maintain the highest level of precision initially, but it rapidly loses precision at higher recall values. Panel B of Fig. S4 shows the recall at 0.01 EPQ with linear normalization vs. number of letters for the GBMR, SDM and HSDM alphabets.


Figure S4: Reduced alphabet performance in recall vs. errors per query with linear normalization. (A) Linearly normalized recall (or coverage) vs. the number of errors per query (EPQ). Curves that tend toward the lower right-hand corner perform better, detecting more true positives at a given error rate. Small alphabets show good performance at lower error rates (EPQ $<0.1$ ) with GBMR4 being the top performer. (B) Recall with linear normalization at 0.01 EPQ for various numbers of letters in the GBMR, HSDM and SDM reduced alphabet schemes. The level of performance of BL62 11/1 is shown with the black dashed line. Points indicate reduced alphabets that were tested; the connecting lines are a guide to the eye.

## III. ALIGNMENT ACCURACY

We evaluated how well pairwise sequence alignments with reduced alphabets identified pairs of residues that are structurally equivalent as defined by DALI. The results are shown in Fig. S5, plotted as the fraction of structurally equivalent residue pairs identified by SSEARCH using the SDM, HSDM and GBMR reduced alphabet schemes. The curves tend to saturate at around 10 letters, implying that expanding the alphabet beyond this point does not improve the alignments but tends to increase their sensitivity to more recently diverged proteins. The top 10 finishers in alignment accuracy are shown in Table I; HSDM and SDM show the best performance which is not surprising given that they were derived from structurally equivalent pairs of residues [5]. It is interesting that the highly simplified GBMR4 alphabet is able to achieve nearly the same level of accuracy as the full BL62 11/1 matrix. The DALI database of structurally equivalent residues is an exceedingly challenging test of pairwise sequence comparison since the equivalenced residues share only $11 \%$ identity overall; even the best alphabet, HSDM17, achieves exact agreement with less than one tenth of all residues in the DALI structural alignments.


Figure S5: Agreement of structural and sequence alignments. The fraction of DALI equivalent residue pairs found by SSEARCH alignment is shown for various reduced alphabet schemes. Most of the gains are made as classes are added up until around 10 classes, after which the performance levels off. Points indicate reduced alphabets that were tested; the connecting lines are a guide to the eye.

| Rank | Scheme | Letters | Fraction aligned |
| :---: | :---: | :---: | :---: |
| 1 | HSDM | 17 | 0.08887 |
| 2 | HSDM | 20 | 0.08882 |
| 3 | HSDM | 14 | 0.08862 |
| 4 | HSDM | 15 | 0.08857 |
| 5 | HSDM | 16 | 0.08849 |
| 6 | HSDM | 9 | 0.08714 |
| 7 | HSDM | 10 | 0.08691 |
| 8 | SDM | 11 | 0.08686 |
| 9 | HSDM | 12 | 0.08676 |
| 10 | SDM | 13 | 0.08675 |

TABLE I: The top 10 performers in agreement between sequence and structural alignments, using DALI structurally equivalent residues as the "gold standard". As expected, the two structure-derived matrices, HSDM and SDM, completely dominate the results.

## IV. COMPARISON OF DETECTED RELATIONSHIPS

It is also valuable to compare the hits returned by two matrices at a given errors per query level to see what types of relationships are more easily detected by one relative to another. We compared the hits returned by the SDM12 and BL62 11/1 matrices at or above 0.01 EPQ and found that each matrix finds about 3000 true positives at that error level. After separating out the hits that were unique to each matrix (they share 2724 hits in common) SDM12 was left with 271 unique hits and BL62 11/1 with 139. The approximate mean percent identity of the SDM12 unique hits is $60 \%$ whereas for BL62 11/1 it is $70 \%$. Although SDM12 and BL62 have essentially identical relative entropy ( -0.703 and -0.699 bits respectively) SDM12 is able to detect more distant relationships than BL62. A histogram of the hits unique to each matrix is shown in Fig. S6.


Figure S6: Histogram (non-stacked) of the hits at or above 0.01 errors per query unique to the SDM12 and BL62 11/1 matrices. The results from SDM12 are both more numerous and shifted towards lower identity, showing its increased ability to detect more remote relationships.

## V. PRELIMINARY SCOP STUDY RESULTS

In the main text we refer to a study of all vs. all alignments with HSDM17, SDM12, GBMR4 and BL62 11/1 using proteins belonging to the same SCOP superfamily to define true positives [4]. The complete results of this smallscale study are shown in Table II below, with best results in bold. The HSDM17 and SDM12 schemes maintain an advantage over BL62 11/1 in the SCOP study, while the smaller GBMR4 alphabet does not perform as well relative to BL62 $11 / 1$ as it did in the DALI study. At both the $40 \%$ and $95 \%$ levels of identity, the HSDM17 alphabet performed best with the SCOP databases in mean precision, area under the ROC curve and linearly normalized recall. The SCOP database includes curation by experts to make judgements about the evolutionary relationships between proteins, whereas DALI uses structural similarity alone as the criteria for determining relatedness.

|  | scop40 |  |  |  | scop95 |  |  | DALI |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scheme | MPP | AUC | Recall | MPP | AUC | Recall | MPP | AUC | Recall |  |
| GBMR4 | 0.089 | 0.658 | 0.100 | 0.259 | 0.727 | 0.204 | 0.212 | 0.667 | $\mathbf{0 . 0 2 2}$ |  |
| SDM12 | 0.156 | 0.734 | 0.136 | 0.419 | 0.833 | 0.250 | 0.332 | $\mathbf{0 . 8 0 1}$ | 0.020 |  |
| HSDM17 | $\mathbf{0 . 1 7 3}$ | $\mathbf{0 . 7 5 1}$ | $\mathbf{0 . 1 4 8}$ | $\mathbf{0 . 4 3 6}$ | $\mathbf{0 . 8 4 0}$ | $\mathbf{0 . 2 5 9}$ | $\mathbf{0 . 3 4 7}$ | 0.796 | 0.020 |  |
| BL62 11/1 | 0.156 | 0.714 | 0.134 | 0.408 | 0.812 | 0.245 | 0.329 | 0.759 | 0.019 |  |

TABLE II: Comparison of results from all vs. all studies with scop40, scop95 and DALI. In the SCOP results GMBR4 is unable to maintain its advantage in linearly normalized recall at 0.01 EPQ over BL62 11/1. However both SDM12 and HSDM17 are able to match or better the results of BL62 $11 / 1$ in mean pooled precision (MPP), area under the ROC curve (AUC) and linearly normalized recall at 0.01 EPQ . Version 1.71 of the scop40 and scop 95 sequence databases were used.

## VI. DALI STUDY RESULTS

## A. Top 10 performers

| (A) Mean pooled precision (B) Area under ROC curve |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rank | Scheme | Groups | MPP | Scheme Groups | AUC | Scheme | Groups Recall 0.01 EPQ |  |  |
| 1 | HSDM | 17 | 0.347 | SDM | 12 | 0.801 | GBMR | 4 | 0.022 |
| 2 | BL62 $7 / 1$ | 20 | 0.347 | SDM | 11 | 0.800 | CB/LW | 2 | 0.021 |
| 3 | BL50 11/1 | 20 | 0.346 | SDM | 13 | 0.800 | HSDM | 2 | 0.021 |
| 4 | LZ-BL | 16 | 0.346 | HSDM | 17 | 0.796 | LZ-BL | 7 | 0.021 |
| 5 | HSDM | 20 | 0.345 | SDM | 14 | 0.795 | SDM | 8 | 0.021 |
| 6 | HSDM | 16 | 0.344 | LZ-MJ | 6 | 0.793 | TD | 2 | 0.021 |
| 7 | HSDM | 15 | 0.343 | HSDM | 20 | 0.791 | BL50 11/1 | 20 | 0.021 |
| 8 | HSDM | 14 | 0.341 | HSDM | 16 | 0.789 | LZ-BL | 6 | 0.020 |
| 9 | LZ-BL | 15 | 0.339 | HSDM | 9 | 0.784 | HSDM | 20 | 0.020 |
| 10 | SDM | 13 | 0.335 | HSDM | 15 | 0.783 | SDM | 7 | 0.020 |

TABLE III: Top 10 performers in mean pooled precision (MPP), area under the Receiver Operating Characteristic curve (AUC) and recall at 0.01 errors per query with linear normalization. Mean pooled precision is a measure of the selectivity of a matrix i.e. its ability to retain high recall of true positive relationships at low error rates. The area under the ROC curve measures the sensitivity of a matrix to true positive alignments over the entire list of results. Recall at 0.01 EPQ measures the selectivity of a matrix but is drawn from a limited set of hits such as a researcher might reasonably peruse manually.

## B. Complete DALI study results

TABLE IV: Results for all alphabets and matrices tested

|  |  |  |  |  | Recall at 0.01 EPQ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scheme | Letters | AUC | MPP | Align | None | Linear | Quadratic |
| AB | 2 | 0.665 | 0.159 | 0.04844 | 0.0026 | 0.020 | 0.034 |
| AB | 3 | 0.674 | 0.178 | 0.04968 | 0.0025 | 0.019 | 0.033 |
| AB | 4 | 0.682 | 0.194 | 0.05828 | 0.0026 | 0.020 | 0.034 |
| AB | 5 | 0.702 | 0.206 | 0.06143 | 0.0025 | 0.019 | 0.033 |
| AB | 6 | 0.719 | 0.210 | 0.05877 | 0.0024 | 0.019 | 0.034 |
| AB | 7 | 0.731 | 0.234 | 0.06827 | 0.0025 | 0.019 | 0.033 |
| AB | 8 | 0.721 | 0.252 | 0.07310 | 0.0026 | 0.020 | 0.034 |
| AB | 9 | 0.728 | 0.294 | 0.07554 | 0.0026 | 0.019 | 0.033 |
| AB | 10 | 0.740 | 0.297 | 0.07509 | 0.0026 | 0.020 | 0.034 |
| AB | 11 | 0.749 | 0.310 | 0.07690 | 0.0027 | 0.020 | 0.034 |
| AB | 12 | 0.749 | 0.313 | 0.07736 | 0.0027 | 0.020 | 0.034 |
| AB | 13 | 0.750 | 0.312 | 0.07610 | 0.0027 | 0.020 | 0.034 |
| AB | 14 | 0.755 | 0.314 | 0.07599 | 0.0026 | 0.020 | 0.034 |
| AB | 15 | 0.753 | 0.319 | 0.07603 | 0.0026 | 0.020 | 0.033 |
| AB | 16 | 0.754 | 0.320 | 0.07648 | 0.0026 | 0.019 | 0.033 |
| AB | 17 | 0.752 | 0.322 | 0.07702 | 0.0026 | 0.019 | 0.033 |
| AB | 18 | 0.756 | 0.326 | 0.07876 | 0.0026 | 0.020 | 0.034 |
| AB | 19 | 0.757 | 0.323 | 0.07828 | 0.0026 | 0.019 | 0.033 |
| BL50 11/1 | 20 | 0.779 | 0.346 | 0.08476 | 0.0027 | 0.021 | 0.035 |
| BL50 12/2 | 20 | 0.762 | 0.334 | 0.08111 | 0.0026 | 0.020 | 0.034 |
| BL62 11/1 | 20 | 0.759 | 0.329 | 0.08322 | 0.0025 | 0.019 | 0.033 |
| CB | 2 | 0.705 | 0.188 | 0.06774 | 0.0029 | 0.021 | 0.035 |
| CB | 5 | 0.674 | 0.191 | 0.05904 | 0.0024 | 0.018 | 0.031 |
| DSSP | 2 | 0.679 | 0.154 | 0.05393 | 0.0044 | 0.019 | 0.033 |
| DSSP | 3 | 0.731 | 0.209 | 0.07479 | 0.0025 | 0.020 | 0.034 |
| DSSP | 4 | 0.709 | 0.222 | 0.07996 | 0.0027 | 0.020 | 0.033 |
| DSSP | 5 | 0.723 | 0.219 | 0.07736 | 0.0026 | 0.019 | 0.032 |
| DSSP | 6 | 0.729 | 0.230 | 0.07913 | 0.0025 | 0.019 | 0.033 |
| DSSP | 7 | 0.738 | 0.246 | 0.08042 | 0.0025 | 0.019 | 0.032 |
| DSSP | 8 | 0.730 | 0.233 | 0.07572 | 0.0024 | 0.018 | 0.031 |
| DSSP | 9 | 0.731 | 0.244 | 0.07631 | 0.0024 | 0.019 | 0.033 |
| DSSP | 10 | 0.733 | 0.253 | 0.07740 | 0.0025 | 0.019 | 0.032 |
| DSSP | 11 | 0.757 | 0.282 | 0.07829 | 0.0026 | 0.019 | 0.033 |
| DSSP | 12 | 0.759 | 0.287 | 0.07942 | 0.0026 | 0.019 | 0.033 |
| DSSP | 13 | 0.758 | 0.290 | 0.08084 | 0.0026 | 0.019 | 0.033 |
| DSSP | 14 | 0.768 | 0.297 | 0.08252 | 0.0026 | 0.020 | 0.034 |
| GBMR | 2 | 0.605 | 0.091 | 0.02423 | 0.0029 | 0.018 | 0.032 |
| GBMR | 3 | 0.614 | 0.122 | 0.03261 | 0.0025 | 0.020 | 0.035 |

TABLE IV: Results for all alphabets and matrices tested (continued)

|  |  |  |  |  | Recall at 0.01 EPQ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scheme | Letters | AUC | MPP | Align | None | Linear | Quadratic |
| GBMR | 4 | 0.667 | 0.212 | 0.07676 | 0.0029 | 0.022 | 0.036 |
| GBMR | 5 | 0.678 | 0.220 | 0.07549 | 0.0027 | 0.020 | 0.033 |
| GBMR | 6 | 0.691 | 0.196 | 0.06778 | 0.0097 | 0.019 | 0.031 |
| GBMR | 7 | 0.709 | 0.202 | 0.06784 | 0.0089 | 0.019 | 0.032 |
| GBMR | 8 | 0.716 | 0.205 | 0.06857 | 0.0085 | 0.020 | 0.032 |
| GBMR | 9 | 0.719 | 0.206 | 0.06871 | 0.0067 | 0.018 | 0.030 |
| GBMR | 10 | 0.726 | 0.217 | 0.07052 | 0.0038 | 0.020 | 0.033 |
| GBMR | 11 | 0.735 | 0.240 | 0.07264 | 0.0028 | 0.019 | 0.032 |
| GBMR | 12 | 0.738 | 0.240 | 0.07098 | 0.0027 | 0.020 | 0.035 |
| GBMR | 13 | 0.742 | 0.250 | 0.07096 | 0.0026 | 0.020 | 0.034 |
| GBMR | 14 | 0.742 | 0.249 | 0.07022 | 0.0026 | 0.020 | 0.034 |
| HSDM | 2 | 0.725 | 0.199 | 0.07214 | 0.0029 | 0.021 | 0.036 |
| HSDM | 3 | 0.732 | 0.203 | 0.07266 | 0.0026 | 0.020 | 0.034 |
| HSDM | 4 | 0.726 | 0.210 | 0.07306 | 0.0026 | 0.019 | 0.034 |
| HSDM | 5 | 0.751 | 0.234 | 0.07562 | 0.0027 | 0.019 | 0.034 |
| HSDM | 6 | 0.751 | 0.262 | 0.07827 | 0.0027 | 0.020 | 0.035 |
| HSDM | 7 | 0.751 | 0.279 | 0.08154 | 0.0028 | 0.020 | 0.033 |
| HSDM | 8 | 0.759 | 0.295 | 0.08235 | 0.0027 | 0.020 | 0.034 |
| HSDM | 9 | 0.784 | 0.319 | 0.08714 | 0.0028 | 0.020 | 0.033 |
| HSDM | 10 | 0.776 | 0.325 | 0.08691 | 0.0027 | 0.020 | 0.034 |
| HSDM | 12 | 0.771 | 0.323 | 0.08676 | 0.0026 | 0.020 | 0.035 |
| HSDM | 14 | 0.783 | 0.341 | 0.08862 | 0.0027 | 0.020 | 0.035 |
| HSDM | 15 | 0.783 | 0.343 | 0.08857 | 0.0026 | 0.020 | 0.035 |
| HSDM | 16 | 0.789 | 0.344 | 0.08849 | 0.0026 | 0.020 | 0.035 |
| HSDM | 17 | 0.796 | 0.347 | 0.08887 | 0.0027 | 0.020 | 0.035 |
| HSDM | 20 | 0.791 | 0.345 | 0.08882 | 0.0026 | 0.020 | 0.036 |
| JO20 | 20 | 0.725 | 0.274 | 0.05900 | 0.0024 | 0.019 | 0.033 |
| LR | 10 | 0.719 | 0.280 | 0.07019 | 0.0026 | 0.020 | 0.034 |
| LW-I | 2 | 0.705 | 0.188 | 0.06774 | 0.0029 | 0.021 | 0.035 |
| LW-I | 3 | 0.720 | 0.203 | 0.06403 | 0.0027 | 0.020 | 0.034 |
| LW-I | 4 | 0.697 | 0.232 | 0.07038 | 0.0026 | 0.019 | 0.032 |
| LW-I | 5 | 0.701 | 0.227 | 0.06388 | 0.0027 | 0.020 | 0.034 |
| LW-I | 6 | 0.695 | 0.241 | 0.06369 | 0.0027 | 0.020 | 0.034 |
| LW-I | 7 | 0.688 | 0.240 | 0.06681 | 0.0026 | 0.020 | 0.033 |
| LW-I | 8 | 0.737 | 0.286 | 0.07320 | 0.0026 | 0.020 | 0.034 |
| LW-I | 9 | 0.740 | 0.290 | 0.07389 | 0.0026 | 0.020 | 0.035 |
| LW-I | 10 | 0.728 | 0.292 | 0.07218 | 0.0025 | 0.019 | 0.033 |
| LW-I | 11 | 0.735 | 0.303 | 0.07579 | 0.0026 | 0.020 | 0.035 |
| LW-I | 12 | 0.740 | 0.303 | 0.07605 | 0.0026 | 0.020 | 0.034 |
| LW-I | 13 | 0.754 | 0.310 | 0.07662 | 0.0026 | 0.020 | 0.034 |

TABLE IV: Results for all alphabets and matrices tested (continued)

|  |  |  |  |  | Recall at 0.01 EPQ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scheme | Letters | AUC | MPP | Align | None | Linear | Quadratic |
| LW-I | 14 | 0.756 | 0.307 | 0.07569 | 0.0025 | 0.020 | 0.034 |
| LW-I | 15 | 0.757 | 0.308 | 0.07593 | 0.0025 | 0.020 | 0.034 |
| LW-I | 16 | 0.754 | 0.314 | 0.07599 | 0.0026 | 0.020 | 0.034 |
| LW-I | 17 | 0.752 | 0.317 | 0.07619 | 0.0026 | 0.020 | 0.034 |
| LW-I | 18 | 0.753 | 0.318 | 0.07663 | 0.0026 | 0.020 | 0.034 |
| LW-I | 19 | 0.755 | 0.321 | 0.07693 | 0.0026 | 0.020 | 0.034 |
| LW-NI | 2 | 0.705 | 0.188 | 0.06774 | 0.0029 | 0.021 | 0.035 |
| LW-NI | 3 | 0.720 | 0.203 | 0.06403 | 0.0027 | 0.020 | 0.034 |
| LW-NI | 4 | 0.723 | 0.224 | 0.06361 | 0.0025 | 0.019 | 0.032 |
| LW-NI | 5 | 0.702 | 0.229 | 0.06417 | 0.0026 | 0.019 | 0.032 |
| LW-NI | 6 | 0.707 | 0.243 | 0.06453 | 0.0026 | 0.019 | 0.033 |
| LW-NI | 7 | 0.698 | 0.245 | 0.06795 | 0.0026 | 0.020 | 0.033 |
| LW-NI | 8 | 0.698 | 0.244 | 0.06509 | 0.0025 | 0.020 | 0.034 |
| LW-NI | 9 | 0.696 | 0.249 | 0.06569 | 0.0025 | 0.019 | 0.034 |
| LW-NI | 10 | 0.706 | 0.263 | 0.06816 | 0.0025 | 0.020 | 0.034 |
| LW-NI | 11 | 0.739 | 0.292 | 0.07406 | 0.0025 | 0.020 | 0.034 |
| LW-NI | 12 | 0.740 | 0.303 | 0.07605 | 0.0026 | 0.020 | 0.034 |
| LW-NI | 13 | 0.754 | 0.310 | 0.07662 | 0.0026 | 0.020 | 0.034 |
| LW-NI | 14 | 0.756 | 0.312 | 0.07688 | 0.0027 | 0.020 | 0.034 |
| LW-NI | 15 | 0.757 | 0.308 | 0.07593 | 0.0025 | 0.020 | 0.034 |
| LW-NI | 16 | 0.754 | 0.314 | 0.07599 | 0.0026 | 0.020 | 0.034 |
| LW-NI | 17 | 0.752 | 0.317 | 0.07619 | 0.0026 | 0.020 | 0.034 |
| LW-NI | 18 | 0.753 | 0.318 | 0.07663 | 0.0026 | 0.020 | 0.034 |
| LW-NI | 19 | 0.755 | 0.321 | 0.07693 | 0.0026 | 0.020 | 0.034 |
| LZ-BL | 2 | 0.690 | 0.194 | 0.06969 | 0.0026 | 0.020 | 0.033 |
| LZ-BL | 3 | 0.719 | 0.217 | 0.07751 | 0.0026 | 0.019 | 0.033 |
| LZ-BL | 4 | 0.736 | 0.242 | 0.08056 | 0.0027 | 0.020 | 0.033 |
| LZ-BL | 5 | 0.734 | 0.282 | 0.08134 | 0.0028 | 0.020 | 0.034 |
| LZ-BL | 6 | 0.742 | 0.299 | 0.08337 | 0.0028 | 0.020 | 0.035 |
| LZ-BL | 7 | 0.744 | 0.297 | 0.08129 | 0.0027 | 0.021 | 0.036 |
| LZ-BL | 8 | 0.736 | 0.299 | 0.08115 | 0.0026 | 0.020 | 0.036 |
| LZ-BL | 9 | 0.744 | 0.300 | 0.08092 | 0.0026 | 0.020 | 0.034 |
| LZ-BL | 10 | 0.749 | 0.327 | 0.08417 | 0.0026 | 0.020 | 0.034 |
| LZ-BL | 11 | 0.750 | 0.325 | 0.08184 | 0.0026 | 0.020 | 0.035 |
| LZ-BL | 12 | 0.769 | 0.328 | 0.08326 | 0.0025 | 0.019 | 0.033 |
| LZ-BL | 13 | 0.774 | 0.331 | 0.08380 | 0.0026 | 0.020 | 0.034 |
| LZ-BL | 14 | 0.774 | 0.334 | 0.08391 | 0.0025 | 0.019 | 0.033 |
| LZ-BL | 15 | 0.777 | 0.339 | 0.08413 | 0.0026 | 0.020 | 0.034 |
| LZ-BL | 16 | 0.783 | 0.346 | 0.08451 | 0.0027 | 0.020 | 0.034 |
| LZ-MJ | 2 | 0.700 | 0.165 | 0.05816 | 0.0026 | 0.019 | 0.033 |

TABLE IV: Results for all alphabets and matrices tested (continued)

|  |  |  |  |  | Recall at 0.01 EPQ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scheme | Letters | AUC | MPP | Align | None | Linear | Quadratic |
| LZ-MJ | 3 | 0.666 | 0.173 | 0.05389 | 0.0023 | 0.018 | 0.032 |
| LZ-MJ | 4 | 0.722 | 0.203 | 0.06992 | 0.0024 | 0.019 | 0.032 |
| LZ-MJ | 5 | 0.779 | 0.221 | 0.07165 | 0.0022 | 0.017 | 0.031 |
| LZ-MJ | 6 | 0.793 | 0.220 | 0.07124 | 0.0022 | 0.018 | 0.031 |
| LZ-MJ | 7 | 0.770 | 0.246 | 0.07434 | 0.0023 | 0.018 | 0.030 |
| LZ-MJ | 8 | 0.750 | 0.250 | 0.07749 | 0.0025 | 0.019 | 0.032 |
| LZ-MJ | 9 | 0.757 | 0.261 | 0.08010 | 0.0024 | 0.018 | 0.031 |
| LZ-MJ | 10 | 0.764 | 0.266 | 0.08065 | 0.0024 | 0.018 | 0.031 |
| LZ-MJ | 11 | 0.759 | 0.265 | 0.07871 | 0.0023 | 0.018 | 0.030 |
| LZ-MJ | 12 | 0.782 | 0.279 | 0.07966 | 0.0023 | 0.018 | 0.031 |
| LZ-MJ | 13 | 0.782 | 0.285 | 0.08017 | 0.0024 | 0.018 | 0.031 |
| LZ-MJ | 14 | 0.783 | 0.285 | 0.08082 | 0.0023 | 0.018 | 0.031 |
| LZ-MJ | 15 | 0.773 | 0.311 | 0.08207 | 0.0024 | 0.019 | 0.032 |
| LZ-MJ | 16 | 0.773 | 0.312 | 0.08259 | 0.0024 | 0.019 | 0.032 |
| ML | 4 | 0.693 | 0.236 | 0.07146 | 0.0026 | 0.019 | 0.032 |
| ML | 8 | 0.753 | 0.294 | 0.07733 | 0.0027 | 0.020 | 0.035 |
| ML | 10 | 0.757 | 0.304 | 0.08087 | 0.0027 | 0.020 | 0.033 |
| ML | 15 | 0.762 | 0.331 | 0.08063 | 0.0027 | 0.020 | 0.034 |
| MM | 5 | 0.691 | 0.210 | 0.06894 | 0.0023 | 0.017 | 0.030 |
| MS | 6 | 0.715 | 0.232 | 0.06853 | 0.0027 | 0.020 | 0.035 |
| SDM | 2 | 0.740 | 0.145 | 0.06695 | 0.0022 | 0.013 | 0.020 |
| SDM | 3 | 0.775 | 0.184 | 0.07099 | 0.0022 | 0.016 | 0.026 |
| SDM | 4 | 0.767 | 0.212 | 0.07450 | 0.0026 | 0.015 | 0.024 |
| SDM | 6 | 0.766 | 0.232 | 0.07591 | 0.0030 | 0.016 | 0.029 |
| SDM | 7 | 0.773 | 0.255 | 0.08029 | 0.0028 | 0.020 | 0.034 |
| SDM | 8 | 0.759 | 0.268 | 0.07952 | 0.0028 | 0.021 | 0.035 |
| SDM | 10 | 0.764 | 0.310 | 0.08642 | 0.0026 | 0.019 | 0.031 |
| SDM | 11 | 0.800 | 0.329 | 0.08686 | 0.0027 | 0.019 | 0.033 |
| SDM | 12 | 0.801 | 0.332 | 0.08670 | 0.0026 | 0.020 | 0.034 |
| SDM | 13 | 0.800 | 0.335 | 0.08675 | 0.0027 | 0.020 | 0.034 |
| SDM | 14 | 0.795 | 0.332 | 0.08603 | 0.0027 | 0.020 | 0.034 |
| SDM | 20 | 0.770 | 0.331 | 0.08594 | 0.0026 | 0.019 | 0.033 |
| TD | 2 | 0.678 | 0.162 | 0.05673 | 0.0027 | 0.021 | 0.035 |
| TD | 3 | 0.679 | 0.162 | 0.05631 | 0.0025 | 0.020 | 0.034 |
| TD | 4 | 0.704 | 0.175 | 0.06090 | 0.0024 | 0.019 | 0.031 |
| TD | 5 | 0.718 | 0.185 | 0.06316 | 0.0023 | 0.018 | 0.032 |
| TD | 6 | 0.768 | 0.224 | 0.07772 | 0.0023 | 0.018 | 0.031 |
| TD | 7 | 0.740 | 0.237 | 0.08096 | 0.0023 | 0.018 | 0.031 |
| TD | 8 | 0.748 | 0.265 | 0.08159 | 0.0024 | 0.018 | 0.031 |
| TD | 9 | 0.737 | 0.278 | 0.08153 | 0.0025 | 0.019 | 0.032 |

TABLE IV: Results for all alphabets and matrices tested (continued)

|  |  | Recall at 0.01 EPQ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scheme | Letters | AUC MPP | Align | None Linear Quadratic |  |  |  |
| TD | 10 | 0.743 | 0.283 | 0.08033 | 0.0025 | 0.019 | 0.032 |
| TD | 14 | 0.743 | 0.306 | 0.07984 | 0.0026 | 0.020 | 0.034 |
| WW | 5 | 0.709 | 0.219 | 0.07172 | 0.0026 | 0.019 | 0.033 |

$\qquad$
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