Real time observations of single bacteriophage λ DNA ejections *in vitro*.

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Abstract

The physical, chemical, and structural features of bacteriophage genome release have been the subject of much recent attention. Many theoretical and experimental studies have centered on the internal forces driving the ejection process. However, it is still not known how quickly DNA exits under these forces or what limits the speed. Recently, Mangenot et al. (2005) reported fluorescence microscopy of phage T5 ejections, which proceeded stepwise between DNA nicks. This paper reports the first real-time measurements of ejection from phage lambda, revealing how the speed depends on key physical parameters such as genome length and ionic state of the buffer. Except for a pause before DNA is finally released, the entire 48.5 kbp genome is translocated in about 1.5 s without interruption, reaching a speed of 60 kbp/s. The process gives insights particularly into the effects of two parameters: a shorter genome length results in lower speed but a shorter total time, while the presence of divalent magnesium ions (replacing sodium) reduces the pressure, increasing ejection time to 8–11 s. Pressure caused by DNA-DNA interactions within the head affects the initiation of ejection, but the close packing is also the dominant source of friction: more tightly packed phages initiate ejection earlier but with a lower initial speed. The details of ejection revealed in this study are probably generic features of DNA translocation in bacteriophages and have implications for the dynamics of DNA in other biological systems.

1 Introduction

The transfer of bacteriophage DNA from a capsid into the host cell is an event of great importance to biology and physics. In biology, DNA ejection was the key piece of evidence demonstrating that the genetic material was DNA and not protein [1], phages have long been used to insert foreign genes into bacteria [2], and phage-mediated DNA transfer between species is a challenge to theories of evolution [3]. In physics, the translocation of DNA through a pore has been studied from the theoretical and experimental points of view [4, 5, 6, 7, 8]. Since phage DNA ejection is such a well-known example of this process, it is important to understand it from a quantitative point of view.

This paper addresses a longstanding, quantitative puzzle about phage DNA ejection: How fast is the ejection process? We use bacteriophage λ , a typical tailed phage, to answer this question. In a λ infection, first the phage tail binds to the *E. coli* outer membrane protein LamB, triggering ejection. Then the genome, 48.5 kbp of double-stranded DNA, moves out of the phage head, through the tail, and into the cytoplasmic space, which requires force on the DNA directed into the cell. A force of tens of piconewtons (pN) is produced by the highly bent and compressed DNA within the capsid [9, 10, 11], but not much is known about how fast the DNA transfer occurs, except that ejection reaches completion *in vivo* in less than two minutes [12]. One study used lipid vesicles incorporating LamB and filled with ethidium bromide—the DNA was ejected into the vesicles, causing an increase in fluorescence over about 30 s [13]. However, the ~1000 molecules of ethidium bromide in each vesicle were enough for only the first 1 kbp of DNA [14]. Also, since the ejections could have started at different times, that experiment says very little about the DNA translocation process. This paper aims to resolve these challenges in describing the λ ejection process.

An important insight from theory is that frictional forces limit the speed of ejection, due to DNA rearrangement in the phage head or sliding forces in the tail [15, 16]. Since the DNA is in a liquid state [17], we expect friction to behave at least somewhat like macroscopic hydrodynamic drag: stronger at higher speed or at smaller spacings between the

moving parts. The DNA-tail interaction does not change during the ejection process, so we expect friction in the tail to remain constant. In contrast, friction in the head should be stronger when the spacing between the loops of DNA is small, *i.e.*, at the beginning of ejection.

To quantify the rate of ejection, a single-phage technique is necessary. Single phage ejections were first observed with fluorescence microscopy on phage T5, revealing an effect of the unique structure of the T5 genome: nicks in the DNA resulted in predefined stopping points and a stepwise translocation process, with speeds that were too high to be quantified, so that further analysis of the speed and source of friction was not possible [18]. As we will show here, λ ejects its DNA differently from T5, following a continuous process that we can quantify with single-molecule measurements. This allows us to clarify the earlier vesicle-ejection results and to study the speed of the ejection process. In fact, knowing the forces involved in the λ ejection process makes λ an ideal subject for study at the singlemolecule level. By comparing the forces to the rate of ejection, we are able to quantify the friction and determine which source of friction actually dominates. Furthermore, we argue that only through systematic analysis of different phages is it possible to develop a complete picture of the DNA translocation process.

The key to checking quantitative ideas about bacteriophage ejection is to vary parameters that affect the process. Earlier, the genome length of λ was varied to investigate how it affects ejection force [11]. In this paper we exploit the same strategy, using genome length as a control parameter, but this time to control the ejection dynamics. We expected that the dynamics only depends on the amount of DNA within the capsid, not on the length of the genome that was originally enclosed. A second parameter is the ionic composition of the solution, since monovalent cations lead to higher pressures than divalent cations [19]. In fact, Mg²⁺ ions are commonly used to stabilize λ , but these ions are less important for the stability of mutants with shorter genomes [20]. Here we will compare a buffer containing Mg²⁺ to one containing Na⁺. The goal of the paper is to use these tunable parameters to dissect the DNA translocation process.

The paper is organized as follows: in the Results section we describe what we have observed about λ ejection using our single-molecule assay. In the Discussion we analyze these results from a quantitative perspective, looking specifically at what they can tell us about the source of friction during ejection. We conclude by summarizing what we have learned about the ejection process, with recommendations for further experiments and theoretical work. Detailed procedures are give in the Methods section. Videos, information about the computer algorithm used to analyze the data, and additional discussion of the experimental technique are available in the Online Supplement.

2 **Results**

To reveal details of the λ ejection process, we measured the rate of ejection as a quantitative velocity with units of kbp/s, following recent work in which single phage T5 ejections could be seen by fluorescence microscopy [18]: The λ capsids were bound to a microscope coverslip and washed with a dye/LamB solution to initiate ejection, with a high enough dye concentration to stain the DNA immediately after ejection. An oxygen-scavenging system reduced photodamage, allowing high frame-rate (4 s⁻¹) real-time measurement of the amount of DNA leaving the capsid. (See Methods for details.)

As mentioned in the introduction, we can compare our results to models of the ejection process by varying the phage genome length and ion type. The genome length dependence was addressed by using two λ mutants, λ b221 (38 kbp) and λ cI60 (48.5 kbp), which together represent a range close to the maximum allowable range of DNA lengths for λ [21]. To gain an understanding of the effects of various ions on the ejection process, we compared ejection in two buffers, with either Mg²⁺ or Na⁺ ions at a concentration of 10 mM (see Methods.) What we expected to see is that the force driving ejection is significantly reduced in the Mg buffer as compared to the Na buffer. These ions are significantly less concentrated than those within an *E. coli* cell, but the cytoplasmic concentrations are not relevant for the ejection process, which takes place when the capsid is bound to the outer surface of the cell.

Figure 1 shows real-time views of genome ejection from λ . A total of 81 such single-molecule trajectories were selected from the video data and processed, representing different solution conditions, flow rates, and genome lengths. For each set of experimental conditions, the ejection followed a reproducible trajectory: except for experimental noise or photodamage, there were no apparent differences between events, as shown in Figure 2. Figure 3 shows the speed of the ejection process. As these graphs show, the translocation of DNA reaches a high rate but slows as it approaches a maximum extension near 100% ejection, after a total of 1–11 s. This is to be contrasted with the T5 genome, which

exhibited multiple random pauses during the ejection process [18]. At its maximum extension, however, the λ DNA remained attached for a random amount of time, seconds to minutes, often a long enough time that it was destroyed by photodamage before the release could be measured. Just as the pauses in the case of T5 were due to a feature of the T5 genome, this effect could be due to a unique feature of the λ genome: the 12 bp overhang at the end of the DNA might form non-specific hydrogen bonds with the capsid protein. However, the present experimental technique does not have the resolution to address exactly how large the piece of DNA remaining within the capsid is.

Another important feature of the ejection process is the waiting time before translocation begins. Though all ejections proceed nearly identically once they have started, λ exhibits a random waiting time of seconds to minutes, during which time no visible DNA has emerged from the capsid. Figure 4 shows the number of ejections that have been triggered as a function of time, with exponential fits to determine the approximate time constant t_0 of the waiting process.

3 Discussion

The previous section described the general features of the λ ejection process: a stochastic initiation process followed by a continuous, reproducible translocation. Now we will discuss the quantitative details in light of recent theories that model the phage genome, predicting the forces that will be produced by compressed DNA during ejection, as shown in Figure 5.

For DNA translocation to initiate, some kind of molecular door that blocks the exit of the DNA must first open. Figure 4 shows that the parameters known to affect pressure and velocity affect the waiting time before ejection, denoted by t_0 . For example, in Na buffer, λc I60 has $t_0 = 79$ s and λb 221 has $t'_0 = 166$ s. The exponential nature of the waiting time distribution indicates that the initiation of ejection is a one-step kinetic process, in which case the Arrhenius relation holds:

$$\exp\left((E' - E)/k_{\rm B}T\right) = t_0'/t_0 = 2.1\,,\tag{1}$$

where E and E' are the energies of the transition state for initiation of ejection in the two phages. This results in

$$E' - E = 3.1 \,\mathrm{pN}\,\mathrm{nm}\,.$$
 (2)

As shown in Figure 5, the force F on the DNA with 48.5 kbp of DNA in the capsid is predicted to be 36 pN, while with 38 kbp of DNA it is 23 pN. How could the transition state energy be coupled to F? In the transition state, the door may be partially open, having moved a distance Δx along the phage axis. In that case, we find

$$E' - E = \Delta x \cdot (F - F'); \qquad (3)$$

$$\Delta x = 0.24 \,\mathrm{nm}$$

This value of Δx has the right order of magnitude for a transition that involves, for example, the breaking of hydrogen bonds, suggesting that the waiting time distribution can tell us about the mechanics of the initiation process. However, we do not have enough data here to make a claim about exactly what this process is.

After initiation, the DNA begins translocation through the phage tail, proceeding continuously with a varying speed until the entire genome has exited. We would like to understand the details of this process, with particular attention to the source of friction that limits the speed of translocation. Figures 1 and 2 show that the presence of Mg^{2+} has a dramatic effect on the overall speed, with λ cI60 taking about 1.5 s to eject its DNA in Na buffer, which should be compared to 8–11 s in Mg buffer. The most obvious interpretation of this result, in agreement with the findings of bulk DNA pressure measurements [19], is that the higher pressure in Na buffer is responsible for the faster ejection. However, this simplistic view is not entirely correct, as we discuss below.

Figure 3 shows v for each set of parameters. As expected, v is a function only of the ionic conditions and the amount of DNA inside the capsid, independent of the original genome length. The graph shows that the maximum v is actually reached at an intermediate stage of ejection, while it is reduced by about 50% when the capsid is fully packed. The maximum of F is when the capsid is fully packed, so we know that v cannot simply be proportional to F. This suggests a modification to the simplistic idea of v being proportional to the force F with which the DNA is being ejected. The ratio of the two values is called the *mobility*, which we denote by μ :

$$\mu = v/F. \tag{4}$$

Apparently, μ depends on the amount of DNA within the capsid. A reasonable interpretation is that when the capsid is fully packed, contact between strands of DNA or the capsid walls reduces μ , slowing translocation below the maximum. It is possible that μ will be different for Na and Mg buffers, because of the ability of Mg²⁺ ions to bind to two sites at once.

In Figure 5 we plot μ as a function of the amount of DNA within the capsid, showing that the value of μ strongly depends on the amount of DNA in the capsid, decreasing to about 1% of its initial value as the phage becomes fully packed. In fact, over most of this range, μ is independent of all parameters except for the amount of DNA in the capsid. As discussed in the introduction, this dependence on DNA density strongly points to friction originating from hydrodynamic drag within the phage head rather than in the phage tail. The question now becomes whether we can understand the magnitude of μ theoretically. However, two challenges limit the development of models: First, the DNA remaining in the capsid will rearrange as it becomes progressively less dense; it is important to know how its structure changes to estimate how fast these changes can occur. The second is that the forces between DNA strands, water, ions, and the protein capsid are not well understood and are particularly difficult to calculate for the interaction of DNA with the narrowest part of tail. As a result, most theoretical modelers have "deliberately avoided" explicit calculations of the timescale of DNA translocation [15, 16, 22, 23]. We believe that the data presented here will encourage the development of models that can quantitatively account for the actual ejection velocity.

In this paper we have shown that the ejection of DNA from bacteriophage λ can reach speeds of up to 60 kbp/s, consistent with what is known about the translocation speed in T5 [18] and clarifying an earlier bulk experiment [13]. This assay provides a quantitative way to look at parameters that might affect the ejection process: here we have examined the effects of ions and the phage genome length, comparing them to expectations from theory. Other factors could be incorporated into the assay, such as external osmotic pressure, DNA-condensing agents, or DNA-binding proteins, in an effort to develop a better theoretical understanding of the ejection process. Additionally, since we have seen the ejection process from so many different points of view in λ , it would be interesting to know more about the forces and dynamics of DNA packaging in that phage. The ejection assay could also be replicated with other phages, to provide points of comparison to λ . In particular, ϕ 29 has been shown to experience forces of up to 100 pN during packaging; its ejection could be significantly different than that of λ [24, 25].

Finally, it should be noted that the DNA ejection process *in vivo* may be quite different from what we observe here, due to osmotic pressure in the bacterial cytoplasm and the presence of proteins that can bind to and actively translocate DNA. No matter how high the internal force is when a phage is fully packed, it will drop to zero as the DNA exits the capsid, so it can not be sufficient to complete ejection against the internal osmotic pressure of *E. coli*, which produces an outward force of several pN [11]. Several other forces potentially playing a role include: proteins such as RNA polymerase that bind to DNA and produce an effective inward force by translocation or ratcheting [26], channels opened during the ejection process that allow water to rush in and produce drag on the DNA [27], and even molecular motors found in the phage capsid [28]. For λ , it is not known what part of the process depends on the pressure in the capsid and what part relies on active transport. Further work to visualize the ejection process *in vivo* is probably the only way that this information could be revealed.

4 Methods

Buffers and strains

Several buffers were used for *in vitro* ejection: Na buffer (10 mM Tris, 10 mM NaCl, pH 7.8) was considered representative of buffers containing 100% monovalent cations, while Mg buffer (10 mM Tris, 10 mM MgSO₄, pH 7.8) was considered representative of buffers containing \sim 100% divalent cations. TM buffer (50 mM Tris, 10 mM MgSO₄, pH 7.4) was used in earlier ejection experiments [9, 11]; we use it here for the preparation of the phages and also check in this work that it is equivalent to Mg buffer for ejection; the excess Tris appears not to contribute a significant number of monovalent ions to the solution. Finally, buffer A (50 mM Tris, 50 mM NaCl, 5 mM MgSO₄) was used earlier for experiments on the DNA packaging process [24]. Because of the ten-fold excess of NaCl, it is not clear which type of ion will dominate within the bacteriophage capsid. We found, in fact, that buffer A had an intermediate behavior: calibration DNA behaved identically to DNA in Mg buffer, but DNA translocation required about 4 s, between the values for the Na and Mg buffers (data not shown.)

Phages λ b221cI26 (λ b221) and λ cI60 were extracted from single plaques and grown on *E. coli* C600 cells with the plate-lysis method on 50mL supplemented tryptone-thiamine plates (20 g/L agar, 10 g/L tryptone, 5 g/L NaCl, 2.5 g/L MgSO₄, 13 mg/L CaCl₂, 20 mg/L FeSO₄, 2 mg/L thiamine), which were covered with 20 mL TM buffer after confluent lysis and incubated at room temperature for several hours or 4°C overnight. Phages were then purified by differential sedimentation and equilibrium CsCl gradients, resulting in 10¹²–10¹³ infectious particles, as determined by titering on LB agar. After purification, the CsCl buffer was replaced with TM using 100,000 MWCO spin columns (Amicon).

The λ receptor LamB (maltoporin), required to trigger ejection, was extracted from the membranes of *E. coli* pop154 cells: these cells express a *lamB* gene from *S. sonnei* known to be compatible with a variety of λ strains, allowing ejection in the absence of chloroform [29, 30]. An overnight culture was sonicated, then the membranes were pelleted, homogenized, and washed in 0.3% n-octyl-oligo-oxyethylene (oPOE; Alexis Biochemicals #500-002-L005) at 40°C for 50 min. A second wash was performed in 0.5% oPOE, followed by extraction in 3% oPOE at 37°C. LamB was affinity-purified in amylose resin and spin-filtered to replace the buffer with TM buffer containing 1% oPOE. Based on the sequence of LamB, it follows that a 1 cm absorbance of 1.0 at 280 nm corresponds to 0.34 mg/ml of protein, which we use for computing LamB concentrations in the experiment. Accordingly, from 2 L of cells we were able to obtain at least 1 mg of protein, enough for many ejection experiments.

Single molecule measurement

Our single molecule ejection assay essentially uses an earlier technique [18], with modifications for use with phage λ . A 5 mm wide, 120 μ m thick channel was constructed from double-sided adhesive sheets (Grace Biolabs). The channels were produced with laser cutting to assure reproducible dimensions (Pololu Corporation). Tygon tubing (inner diameter: 0.02 in) was epoxied to holes at each end of a glass slide. Before each observation, we cleaned a #1 coverslip by heating to 95°C in 0.5% Alconox detergent for 30–60 min, rinsing twice with water, and drying in a stream of air. Chambers were assembled, placed on a warm hot-plate for several seconds to seal, and used immediately after cooling. This cleaning process is critical for good imaging, and we noticed a significant degradation in image quality due to SYBR Gold/protein/glass interactions if the chambers were used just a few hours later.

Mg buffer containing 10^{10} pfu/mL λ cI60 or λ b221 was incubated with 4 µg/mL DNase I at 37°C for 15 minutes to remove any prematurely released DNA. As a focusing aid, 0.1 µm fluorescent beads were included at a dilution of ~ 10⁷. This phage-bead solution was added to the chamber and left at room temperature for 15 min or more, to allow the phages and beads to adhere to the surface of the coverslip. Then, at the microscope, the left end of the channel was coupled to a reservoir and the right end to a syringe pump, allowing a controlled left-to-right fluid flow along the channel that stretched out the DNA for visualization. To make the observations, the following three solutions were drawn through in succession: First, 800 µL Mg or Na buffer containing 1% oPOE, to wash away unbound phage particles. Second, 40 µL of the same Mg or Na buffer plus 1% oPOE, 10⁻⁵ diluted SYBR Gold, and an oxygen-scavenging system: 1% gloxy (gloxy: 17 mg glucose oxidase, SIGMA G2133-10KU, 60 µL catalase, Roche 10681325, in 140 µL Mg buffer), 0.4% glucose, and 1% β -mercaptoethanol [31]. Third (after sufficient dye was present for observation of the earliest ejections) the same buffer with 2.5 µg/mL LamB added.

Single ejections were observed on an Nikon inverted microscope using a 100x, 1.4 NA oil immersion objective at ambient temperature ($\sim 28^{\circ}$ C). The illumination source was a 100W mercury lamp, used at full intensity. Images were acquired at 4 s⁻¹ with a Photometrics Coolsnap FX camera. Example movies are available in the Online Supplement.

Many individual DNA ejections were visible in each acquired image sequence. Before analysis, each ejection was checked for various artifacts that would interfere with processing: overlap with other strands or the edge of the field of view, sticking of DNA ends to the glass, or breaking of the DNA strand. Overlap is unavoidable, while the sticking and breaking were caused by the intense illumination and greatly ameliorated by the oxygen-scavenging system. The ejections were analyzed using a custom difference-of-gaussians filter running within the GNU Octave programming language: for each frame, the program identified the shape of the DNA and recorded its extension in the direction of the flow. See Supplement A for details of the image processing routine, including source code.

Lengths were calibrated using λ DNAs tethered to specially prepared chambers. The goal was to examine the function that relates the size of a DNA image in pixels to three variables: its length in base pairs, the flow rate, and the ionic composition of the solution. We obtained λ DNA (New England Biolabs) and modified it using Klenow

exo⁻ (New England Biolabs) to add biotin-11-dUTP (Roche) to one end, as a length standard equivalent to an entire piece of ejected DNA from λ cI60. Other length standards were then prepared by digesting aliquots of the DNA with restriction enzymes (EcoRI, BspHI, BsrGI, KpnI) to create a range of fragment lengths (3.5, 7.9, 16.0, and 29.9 kbp). For the flow rate dependence, the DNAs were attached to streptavidin (Sigma) on the surface of a coverslip, and flows of various magnitudes were applied. Images were collected and analyzed identically to the images from the ejection videos. It was found that the DNA fit well to the form

extension = 460 nm + 0.34 nm/bp
$$\cdot \left(L - L_0 \cdot (1 - e^{-L/L_0}) \right)$$
, (5)

where 460 nm was the minimum feature size observable by our technique and L is the length of the DNA fragment in base pairs. The parameter L_0 is a function of flow rate; at $L = L_0$ the DNA is stretched out to 37% of its contour length by the flow. When $L \ll L_0$, there is no observable stretching, and when $L \gg L_0$, the DNA will appear shorter than its actual length by L_0 . The equation we used for fitting is not derived from any physical principles; it is just intended to be a smooth curve having the above properties without introducing any parameters other than L_0 . We found $L_0 = 18$ kbp for Mg buffer and 8 kbp for a flow rate of 40 μ L/min. This flow was determined to have no significant effect on the ejection process (see Supplement B) so it was used throughout the experiment. We note that the physics of tethered DNA in a shear flow is an interesting physical problem in its own right which may have interesting dynamics that would not be completely captured by a time-independent expression like Equation 5 [32].

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- [33] Inamdar, M. (2007) Private communication. Calculations using the parameters for both buffers were run according to the method of Purohit et al. (2003), using values $F_0 = 12,000 \text{ pN/nm}^2$; c = 0.30 nm for Mg buffer and $F_0 = 660 \text{ pN/nm}^2$; c = 0.52 nm for Na buffer, based on fitting to experimental data from Rau and Parsegian (1984). The calculations for magnesium buffer were identical to those reported earlier (Grayson, 2006).

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- 1 Top: time series of single genome ejections from λ cI60, taken at a frame rate of 4 s⁻¹. The upper frame shows ejection in buffer with 10 mM NaCl, which is significantly faster than ejection in 10 mM MgSO₄, shown below that. The 16 μ m scale bar is approximately the contour length of a 48.5 kbp piece of DNA. Bottom: graph of the length of the DNA that has emerged from the capsid at each time point, as computed using a computer image-processing algorithm together with DNA length standards as described in the text.
- 2 Graphs of ejection trajectories, comparing NaCl and MgSO₄ buffers and two genome lengths. Single ejection events were analyzed as described in the text, resulting in trajectories giving the length of DNA out of the capsid as a function of time. These trajectories are aligned and plotted for visual comparison; the offset of the starting time of the ejection is not used in further analysis. The graphs show that ejection proceeds on a timescale of about 1 s in NaCl buffer, or about 10 s in MgSO₄ buffer. The ejection speeds of phages with different genome lengths appear similar in this view.

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- 5 The relationship between force and velocity. Top: force on the DNA, as a function of the amount of DNA left within the capsid, according to theoretical calculations [33]. The force in Na buffer is much higher than that in Mg buffer. Bottom: computed mobility coefficient μ , showing the relationship between DNA packing within the capsid and its friction. The graph shows that μ generally decreases with increasing DNA density. For low concentrations of DNA, μ is much higher for Na buffer than for Mg buffer. However, with more than ~20 kbp in the capsid, μ becomes independent of the type of buffer. The value of μ appears to decrease almost to zero when 100% of the DNA is packed. 13



Figure 1: Top: time series of single genome ejections from λ cl60, taken at a frame rate of 4 s⁻¹. The upper frame shows ejection in buffer with 10 mM NaCl, which is significantly faster than ejection in 10 mM MgSO₄, shown below that. The 16 μ m scale bar is approximately the contour length of a 48.5 kbp piece of DNA. Bottom: graph of the length of the DNA that has emerged from the capsid at each time point, as computed using a computer image-processing algorithm together with DNA length standards as described in the text.



Figure 2: Graphs of ejection trajectories, comparing NaCl and $MgSO_4$ buffers and two genome lengths. Single ejection events were analyzed as described in the text, resulting in trajectories giving the length of DNA out of the capsid as a function of time. These trajectories are aligned and plotted for visual comparison; the offset of the starting time of the ejection is not used in further analysis. The graphs show that ejection proceeds on a timescale of about 1 s in NaCl buffer, or about 10 s in MgSO₄ buffer. The ejection speeds of phages with different genome lengths appear similar in this view.



Velocity of ejection

Figure 3: Averaged speeds of DNA ejection for λ cI60 and λ b221. The plot shows the DNA ejection speed as a function of the amount of DNA within the capsid, averaged in bins of width 2.5 kbp. Error bars are plotted based on the standard deviation of the speed across all analyzed ejections; there may be additional systematic deviations in all curves. The curves for phages of different genome lengths lie close to each other, while most of the variation is caused by the difference in buffer conditions. A maximum of about 60 kbp/s is reached in NaCl buffer, while the maximum in MgSO₄ buffer is about 17 kbp/s.



Figure 4: The number of ejections that have been triggered as a function of time. For each experiment, the total number of ejections that had been observed was plotted as a function of time; these are the same ejections that were used for the analysis above. Also plotted are exponential least-squares fits of the form $a(1 - \exp(-t/t_0)) + b$, where t_0 is the time constant of triggering. To take into account the delay before LamB entered the flow chamber, we set t = 0 at the time of the first observed ejection.



Figure 5: The relationship between force and velocity. Top: force on the DNA, as a function of the amount of DNA left within the capsid, according to theoretical calculations [33]. The force in Na buffer is much higher than that in Mg buffer. Bottom: computed mobility coefficient μ , showing the relationship between DNA packing within the capsid and its friction. The graph shows that μ generally decreases with increasing DNA density. For low concentrations of DNA, μ is much higher for Na buffer than for Mg buffer. However, with more than ~20 kbp in the capsid, μ becomes independent of the type of buffer. The value of μ appears to decrease almost to zero when 100% of the DNA is packed.

Real time observations of single bacteriophage λ DNA ejections *in vitro*.

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Supplement A. Image processing.

Recorded movies of DNA ejection experiments were analyzed in two steps: First, ejections judged "good" (no DNA sticking to the slide, overlapping, or obvious photodamage) were manually selected from the movies, and 20 s of video, starting from the beginning of ejection, was converted into individual cropped image files. Second, these files were analyzed by a computer subroutine that automatically measured the length of the DNA using a *Difference-of-Gaussians* (DOG) filter [1, 2].

The DOG filter is used as a convenient approximation to the *Laplacian-of-Gaussian* (LOG) filter, an edge-detection algorithm that works as follows: We start with a raw image \mathcal{I} that contains a certain amount of noise. The image is smoothed with a Gaussian filter, which we denote by $\mathcal{G}(\sigma)$. The standard deviation of the filter, σ , must be selected so that the filter erases most of the noise. Then, the Laplacian $\mathcal{L} = \nabla^2$ is applied to compute the curvature, which we denote by \mathcal{C} . Mathematically,

$$\mathcal{C} = \mathcal{L}(\mathcal{G}(\sigma) * \mathcal{I}) = (\mathcal{L}\mathcal{G}(\sigma)) * \mathcal{I},$$
(1)

where * represents the convolution operation. The final form of this expression follows because both \mathcal{L} and $\mathcal{G}(\sigma)$ are linear: thus the LOG filter can be represented as a convolution of a single function, $\mathcal{L}\mathcal{G}(\sigma)$ with the image.

This function is closely approximated by the difference of two Gaussians with slightly different values of σ

$$\mathcal{L}\mathcal{G}(\sigma) \approx \mathcal{G}(\sigma) - \mathcal{G}(1.6\,\sigma),$$
(2)

which we call the DOG filter. In Fourier space, this convolution can be computed more efficiently as a product:

$$\tilde{\mathcal{C}} = \left(\tilde{\mathcal{G}}(\sigma) - \tilde{\mathcal{G}}(1.6\,\sigma)\right) \times \tilde{\mathcal{I}}\,. \tag{3}$$

The value of C is expected to change sign at edges, so by thresholding, the shape of the DNA may be extracted from the image. The following code, written in the Octave language, was used to apply the DOG filter to images and find the length of the given piece of DNA.

```
function [mylength] = find_length(img,sigma)
w = size(img)(2);
h = size(img)(1);
## generate the filter function
g1 = zeros(h,w);
g2 = zeros(h,w);
for i=1:h
for j=1:w
ii = min(i-1,h+1-i);
jj = min(j-1,w+1-j);
```

```
g1(i,j) = exp(-(ii**2+jj**2)/(2*sigma**2));
      g2(i,j) = exp(-(ii**2+jj**2)/(2*(sigma*1.6)**2));
    end
  end
  g1 /= sum(sum(g1));
  q2 /= sum(sum(q2));
  dog = q1-q2;
  ## compute the curvature, C
  dog_f = fft2(dog);
  img_f = fft2(img);
  C = real(ifft2(img_f.*dog_f));
  ## compute the thresholded image, T
  cutoff = 0.2 * max(max(C));
  T = curvature > cutoff;
  . . .
  mylength = rightedge - leftedge;
end
```

The removed section . . . finds the left and right edges of the largest region in the image. Figure 1 shows an example of the effect of the DOG filter, applied to image series from the text. As the figure shows, the size of small pieces of DNA is slightly exaggerated by a filter with a large value of σ , and the smallest pieces were entirely lost. We found that by reducing σ iteratively for smaller pieces of DNA, these problems could be eliminated.

Supplement B. Effect of flow.

In this section we present a brief theoretical treatment of the effect of flow and an additional plot in support the claim that the dynamics of DNA translocation is determined primarily by internal pressure rather than force from the flow.

As discussed in the text, one model for the state of a tethered piece of DNA in a shear flow is that there is a ball of unstretched DNA of length L_0 at the free end. The ball experiences a force from the flow; this force is what causes the remained $L - L_0$ of the DNA to be stretched out. We can use the Stokes formula to approximate this force:

$$F_{\rm flow} = 6\pi\eta r v\,,\tag{4}$$

where r is the radius of the ball and v represents the average flow velocity over the ball. This force stretching out the DNA is balanced against its tendency to form a random coil: approximately 1 k_BT of free energy is required for each persistence length ξ of DNA. Balancing the forces, we find

$$F_{\rm flow} \approx 1 \, k_{\rm B} T / \xi \approx 0.1 \, \text{pN} \,,$$
(5)

independent of the size of the ball. This force is trivial compared to the 10–40 pN of internal force found in λ , so we do not expect it to make a significant difference.

Figure 2 shows that when flow velocity is reduced by a factor of four, there is no significant change in the ejection process, indicating that the presence of a flow does not have an important effect on ejection. Additionally, Figure 3 compares the velocity of ejection under both flow rates, binned according to the method described in the text. What Figure 3 shows is that the translocation velocity is not increased under a stronger flow. In fact, for several data points, the translocation appears faster under the weaker flow. We believe that the faster points are due to the high fluctuations that are observed in a weak flow: in particular, the DNA tether calibration at 14 s^{-1} did not fit our model as well as it did at 57 s⁻¹ (data not shown.) Our conclusion is that 57 s⁻¹ is a value that allows the DNA to be stretched out sufficiently to limit fluctuations, but without significantly affecting the translocation process.

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Figure 1: Three steps in analyzing images of ejected DNA fragments. Top: the original image captured on the camera. Middle: the result of applying the DOG filter, referred to as image C in the source code. A smoothing factor $\sigma \approx 0.5 \ \mu$ m was used. Bottom: the thresholded image, image T in the source code.



Figure 2: Graphs of the single ejection trajectories, showing the effect of the flow on the DNA. A four-fold change in the flow velocity appeared to have no effect on the ejection of DNA in $MgSO_4$ buffer. However, the data with a slower flow has an increased noise due to greater fluctuations of the DNA.



Figure 3: Comparison of the velocity of DNA translocation at two different flow rates: 10 and 40 μ L/min, corresponding to shear flows of 14 and 57 s^{-1} , respectively. Except for several points during the middle of ejection, the velocities at both flows correspond closely, and even for the points that do not match, translocation appears faster in the slower flow. The red line indicates the position of the full-length genome, 48.5 kbp.

List of Tables

1 Calibration for various flow rates and buffers. The length L_0 of DNA that stretches out to 37% of its contour length was measured as described in the text. Mg buffer had an L_0 about twice as high as Na buffer, while the flow rate also had a large effect on the value. Additionally, it was noted that other buffers containing Mg²⁺ (TM buffer, buffer A) were equivalent to Mg buffer, indicating that it is the presence of Mg²⁺ rather than the absence of Na⁺ that causes the DNA to be more flexible.

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buffer	flow (μ L/min)	shear (s^{-1})	L_0 (kbp)
Mg	10	14	45
Na	10	14	25
Mg	40	57	18
Na	40	57	8

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